

"MoPro" : a free software for electron density analysis.
of small compounds and biological macromolecules.

Laboratoire de Cristallographie & Résonance Magnétique
& Modélisations (CRM2)

Christian Jelsch

CNRS Nancy Université France

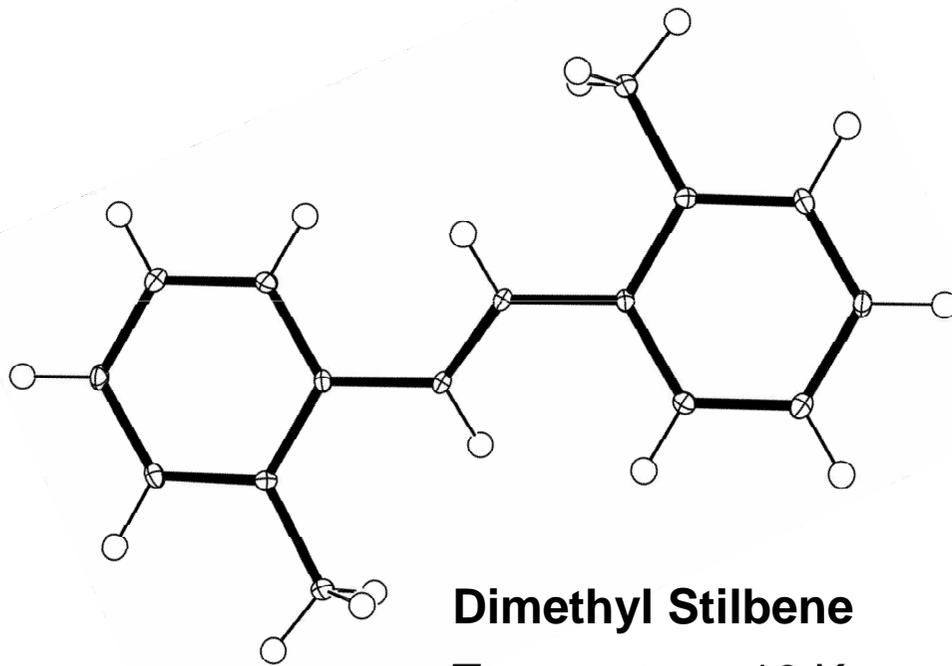


ANGD Reciproc 14 sept. 2011 Aussois

- * Charge density refinement with MoPro
- * VMoPro visualisation tool of properties
- * Database Transfer
- * Application to proteins
- * Electrostatic Interaction Energy

Spherical Atom Model : approximation

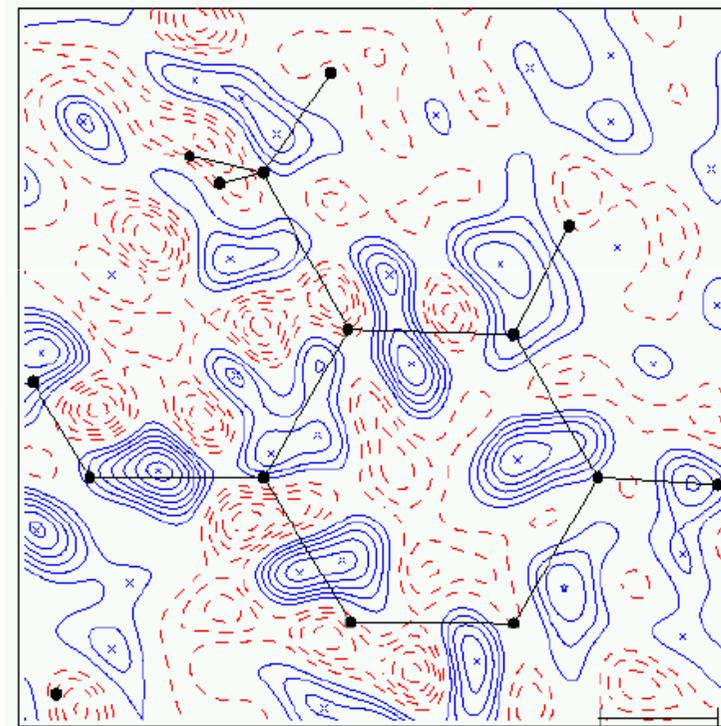
Fourier Residual Map $F_{\text{obs}} - F_{\text{cal}}$



Dimethyl Stilbene

Temperature 16 K

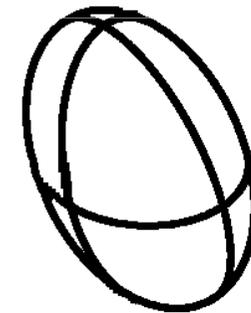
Resolution 0.65 Å



RESOLUTION & X-Ray CRISTALLOGRAPHY

Proteins *X Y Z* Molecular Structure
d ≈ 2 Å Thermal *B* factor isotropic

ATOMIC Thermal *B* anisotropic
d ≈ 1 Å Hydrogen



SUB-ATOMIC Deformation Electron Density
d ≈ 0.5 Å Atomic Charges

Multipolar Atom Model

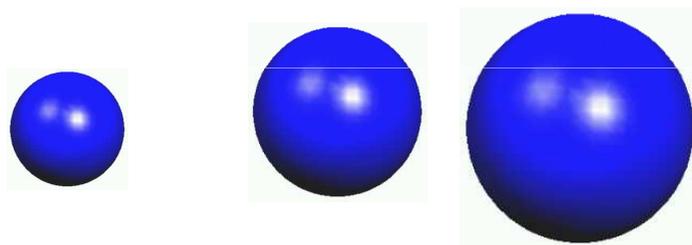
$$\rho(\mathbf{r}) = \rho_c(r) + P_{\text{val}} \kappa^3 \rho(\kappa) + \sum \kappa'^3 R(\kappa' r) \sum P_{\text{lm}} Y_{\text{lm}}$$

Atom

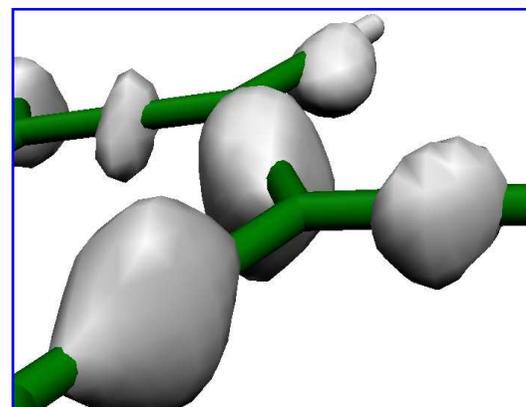
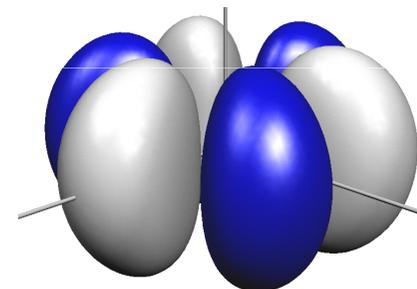
core

Valence
Population

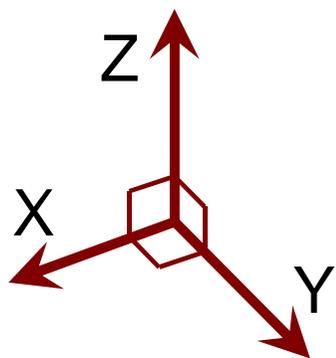
Multipole
Populations



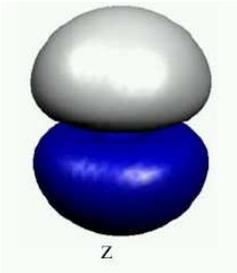
κ κ' expansion
/ contraction



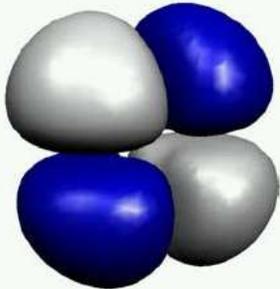
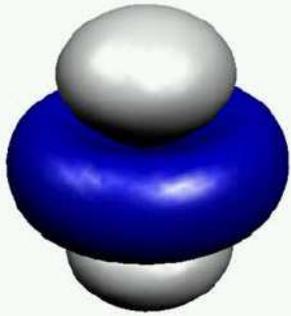
Hansen & Coppens
(1978) *Acta Cryst.* A34, 909



3 dipoles



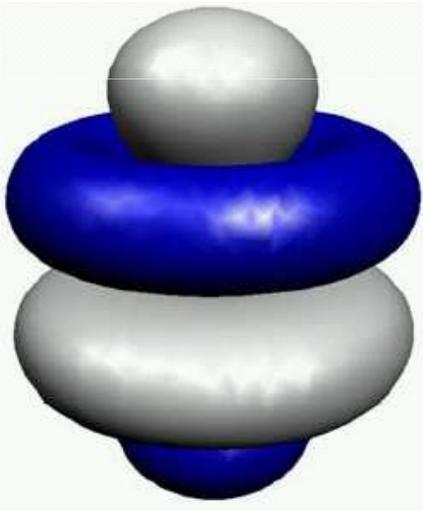
5 quadripoles



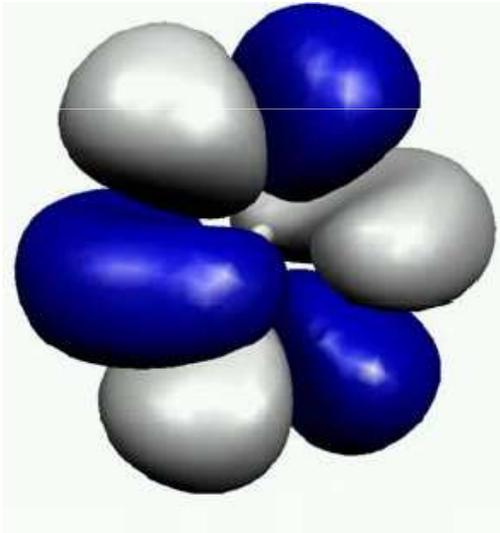
$2z^2-(x^2+y^2)$

xz

7 octupoles



$2z^3 - 3z(x^2+y^2)$

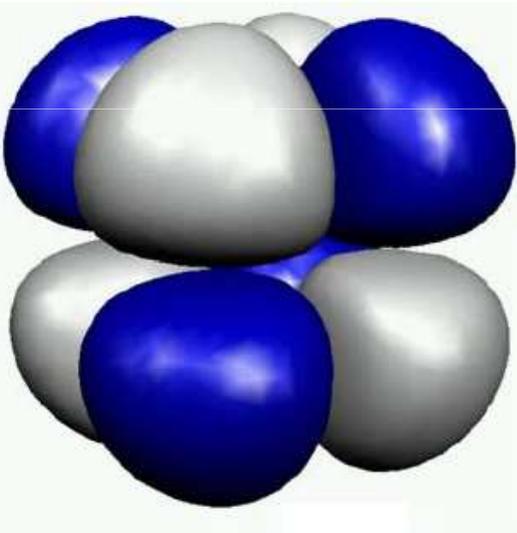


$x[4z^2 - (x^2+y^2)]$

$y[4z^2 - (x^2+y^2)]$

$x(x^2 - 3y^2)$

$y(y^2 - 3x^2)$

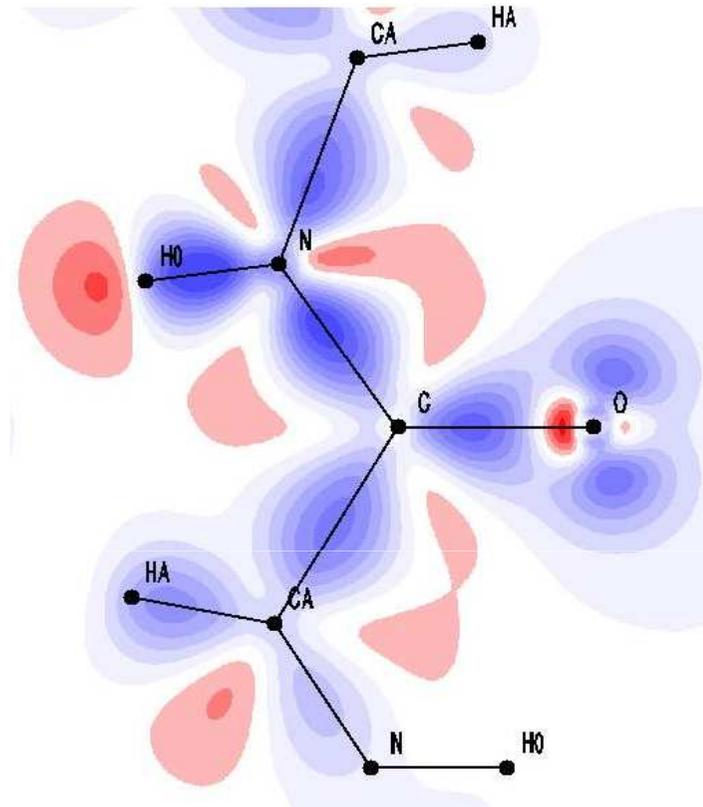


xyz
 $(x^2-y^2)z$

Deformation of Electron Density

+/- 0.05 e/A³

Multipolar
Atom
Model

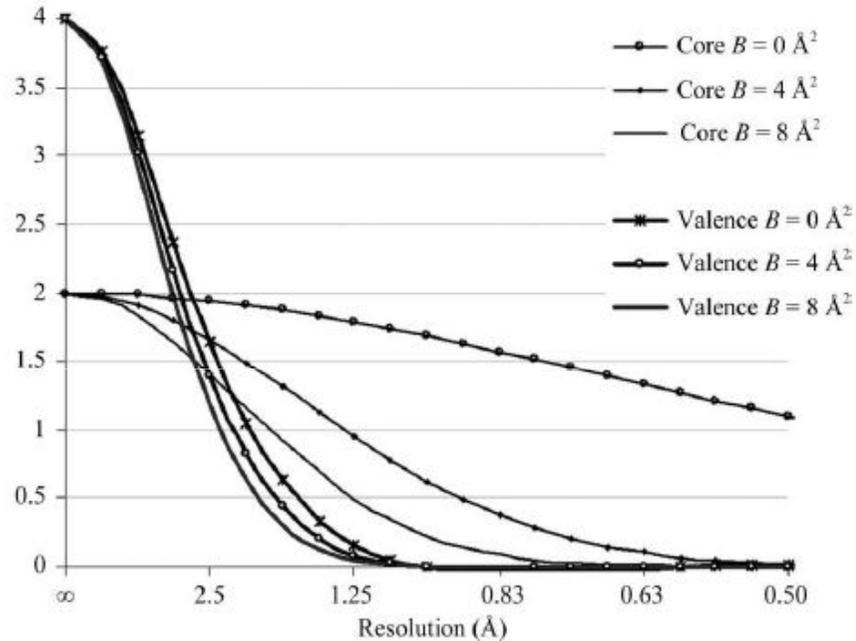


$$\Delta\rho(\mathbf{r}) = \rho_{\text{molecule}} - \sum \rho_{\text{atoms_spherical_neutral}}$$

$$= (N_{\text{val}} - P_{\text{val}}) \kappa^3 \rho(\kappa) + \sum \kappa^3 R(\kappa, r) \sum P_{lm} Y_{lm}$$

High Order Refinement

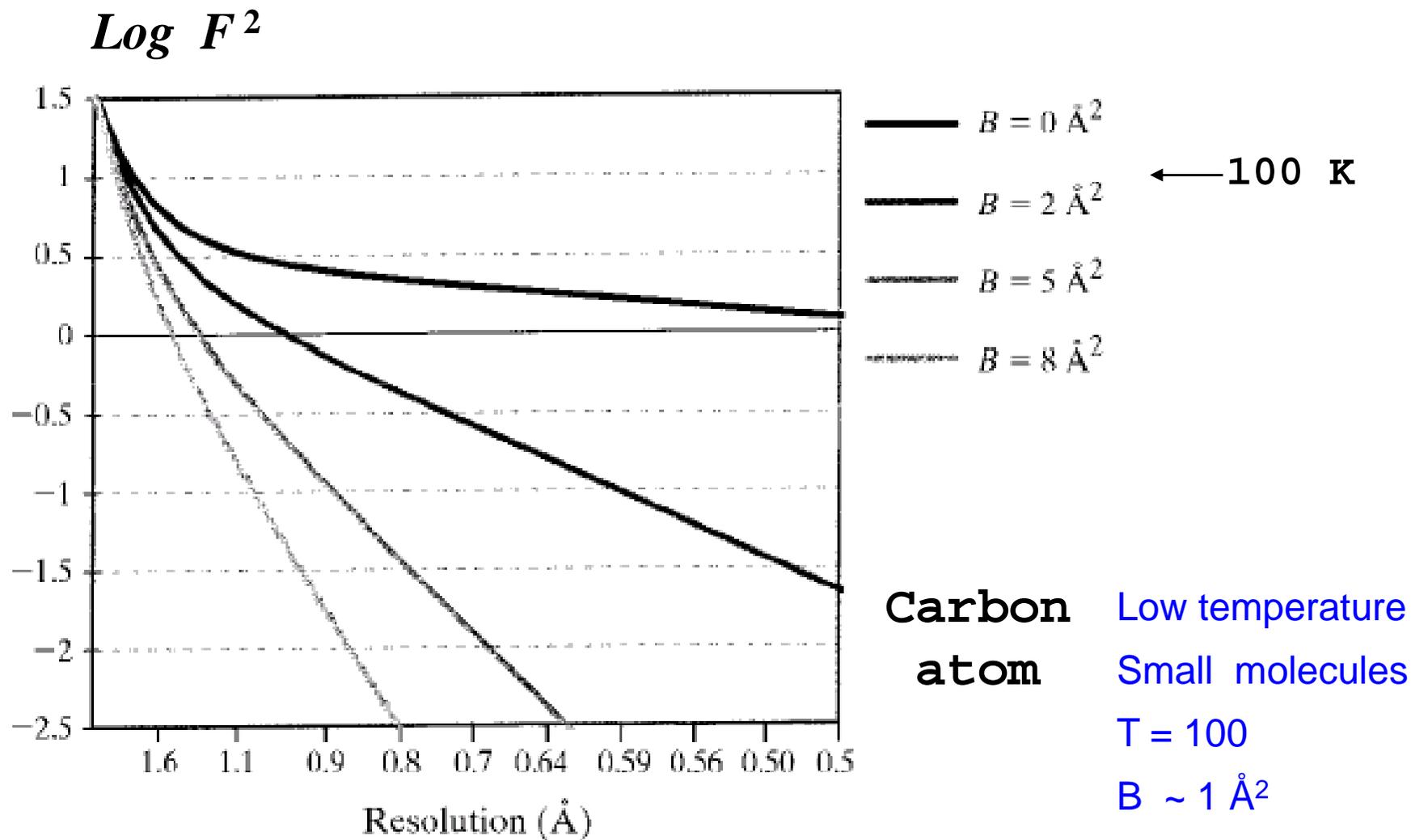
Scattering factor of a carbon atom



Refine vs. Reflections at **High resolution**

Deconvolution of thermal motion
& deformation density

Diffraction Power & Temperature Factor



MOPRO Crystallographic Refinement Software



Subatomic Resolution Structure & Electron Density

~0.5Å

Atomic Resolution Structure with Hydrogen Atoms

0.7 – 1.5 Å Transfer Databank Electron Density

Small Compounds & Macromolecules

Guillot *et al.*, J. Appl. Cryst. (2001) 34, 214-223

Jelsch *et al.*, J. Appl. Cryst. (2005) . 38, 38-54

MoProSuite : the main programs

- * **MoProGUI.jar**

- * **Import2MoPro**

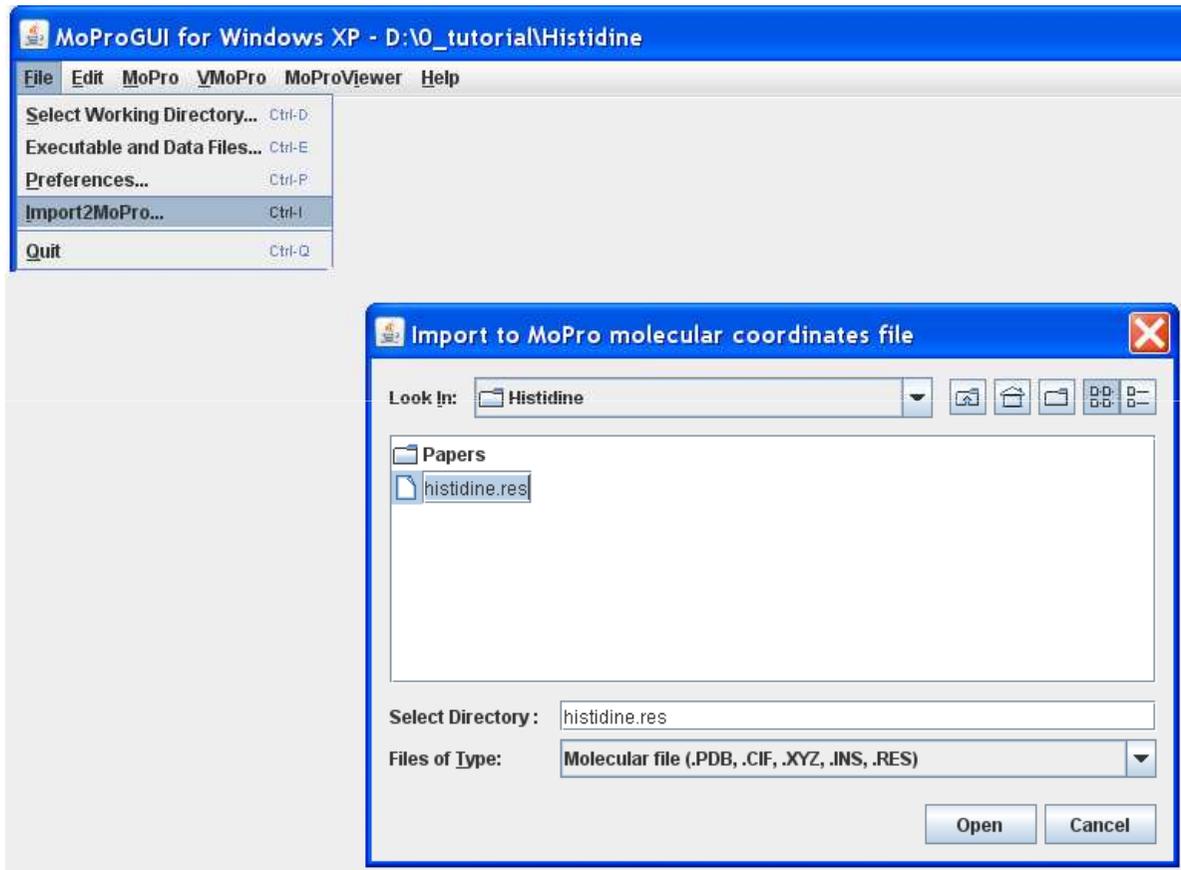
- * **MoPro** : crystallographic refinement
& structure analysis

- * **VMoPro** :
visualisation maps, molecular properties

- * **MoProViewer**

- molecule viewer & GUI

Import2MoPro.exe



Formats :

pdb

Cif

res / ins

Xyz

Molly

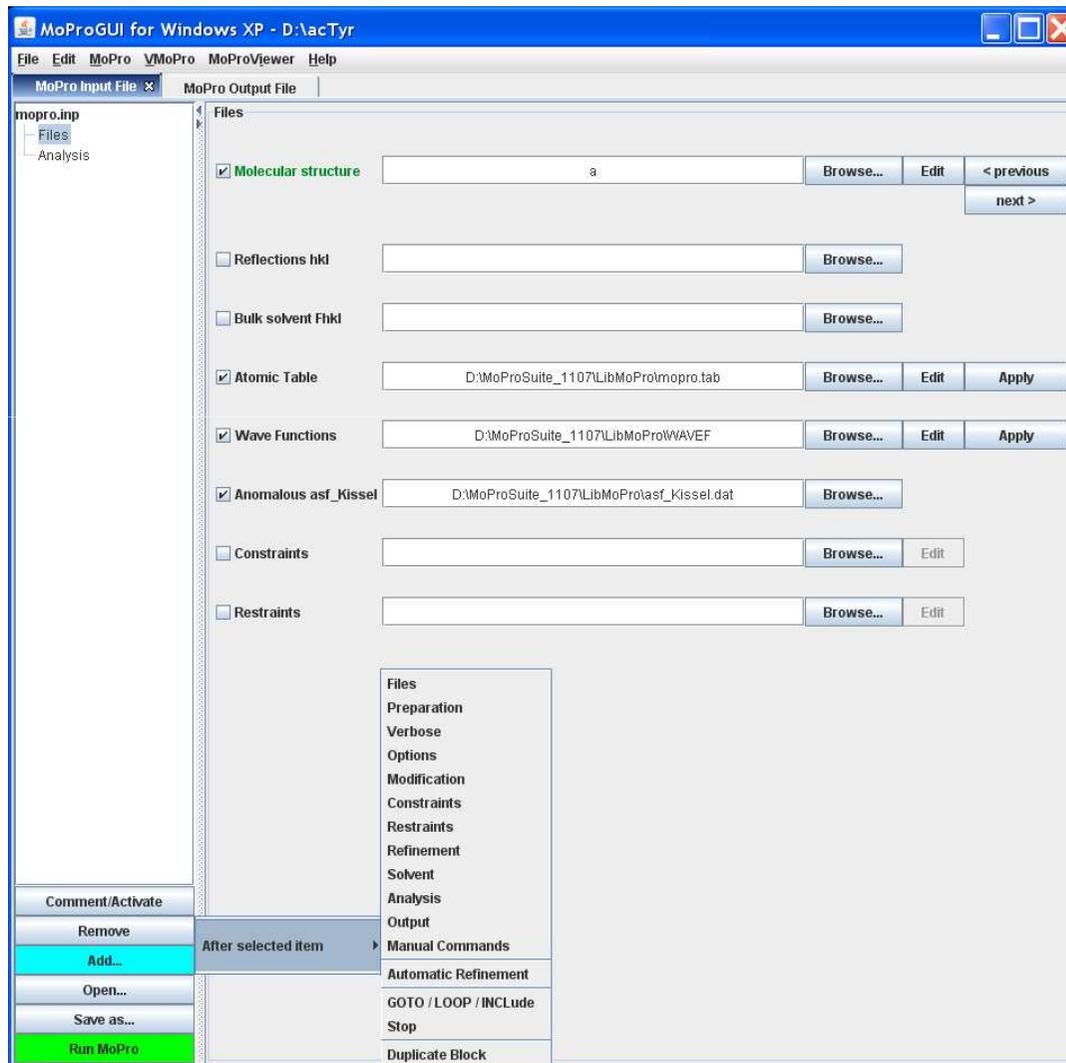
Mopro

XD

MoProGUI - MoPro : Main Menu.

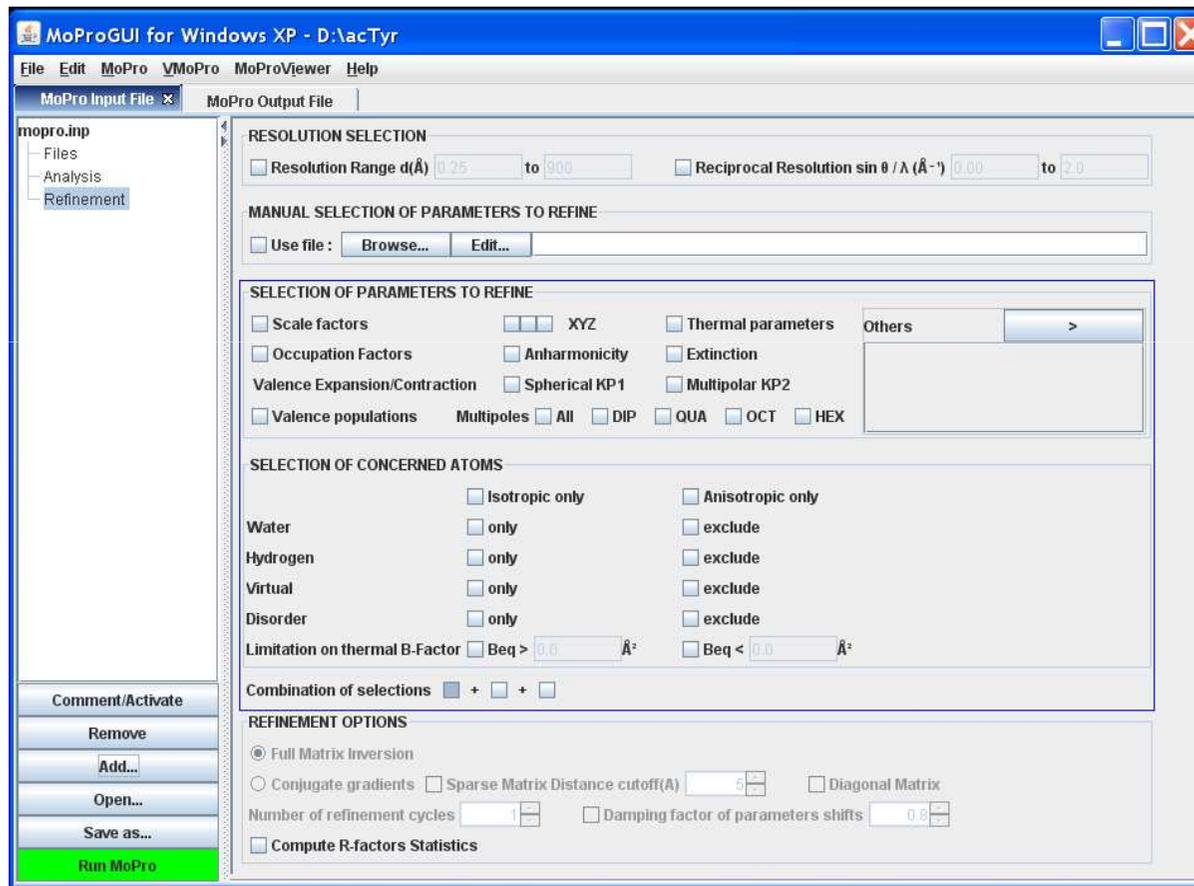
File declarations

Graphical User Interface



- Files
- Preparation
- Verbose
- Options
- Modification
- Constraints
- Restrictions
- Refinement
- Solvent
- Analysis
- Output
- Manual Commands
- Automatic Refinement
- GOTO / LOOP / INCLUDE
- Stop
- Duplicate Block

Refinement of Variables



MoPro input commands file "mopro.inp"

Example of script

```
RESO 0.4 0.7
SELE XYZ UIJ NOH
REFI LS 1

RESO 0.4 99.
SELE KP1 + KP2 NOH
REFI LS 1 DAMP 0.5

CONS DIST
WRIT DIST
```

Can be
generated
by
MoProGUI

(hydrogen H-X)
Print distances

Example of loop in « mopro.inp »

```
LOOP Ip1 5
```

```
RESO 0.4 0.7
```

```
SELE XYZ UIJ NOH
```

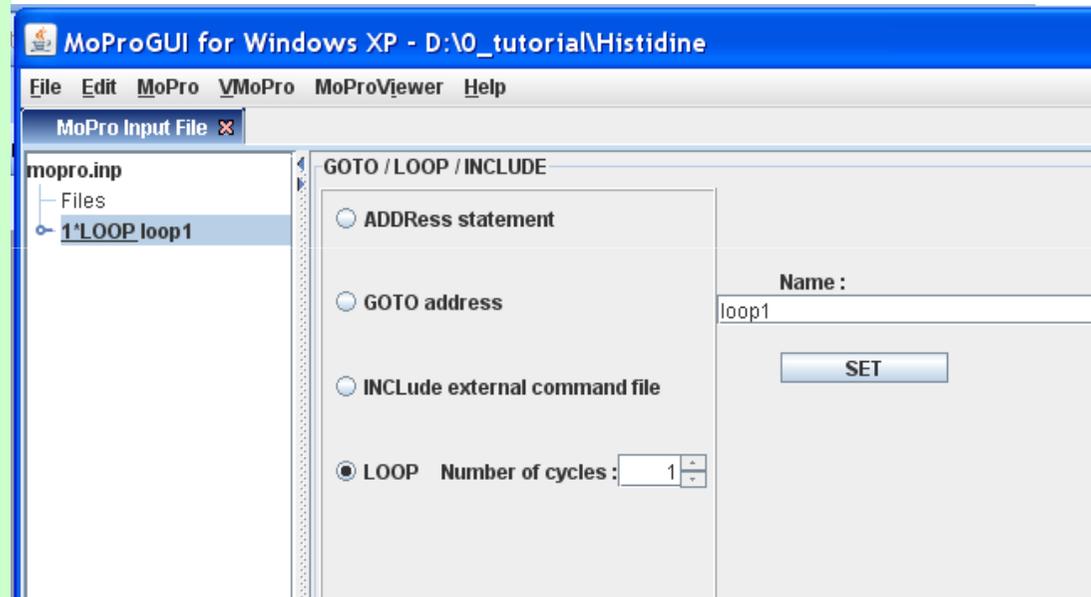
```
REFI LS 1
```

```
RESO 0.4 99.
```

```
SELE SCA PLM VAL
```

```
REFI LS 1
```

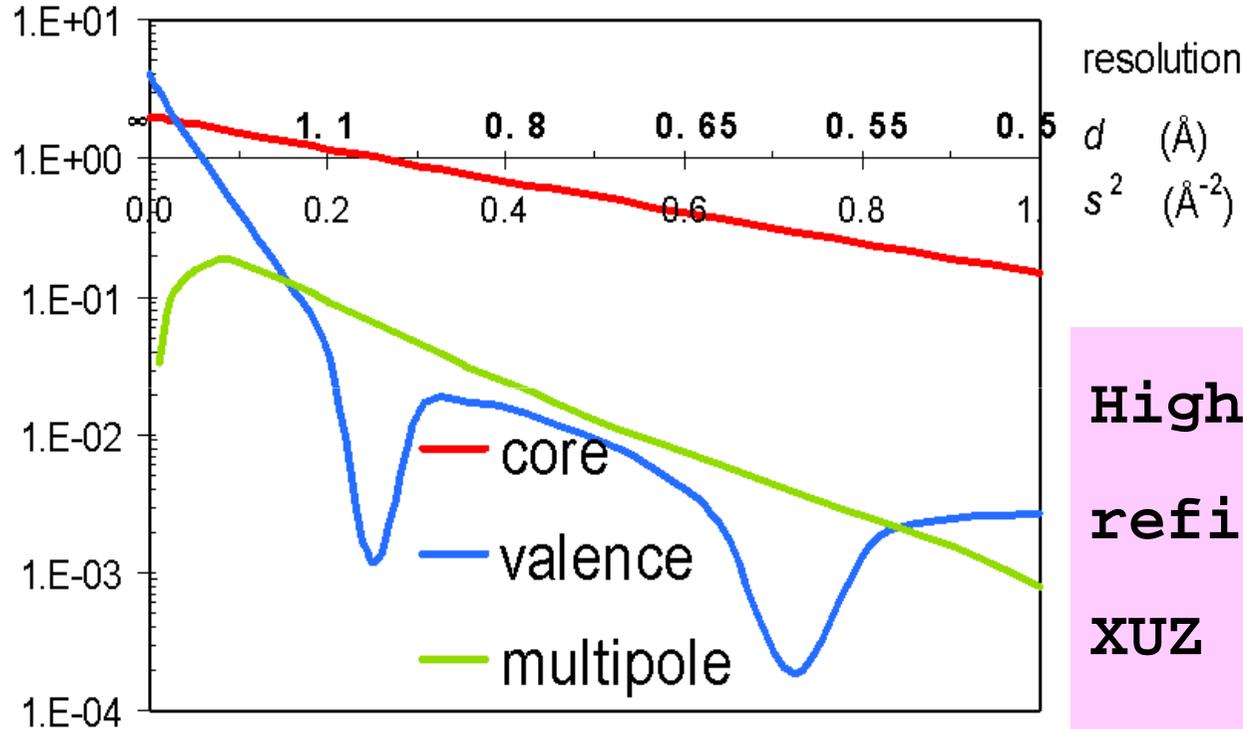
```
ADDR Ip1
```



Scattering Factor

core / valence / multipole

$f(s^2)$



Carbon atom $P_{\text{val}} = 4 e$

$B_{\text{iso}} = 4 \text{\AA}^2$

multipolar part averaged

High order

refinement:

XUZ UIJ

non hydrogen atoms

⇒ Deconvolution

U_{ij} & $\Delta\rho$

Charge Density Refinement Strategy

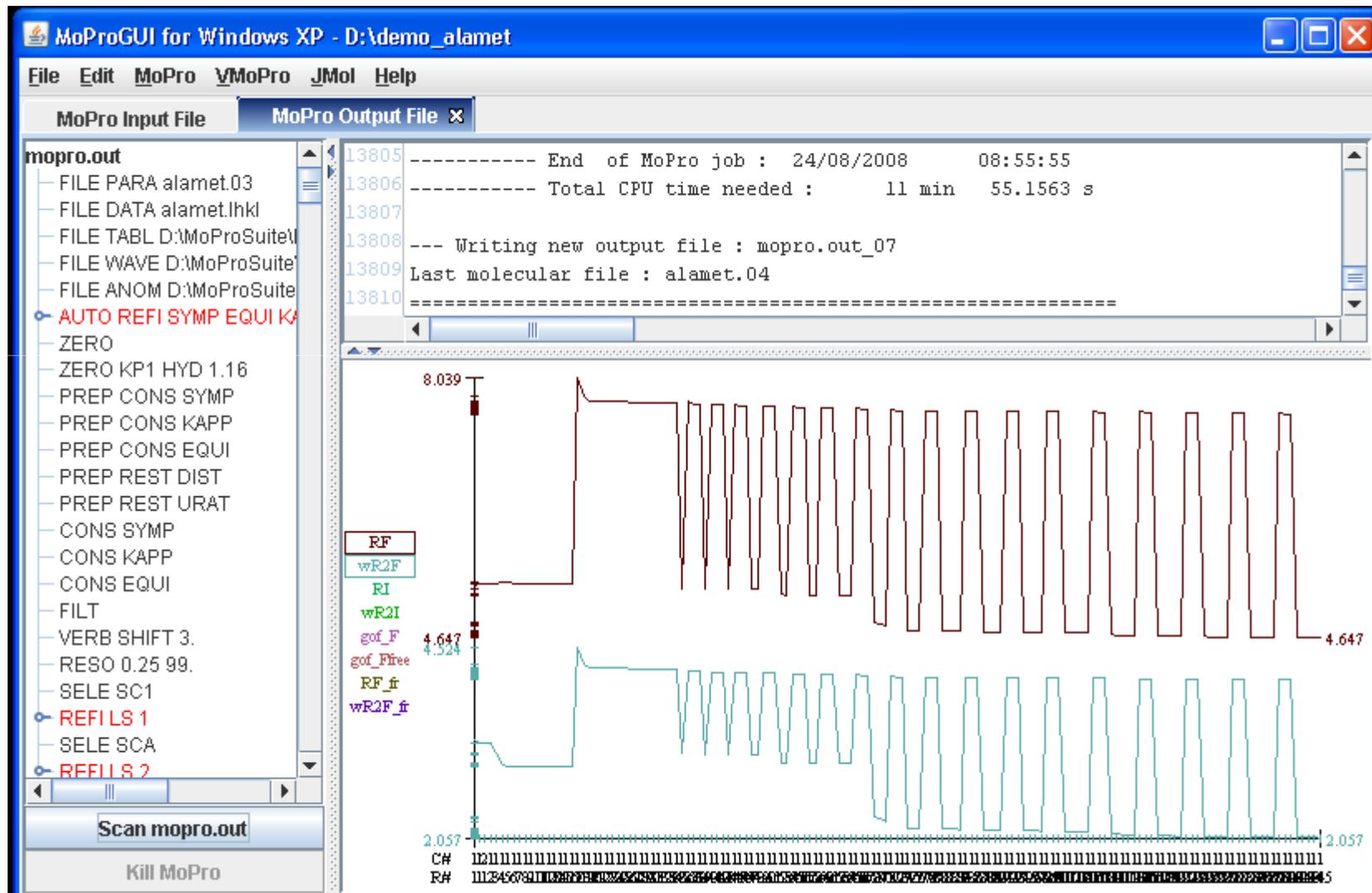
HIGH ORDER : RESOLUTION $d < 0.7 \text{ \AA}$
XYZ UIJ non-hydrogen

WHOLE RESOLUTION
SUCCESSIVE INTRODUCTION OF VARIABLES

- * SCALE FACTOR
- * XYZ Uiso Hydrogen
- * Valence populations
- * Multipoles
- * Kappa (spherical)
- * Kappa' (multipoles)

- * **MoPro**
automatic charge density refinement
small molecules
- **Preparation of restraints & constraints**
- **High order refinement XYZ UIJ NOH**
- **Iterative & progressive refinement of VAL PLM KP1 KP2**
- **Progressive release of constraints**

* MoPro automatic refinement



CRYSTALLOGRAPHIC REFINEMENT

LEAST SQUARES MINIMIZATION

$$\sum_{\mathbf{H}} (I_{\mathbf{H} \text{ calc}} - I_{\mathbf{H} \text{ obs}})^2 / \sigma_I^2$$
$$+ \sum_r (R_{\text{calc}} - R_{\text{target}})^2 / \sigma_r^2$$

\mathbf{H} reflections (h,k,l) $I_{\mathbf{H}}$ Intensity

R restraints (stereochemistry: distances, angles,

thermal motion, charge density similarity, targets for κ & κ' ...)

Least Squares Minimisation

1 refinement cycle : solve

$$\mathbf{A} \, d\mathbf{P} = \mathbf{V} \quad \text{normal equations}$$

$$\mathbf{V}_p = \sum_{\mathbf{H}} w_{\mathbf{H}} (I_{\mathbf{H}}^{obs} - I_{\mathbf{H}}^{calc}) \frac{\partial I_{\mathbf{H}}^{calc}}{\partial p} \quad \text{gradient}$$

**Normal
Matrix**

$$\mathbf{A}_{pq} = \sum_{\mathbf{H}} w_{\mathbf{H}} \frac{\partial I_{\mathbf{H}}^{calc}}{\partial p} \frac{\partial I_{\mathbf{H}}^{calc}}{\partial q}$$

Solve normal equations

$$A \mathbf{dP} = \mathbf{b}$$

matrix inversion $\mathbf{dP} = A^{-1} \mathbf{b}$

conjugate gradients iterative method

$$\mathbf{dP}_0 \rightarrow \mathbf{dP}_1 \rightarrow \dots \rightarrow \mathbf{dP}_n$$

► Useful for Large systems (sparse matrix)

Normal Matrix INVERSION

$$dP = A^{-1} V$$

B = A⁻¹ matrix of (variance , covariance)

$$B_{pp} \cdot Z = \text{VAR}(p) = \sigma^2(p)$$

$$B_{pq} Z = \text{COV}(p, q) = \sigma(p) \sigma(p) \rho(p, q)$$

$$Z = \Sigma_H W_H (I_{\text{obs}} - I_{\text{calc}})^2 / (N_{\text{obs}} - N_{\text{var}})^{1/2}$$

goodness of fit

Binary correlation coefficient
parameters p & q

$$\rho_{p,q} = \frac{B_{pq}}{(B_{pp} B_{qq})^{1/2}}$$

RESTRAINTS

distance, angles, planarity

Thermal motion URATIO ISOTRO
 UIJRES UIJRAT

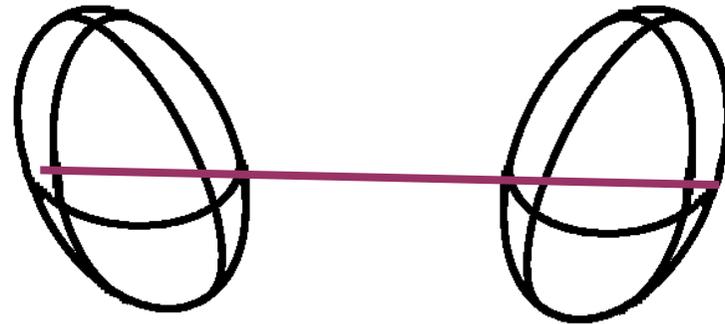
SIMDIS SIMANG
SIMVAL SIMPLM SIMKAP ...

RSYPLM multipoles symmetry
KAPVAL KP1 & Pval correlated

RESTRAINTS

Thermal Displacement Parameters

Rigid Bond $U_{\text{proj}}^{ij} \sim U_{\text{proj}}^{ij'}$



Limited Anisotropy

Uiso proportional

$$U_{\text{iso}} \sim k \cdot U_{\text{eq}}$$

Uij proportional

$$U_{ij} \sim k \cdot U_{ij'}$$

Stereochemical CONSTRAINTS

Distances *d* (Atom,Hydrogen)

Angles **AXYZH** **AXYHH** **AXHHH**
AXYH **AXHH**
AXH **AHH**

Exemple for C-CH₃

CONANG AXHHH C1 C2 H11 H12 H13

Automatic preparation of constraints

Restraints / Constraints on the charge density

in software MoPro

SYMPLM – symmetry of multipoles

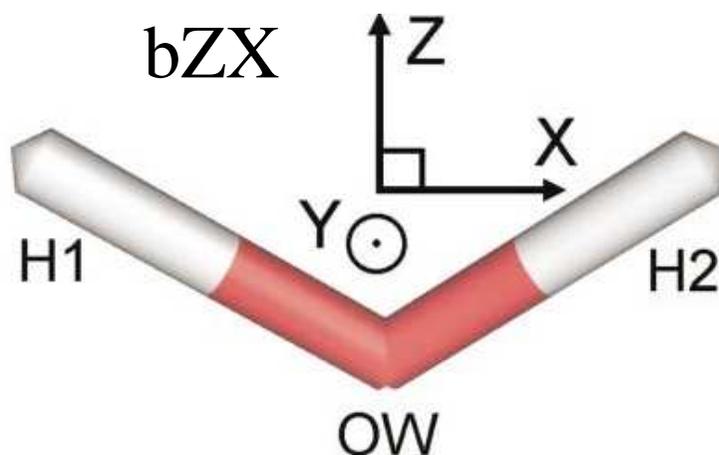
CONPVM – valence and multipole populations

CONPLM – multipole populations

CONVAL – valence populations

CONKAP –kappas expansion/contraction

Equivalence
of atoms



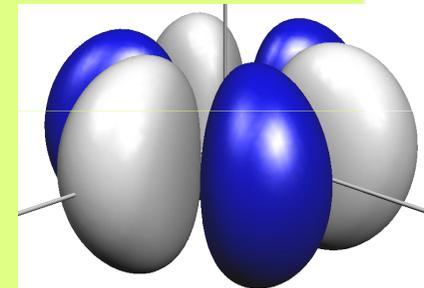
OW has two mirrors

H1 & H2 equivalent

Symmetry CONSTRAINTS / RESTRAINTS on the Charge Density

Symmetry on Multipoles

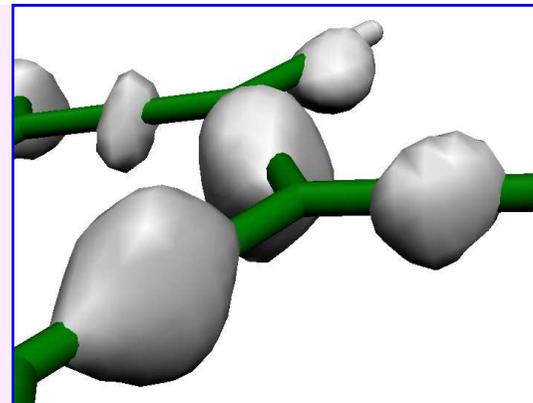
mx 1 mirror plane \perp x
mymz 2 mirrors aromatic C
3m 3m axis **CH₃, NH₃⁺**
i inversion centre
.....



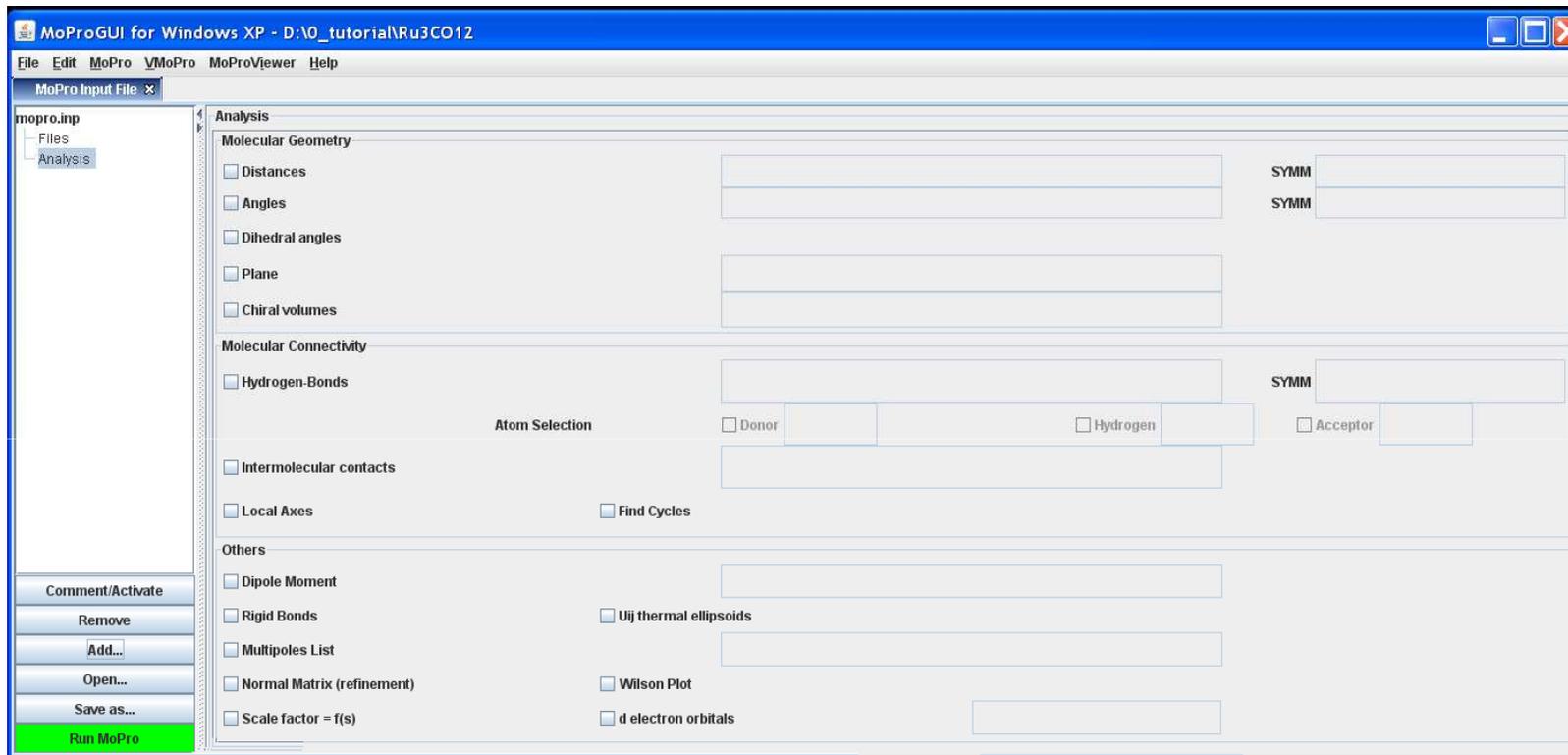
Exemple

SYMPLM 3m ALA CB

SYMPLM mymz PHE CD1

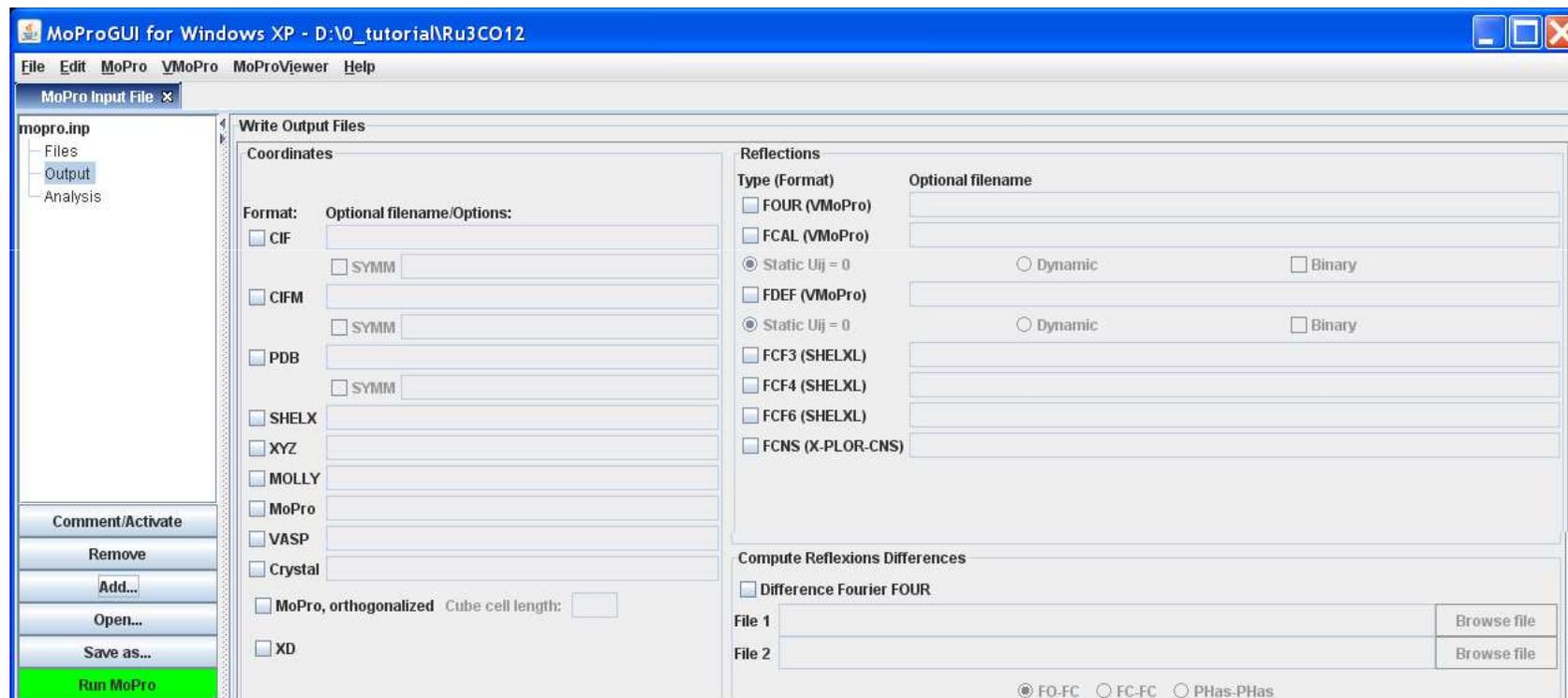


MoProGUI stereochemical analysis by MoPro



MoProGUI write output files

molecular structure & hkl reflections



- * Charge density refinement with MoPro
- * **VMoPro visualisation tool of properties**
- * Database Transfer
- * Application to proteins
- * Electrostatic Interaction Energy

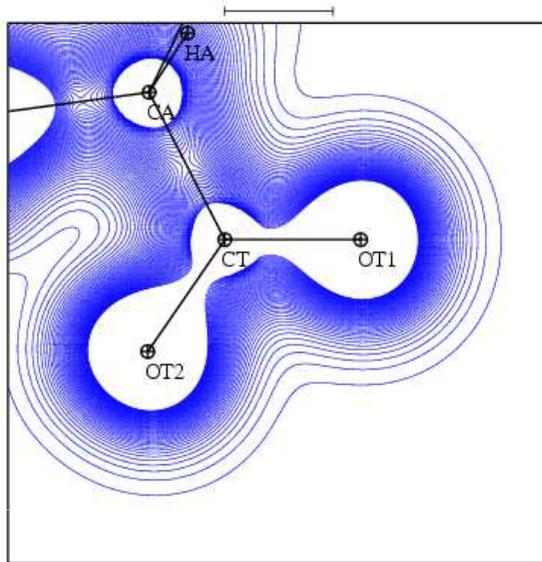
VMoPro

Properties computation & visualization

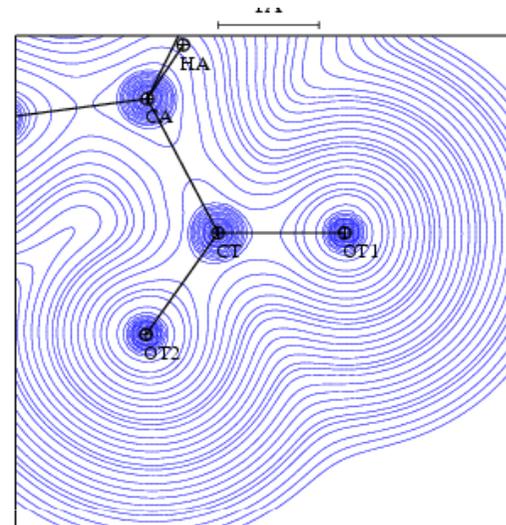
- STAT : STATic (deformation) electron density
- ELEC : ELECtrostatic potential map
- FOUR : FOURier $m \cdot F_o - n \cdot F_c$ electron density
- LAPL : LAPLacian of total electron density
- GRAD : GRADient NORM of electron density or electrostatic potential
- CRIT : CRITical points search of density, laplacian or electrostatic potential
- ENER : ENERgy computations
- INTE : INTEgration : topology

- SELE : define atoms SELEction for property calculation
- PARA : read new MoPro molecular parameters file
- PLOT : create & PLOT postscript image from 2D grid
- GRID : GRIDs handling (+ - x mask statistics)
- CONT : set Gradient / Basin / CONTOur lines options

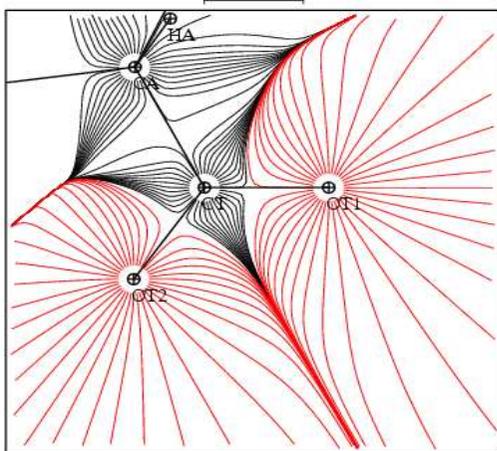
Static total electron density



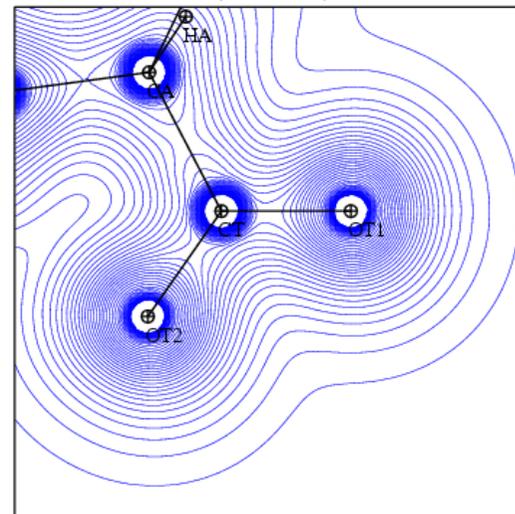
Regular contours



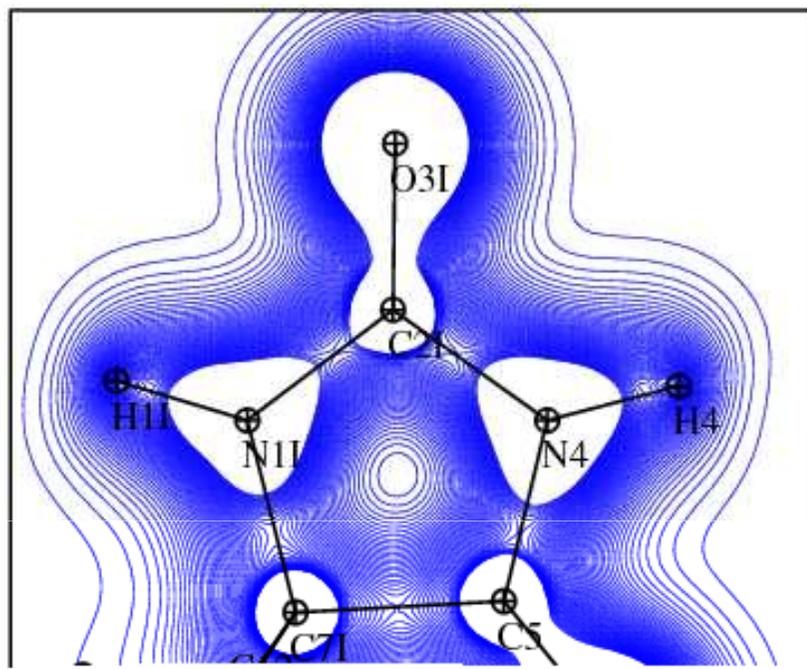
Log scale



Gradient lines

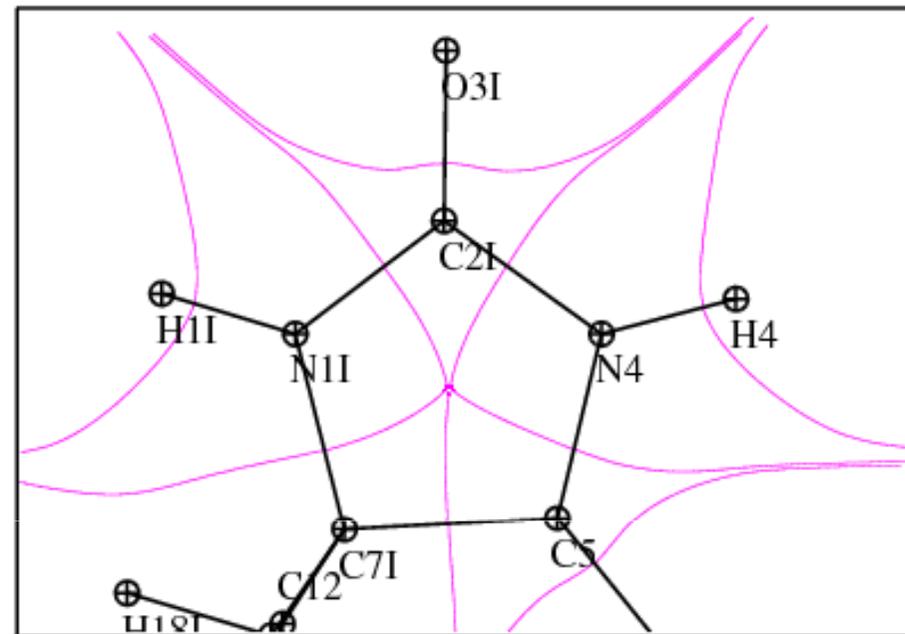


Square Root scale



Total Electron Density

Fidarestat



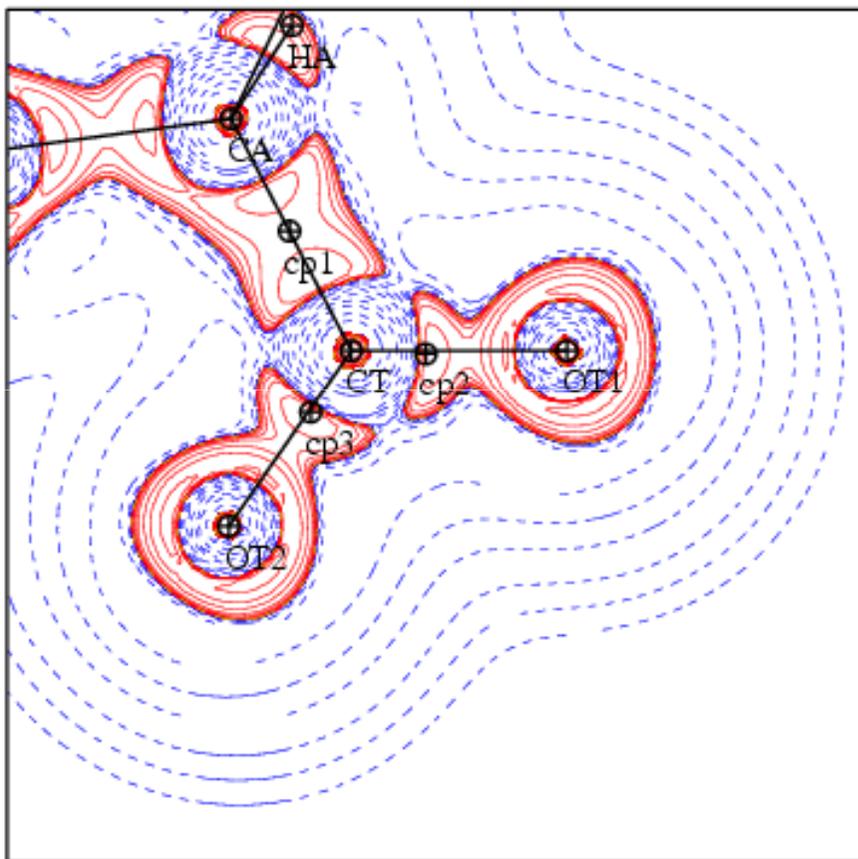
Basin Lines in 2D

Bader Theory : Atoms In Molecules

$$\text{Grad}(\rho) = \mathbf{0}.$$

VMoPro Laplacian

$$\nabla^2 \rho = \partial^2 \rho / \partial x^2 + \partial^2 \rho / \partial y^2 + \partial^2 \rho / \partial z^2$$



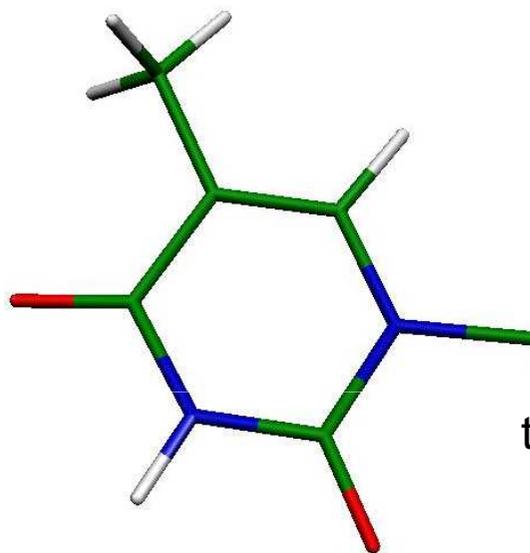
red $\nabla^2 \rho < 0$
electron accumulation

cp critical points:
grad $\rho = 0$

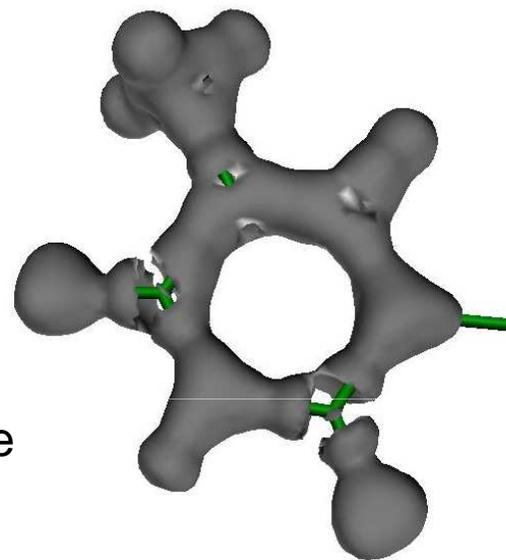
Analysis of CP
Covalent bonds
Hydrogen bonds
Ionic interactions

ρ = total electron density

Surface of Zero Laplacien $\nabla^2\rho = 0$



thymidine



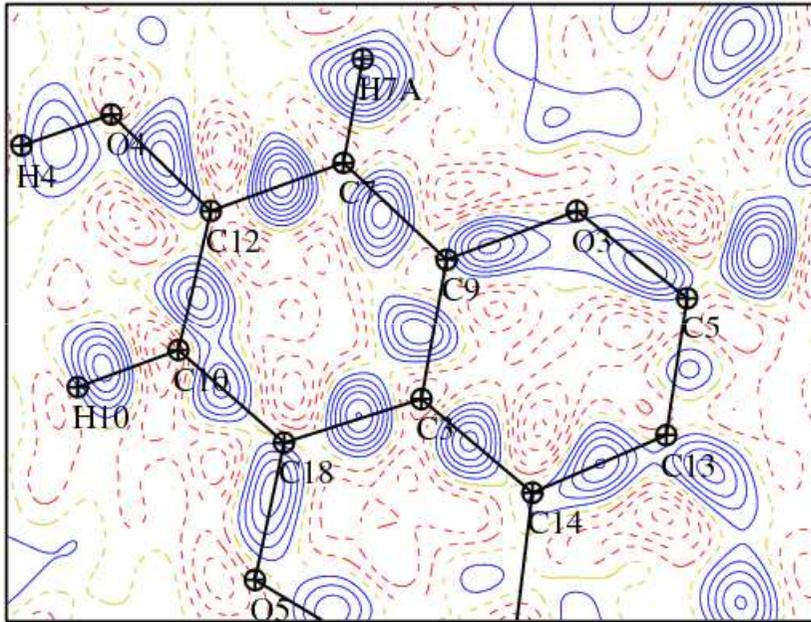
Reactivity Surface

VMoPro Visualisation

Open surface:
sites for nucleophiles

VMoPro FOUR $m * Fo - n * Fc$

Fourier Residual map $m = n = 1$



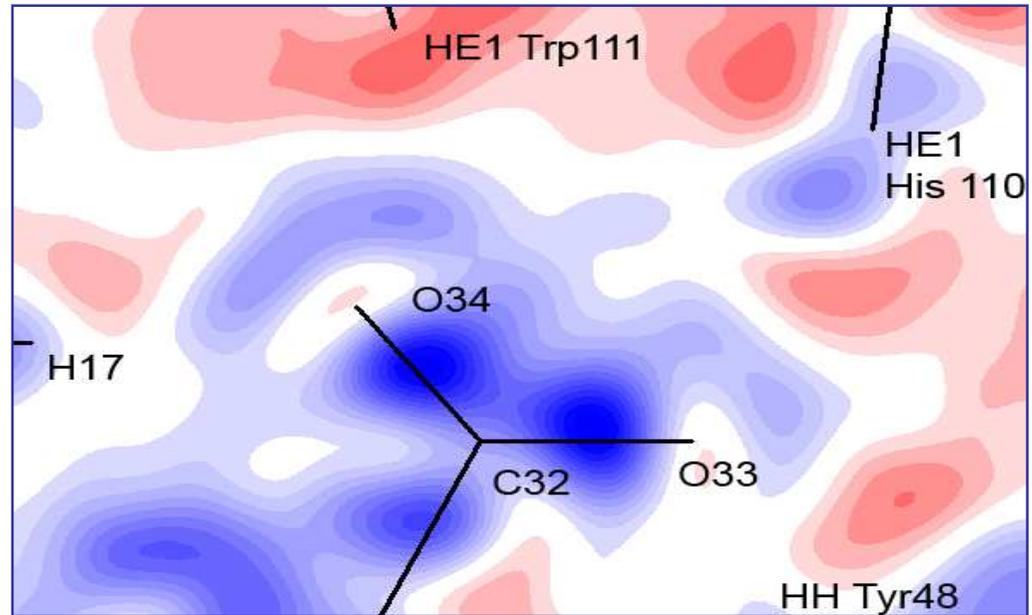
$F_{hkl} \rightarrow \text{grid } \rho(x,y,z)$

FFT Fast Fourier Transform

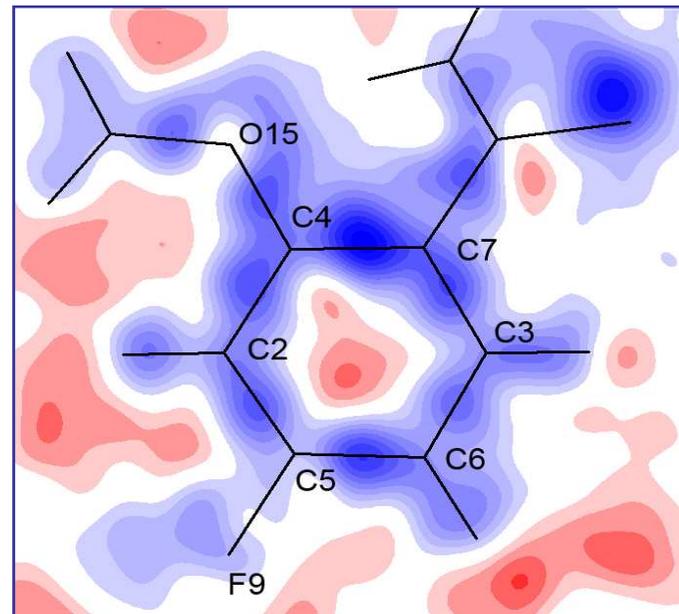
Available for 3D maps of unit cell

Dynamic deformation
electron density

Aldose reductase &
Idd594 inhibitor.

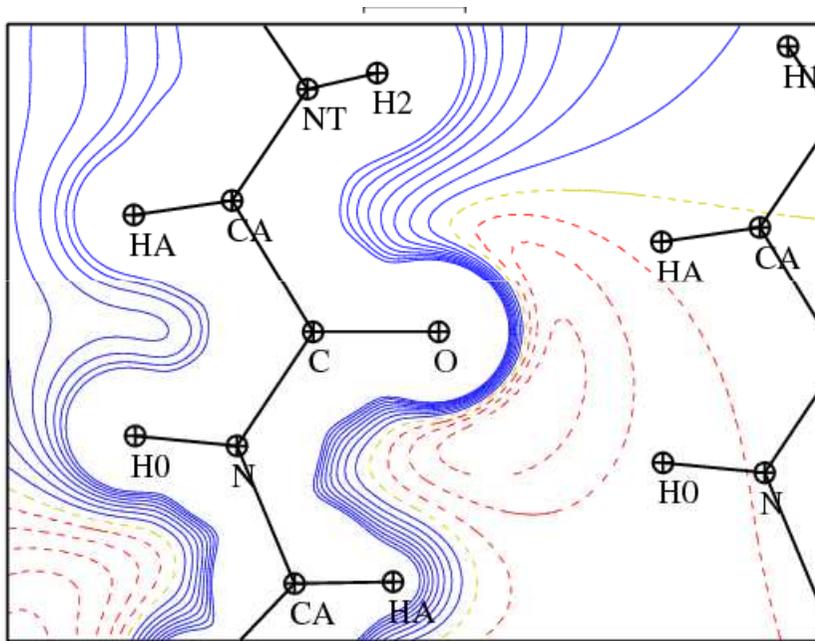


Fourier transform of
 $|F_{obs}| \exp(i\Phi_{mult}) - |F_{calc,sph}| \exp(i\Phi_{sph})$
Difference of 2 Fourier files

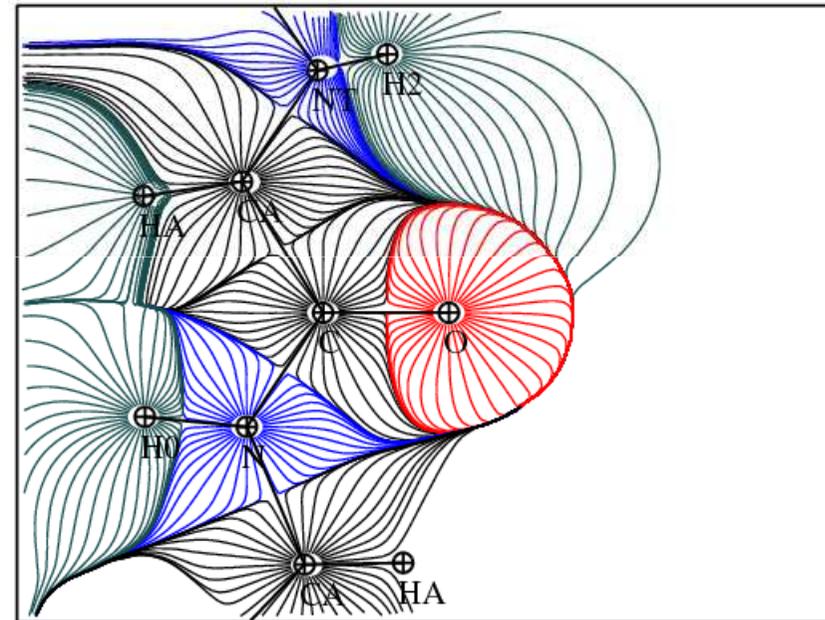


VMoPro ELEC

Electrostatic potential and gradient lines



Contour ± 0.05 e/A

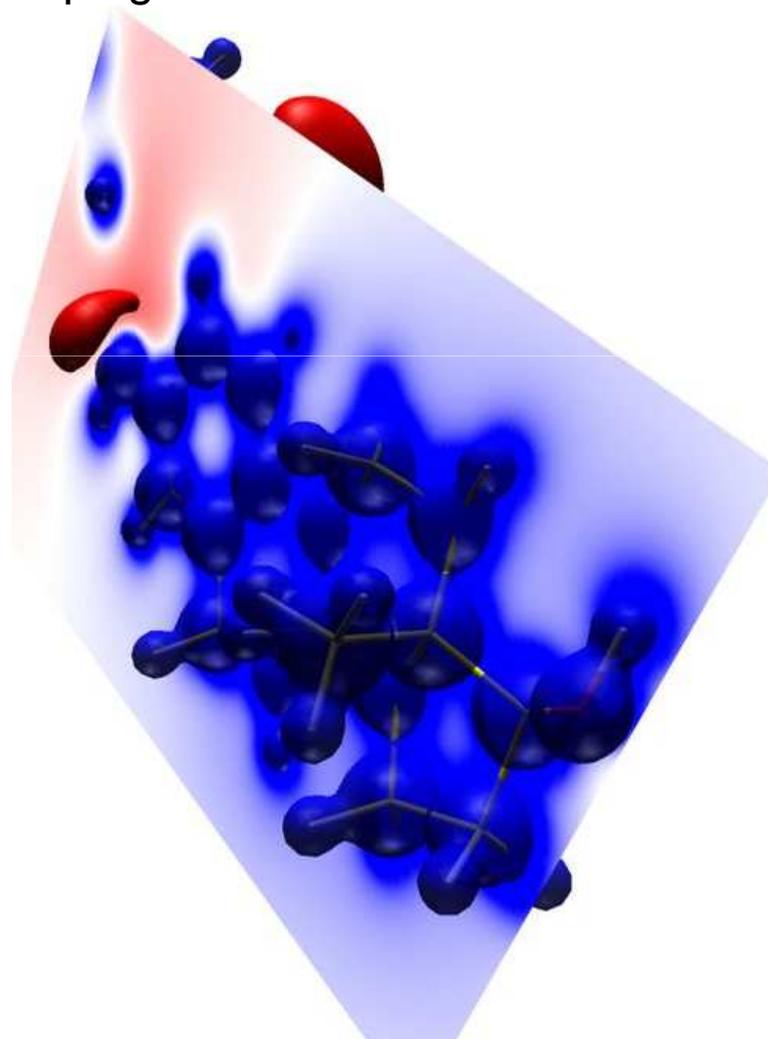
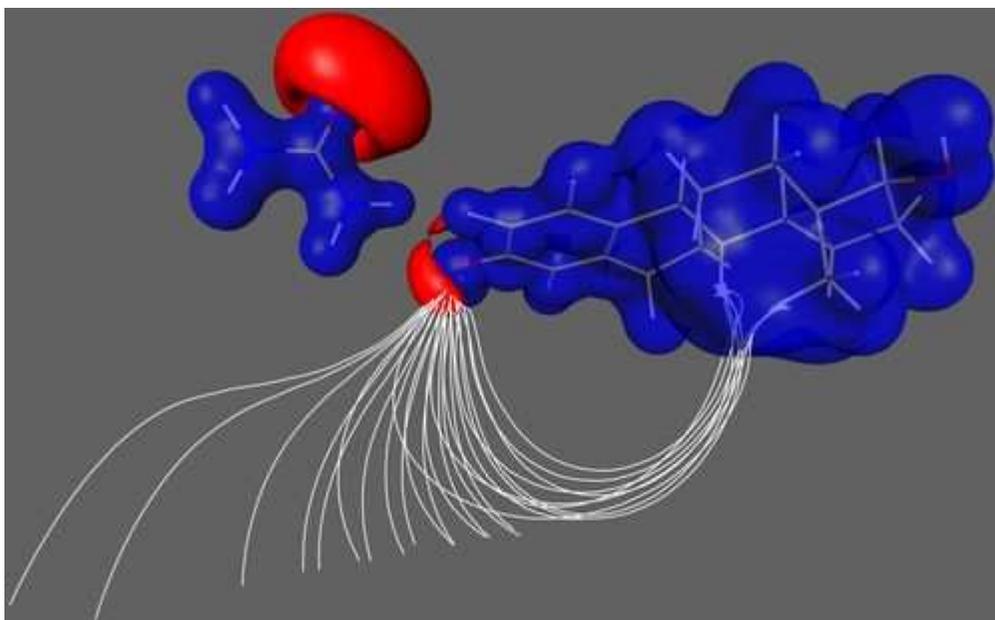


Gradient lines

MoProViewer : a graphical layer for MoPro

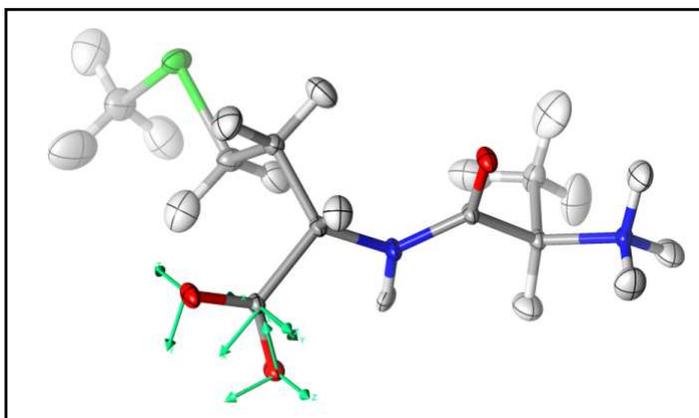
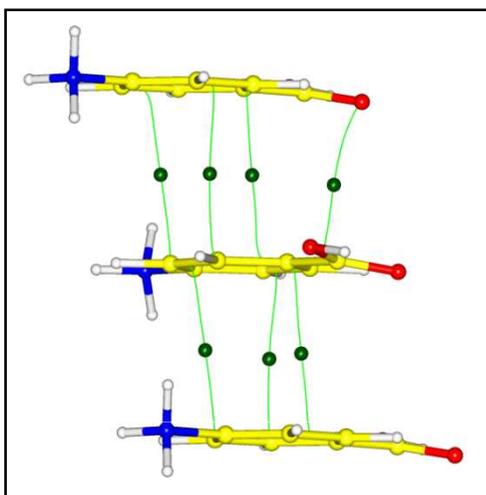
(Benoît Guillot)

- Reads MoPro (and other) file formats
- Easy and graphically aided 2D / 3D VMoPro maps generation
- Classical functionalities of molecular viewer :
 - lines, sticks, ball & sticks representations
 - stereochemistry computation
- Maps representations :
 - iso-surfaces
 - gradient lines
 - 2D slices



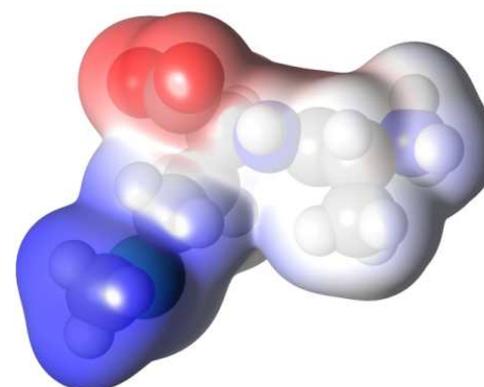
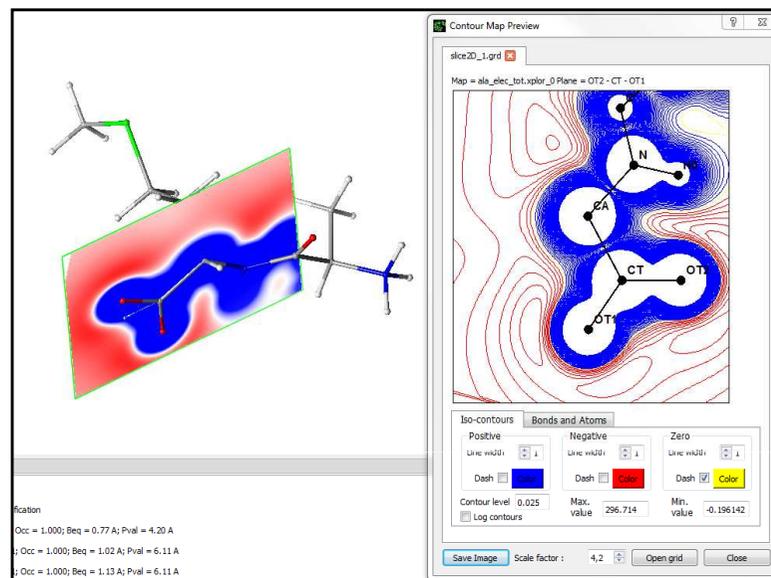
Some other examples of MoProViewer capabilities :

Carboxyphenylammonium stacking with C-C interactions bond paths and their (3,-1) critical points shown as green spheres



AlaMet molecule with 50% probability thermal ellipsoids, and orthogonal atomic axis systems represented for the COO atoms

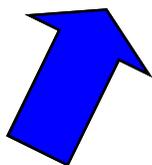
AlaMet molecule with a plane showing a slice of the electrostatic potential in the COO plane (left), and its corresponding 2D contour map (right).



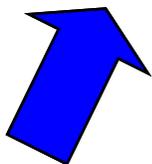
AlaMet electron density isosurface of $0.01 \text{ e}/\text{\AA}^3$ colored according to the molecular electrostatic potential values

- * Charge density refinement with MoPro
- * VMoPro visualisation tool of properties
- * **Database Transfer**
- * Application to proteins
- * Electrostatic Interaction Energy

Database of Experimental Multipolar Parameters

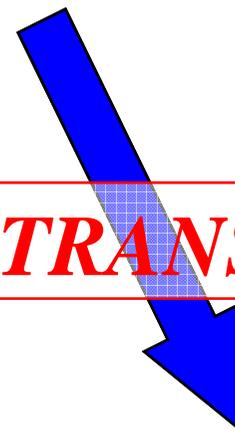


Average { P_{val} ; P_{lm} ; κ }
equivalent atoms



Charge Density
Peptide Crystals

TRANSFER



PROTEIN
or **SMALL COMPOUND**
at lower Resolution

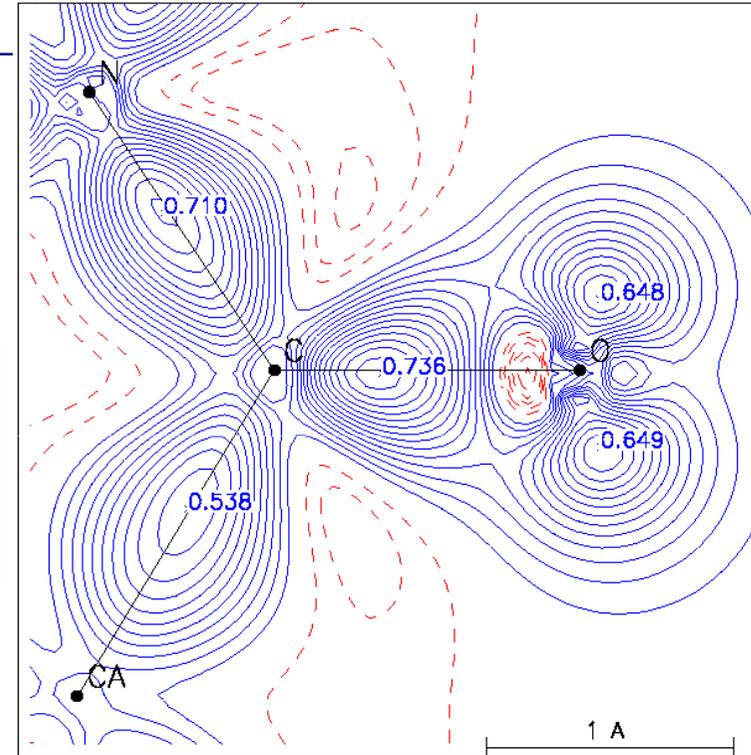
Experimental Library Multipolar Atom Model

TRANSFER

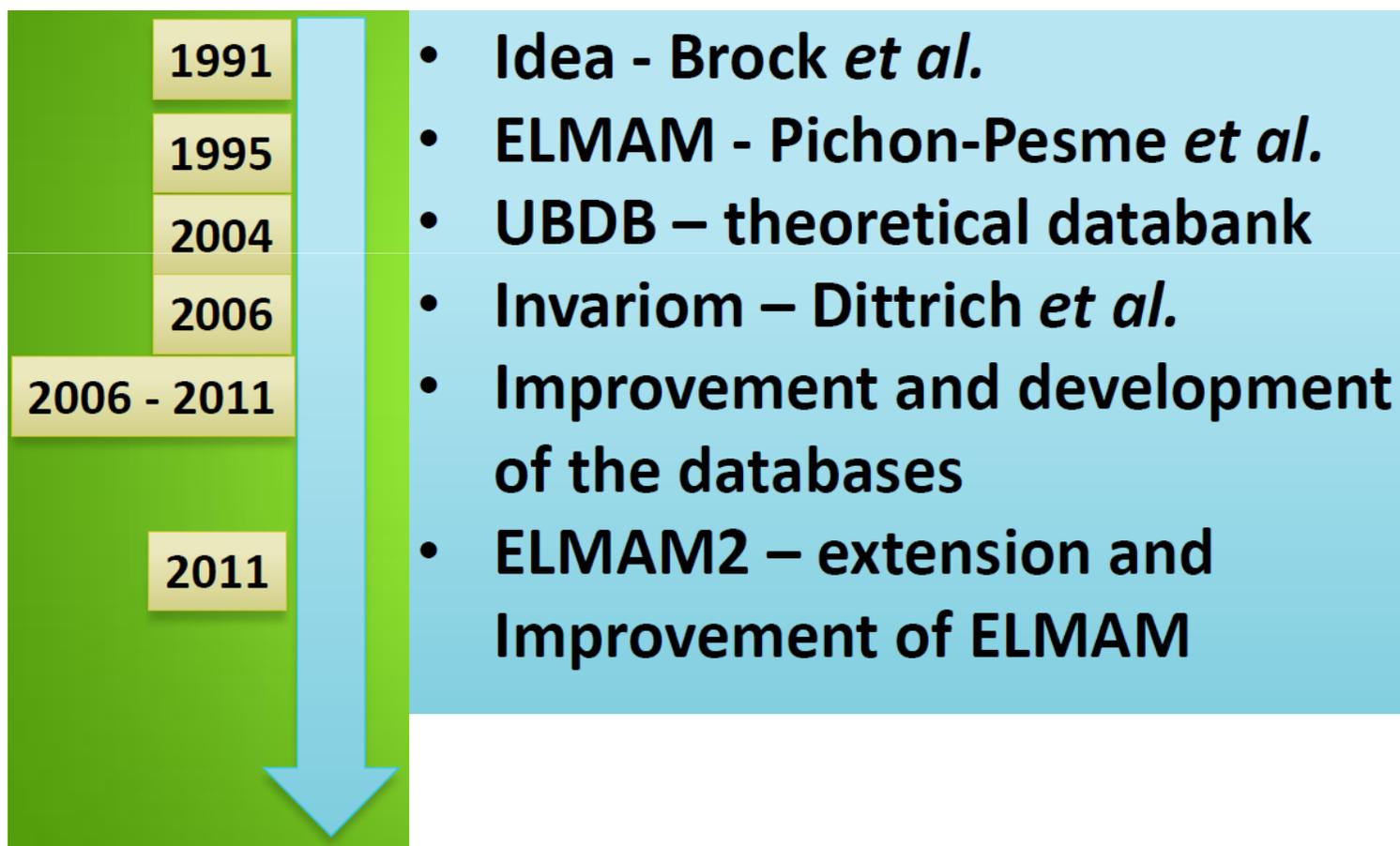
Protein or Small Compound
at Lower Resolution

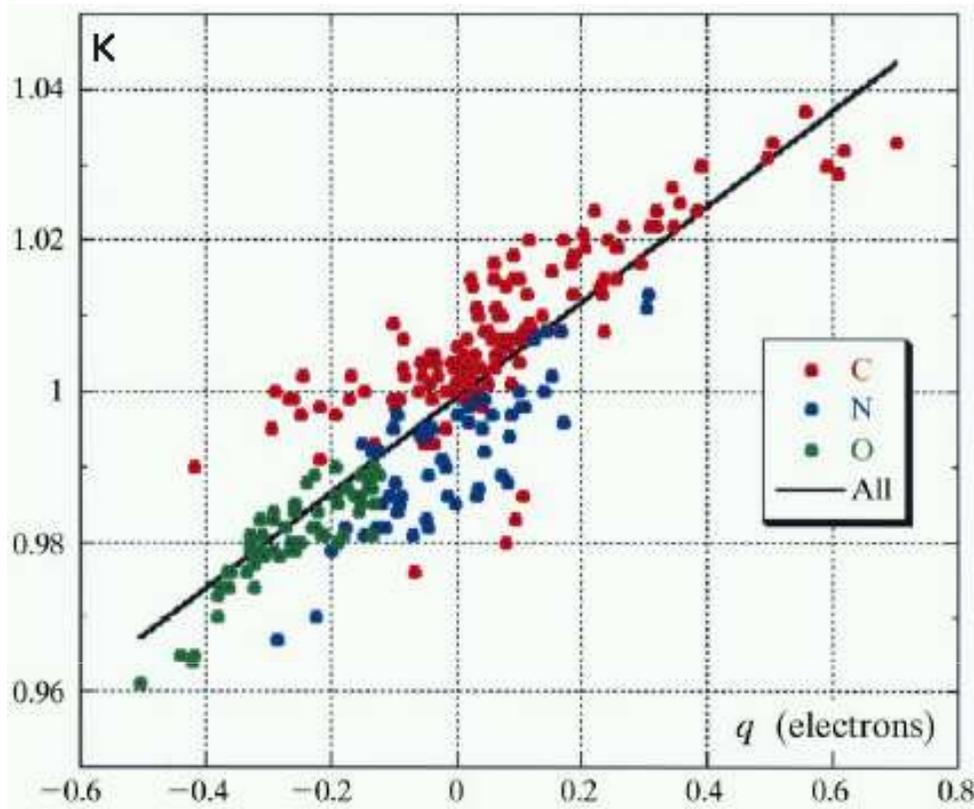
Crystal Structure More Precise

- Thermal Motion,
- Hydrogen Positions
- lower *RF* & *RF*-free factors



History





Volkov, Abramov & Coppens
Acta Cryst (2001). A57, 272

relation between
 expansion/contraction of valence shell (κ)
 & net atomic charge (q)
 for carbon, nitrogen & oxygen atoms
 (multipole refinements of crystal B3LYP/ 6-31G** structure factors)

Experimental Library

Multipolar Atom Model

ELMAM proteins

Zarychta, B., Pichon-Pesme, V., Guillot, B., Lecomte, C.
& Jelsch, C. (2007). Acta Cryst. A63, 108-125

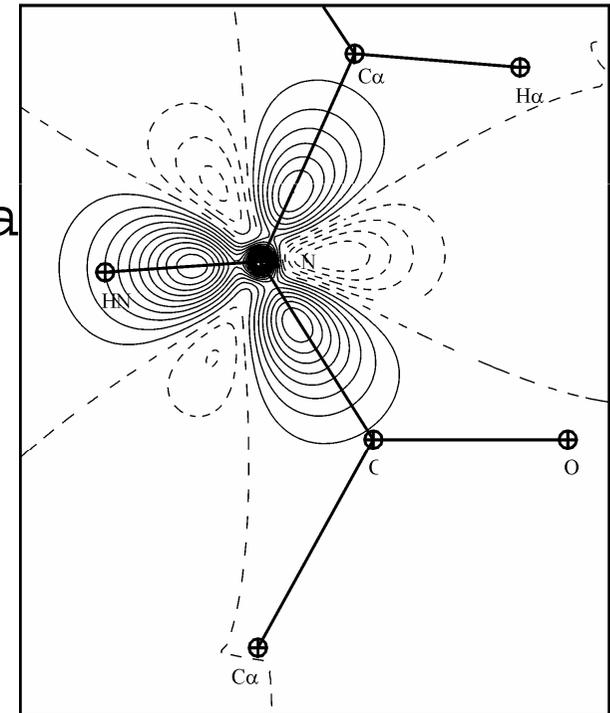
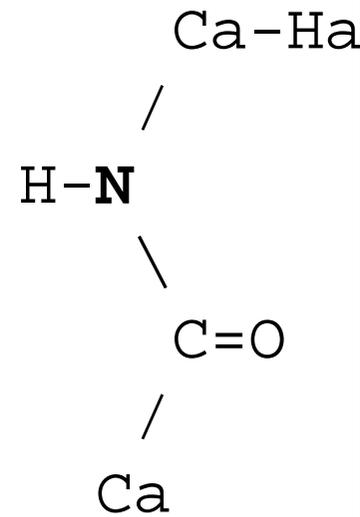
ELMAM2 common chemical groups optimal local axes for multipoles symmetry

Domagala S, Munshi P, Ahmed M, Guillot B & Jelsch C.
Acta Cryst. (2011). B67. 1-16.

Experimental Multipolar Database for Proteins

	Pv	Dx	Dy	Dz	Qz2	Qxz	Qyz	Qx2-y2	Qxy
actr	5.445	0.029	-0.104	-0.019	-0.154	0.021	0.002	-0.056	-0.001
actr	5.445	0.029	-0.104	-0.019	-0.154	0.021	0.002	-0.056	-0.001
acdelt	5.216	0.033	-0.071	-0.010	-0.036	0.013	0.003	-0.004	-0.042
acdelt	5.027	-0.002	-0.169	-0.028	-0.034	0.025	-0.045	-0.039	-0.063
enkad	5.371	-0.024	-0.104	0	-0.074	0	0	0.036	0.111
enkad	5.371	-0.024	-0.104	0	-0.074	0	0	0.036	0.111
enkad	5.371	-0.024	-0.104	0	-0.074	0	0	0.036	0.111
enkad	5.371	-0.024	-0.104	0	-0.074	0	0	0.036	0.111
trigqa	5.330	0.041	-0.048	-0.016	-0.062	-0.021	-0.016	0.042	0.031
trigqa	5.440	-0.031	-0.114	0.017	-0.042	0.012	-0.027	-0.008	0.013
trigqa	5.381	0.006	-0.015	0.014	-0.016	-0.003	0.059	-0.013	0.018
trigqa	5.444	0.001	-0.069	-0.016	0.010	0.020	0.018	0.012	0.007
YGG	5.306	-0.059	-0.070	0	-0.024	0	0	-0.014	0.07
YGG	5.311	-0.083	-0.068	0	-0.061	0	0	-0.029	0.016
GD	5.426	-0.019	-0.052	0	0.06	0	0	-0.008	0.118
actyr	5.154	-0.025	-0.042	-0.028	-0.028	-0.002	0.003	-0.055	0.009
GT	5.313	-0.025	-0.010	0	0.027	0	0	0.053	-0.034
prohis	5.255	0.004	-0.014	0.008	-0.067	0.053	0.004	0.011	0.048
prohis	5.255	0.004	-0.014	0.008	-0.067	0.053	0.004	0.011	0.048
acgln	5.108	-0.017	-0.121	-0.031	-0.069	-0.032	0.049	0.031	0.013
alamet	5.206	0.018	-0.021	-0.014	-0.044	0.008	-0.001	-0.019	0.020
<p>	5.312	-0.009	-0.072	-0.006	-0.050	0.008	0.003	0.000	0.034
SEM	0.026	0.007	0.01	0.003	0.011	0.004	0.005	0.008	0.012

+octapoles
K κ'

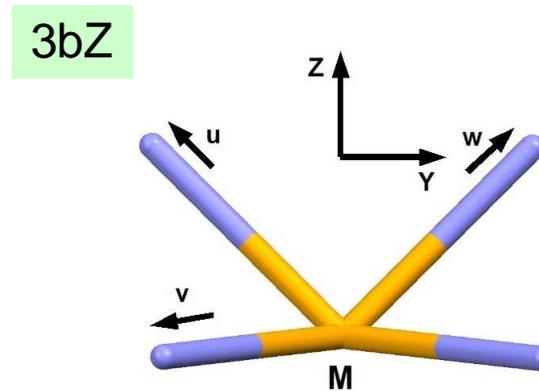
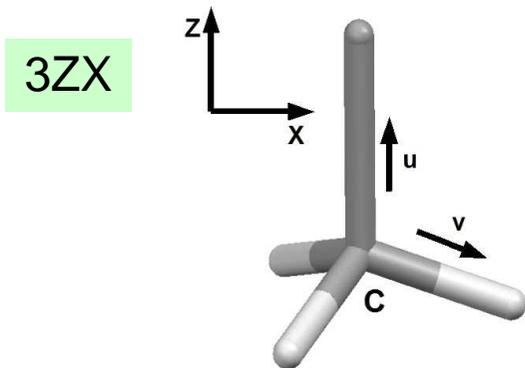
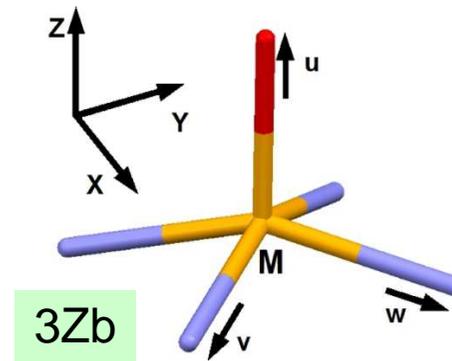
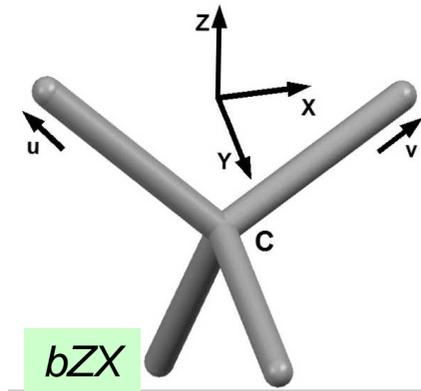
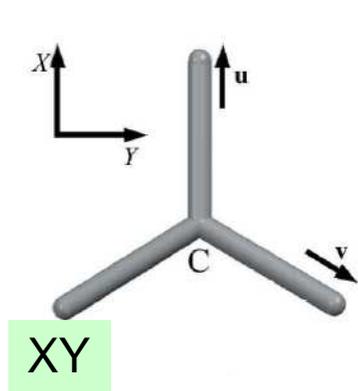


Atom Type N

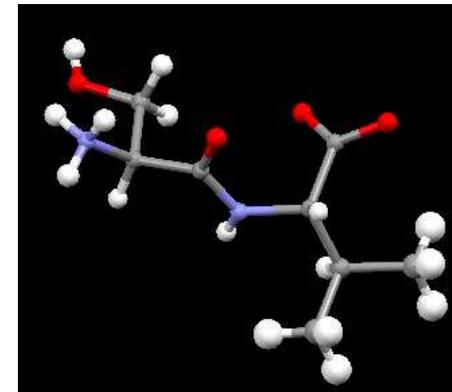
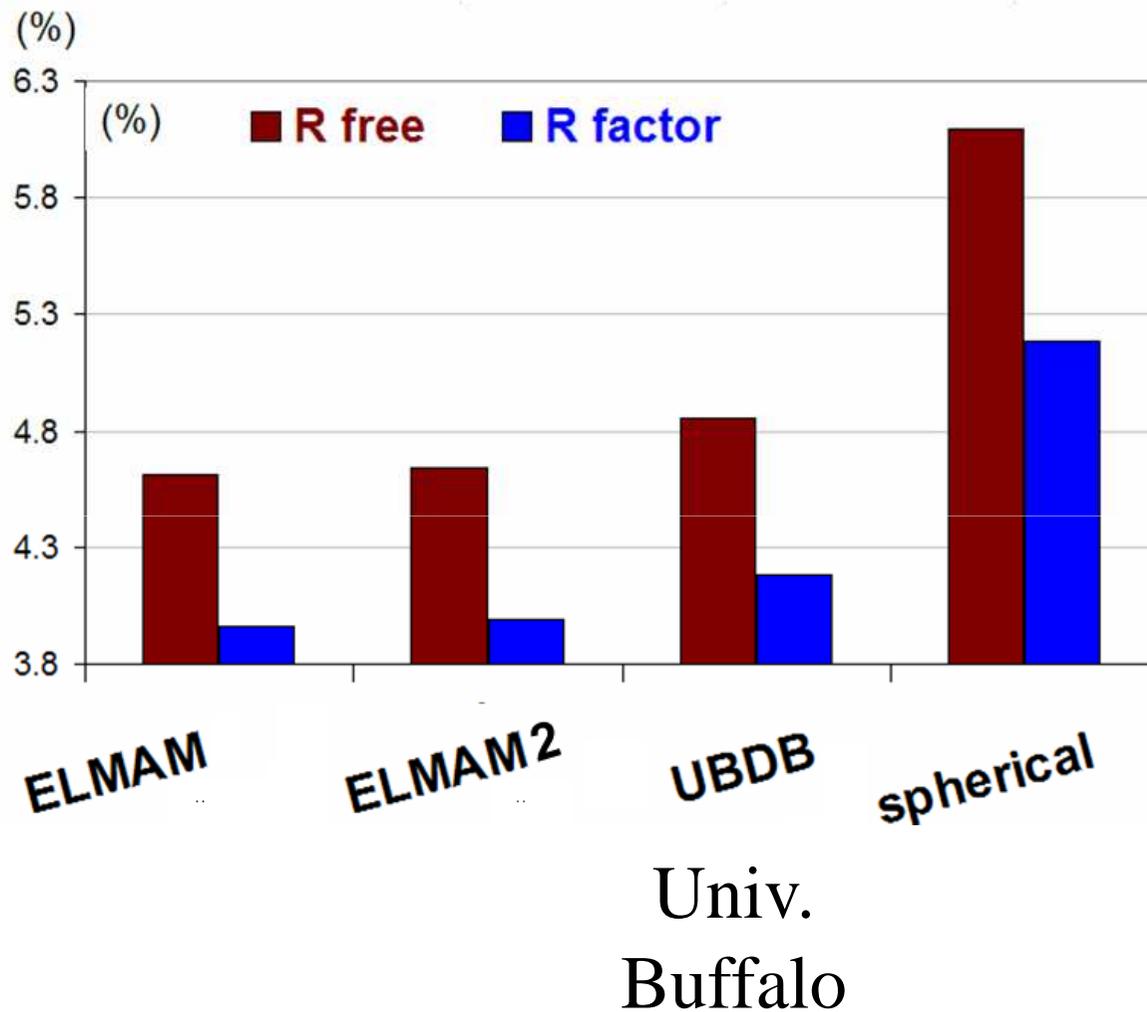
Extension of multipolar database

ELMAM	ELMAM2
<ul style="list-style-type: none">• average values from 14 peptides , amino acids	<ul style="list-style-type: none">• average values from 54 high resolution structures
<ul style="list-style-type: none">• limited to proteins	<ul style="list-style-type: none">• extension common chemical groups
<ul style="list-style-type: none">• XY local axes, no symmetry constraints	<ul style="list-style-type: none">• optimal local axes & symmetry constraints to improve refinements & average statistics
<ul style="list-style-type: none">• manual selection of atom types (chemical intuition)	<ul style="list-style-type: none">• automatic assignement based on connectivity & chemical environment of atoms

ELMAM2 Database : Optimal local axes systems for multipoles



Effect of Database Transfer



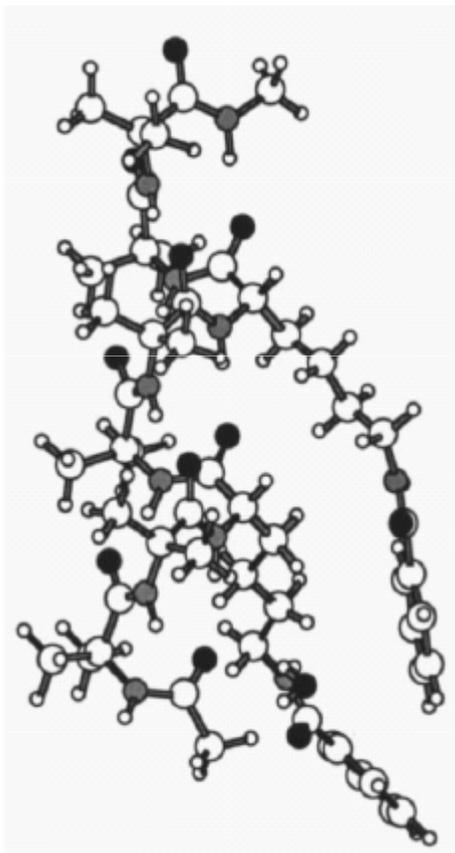
L-Seryl
-L-valine

Moen *et al.*, 2004,
Acta Cryst. C60,
o564–o565

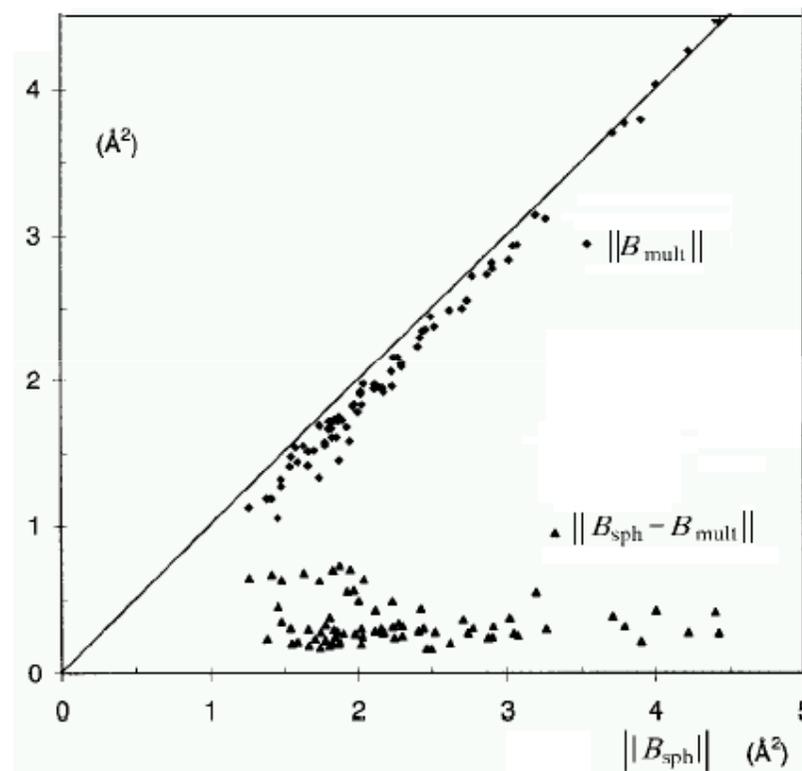
0.73 Å
resolution

Same number of
variables & restraints

EFFECT of TRANSFER on *B*-FACTORS



Helical octapeptide

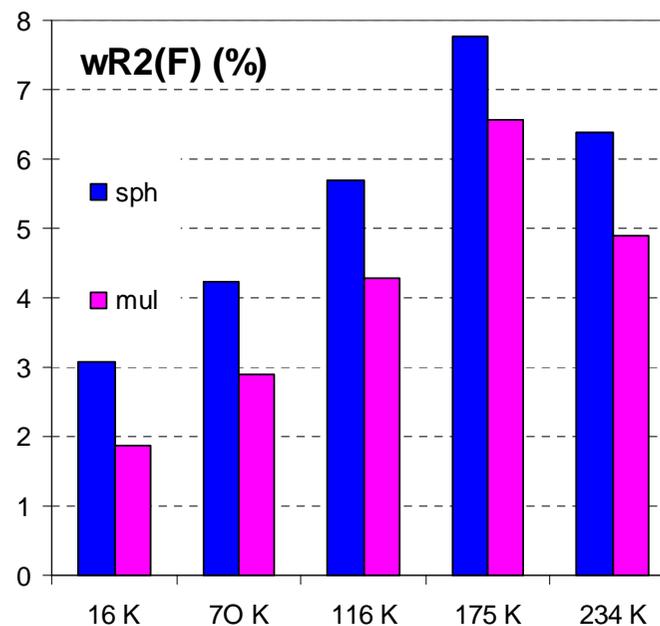
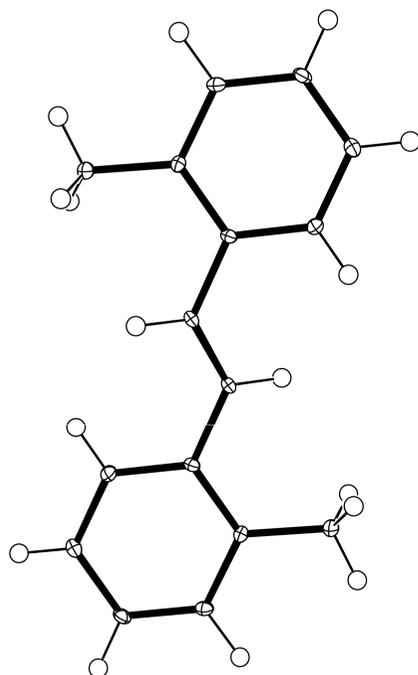


Acta Cryst
(1998) D54 1306

Small Compound & Spherical or Multipolar Atom

(E)-2,2'-dimethylstilbene

(Ogawa *et al.* 1992)



Transfer Library Multipoles & Refinement

Maximal Constraints: atom equivalencies & local symmetries

=> Improved Thermal Displacement Parameters

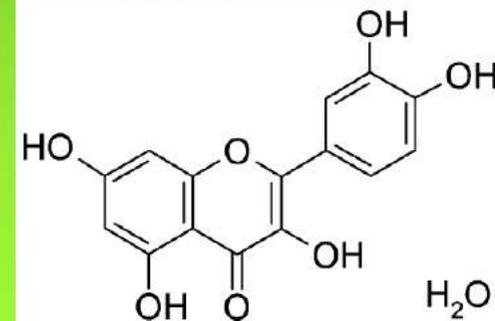
Dynamical Analysis (Pr Bürgi Bern)

Multipole modelling of quercetin

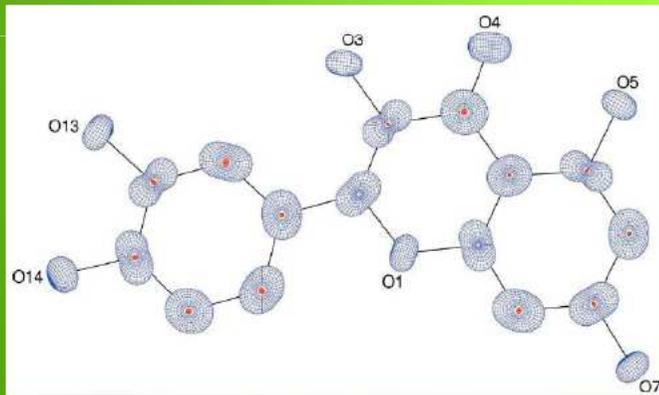
ELMAM2

12 atom-types

Transfer

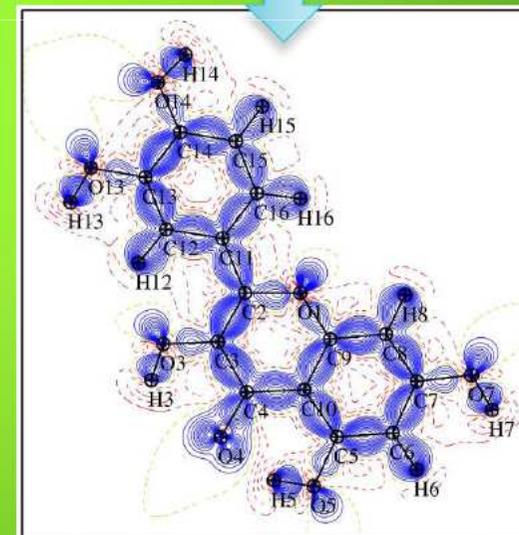


Peanut representation



Improvement of ADPs
IAM – ELMAM2

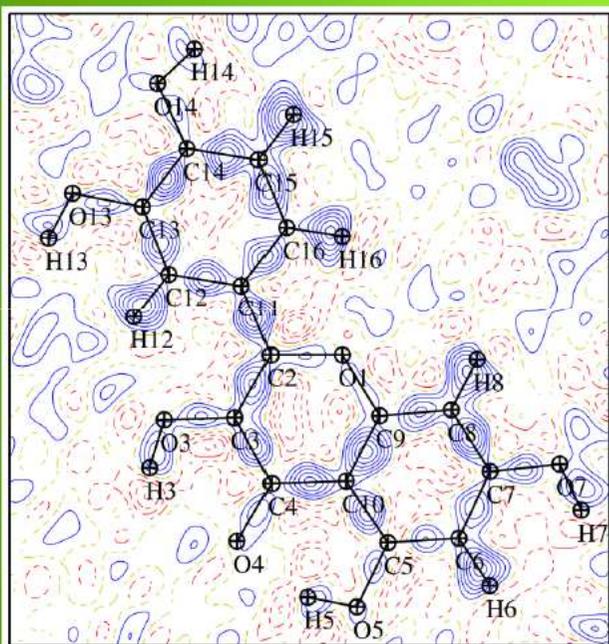
Static
deformation
density
Contour: ± 0.05
 $\text{e}\text{\AA}^{-3}$



Domagała et al., *Acta Cryst.* **2011**, B67, 63-78

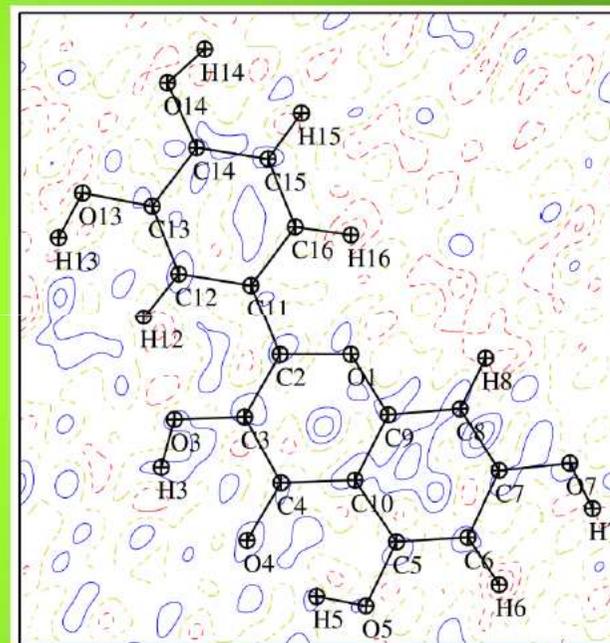
Quality of the multipolar transfer

IAM model refinement



$$\begin{aligned}\rho_{\max} &= +0.39 \text{ e}\text{\AA}^{-3} \\ \rho_{\min} &= -0.24 \text{ e}\text{\AA}^{-3} \\ R(F) &= 4.00 \%\end{aligned}$$

ELMAM2 + xyz & U_{ij} refinement



$$\begin{aligned}\rho_{\max} &= +0.14 \text{ e}\text{\AA}^{-3} \\ \rho_{\min} &= -0.16 \text{ e}\text{\AA}^{-3} \\ R(F) &= 2.20 \%\end{aligned}$$

Residual
Density

Contour
 $\pm 0.05 \text{ e}\text{\AA}^{-3}$

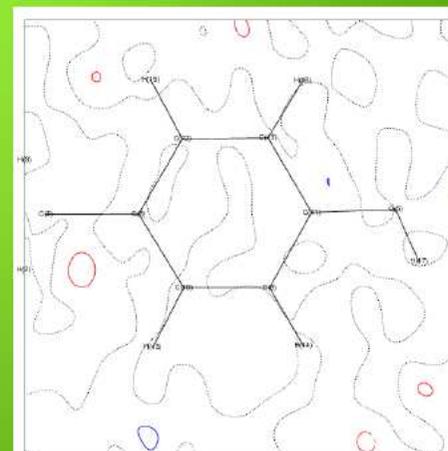
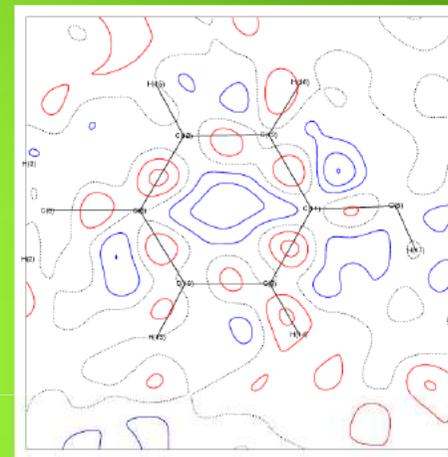
quercetin

Refinements of experimental X-ray data

Application of the databanks to low-resolution data (transferred aspherical atom model refinement, TAAM):

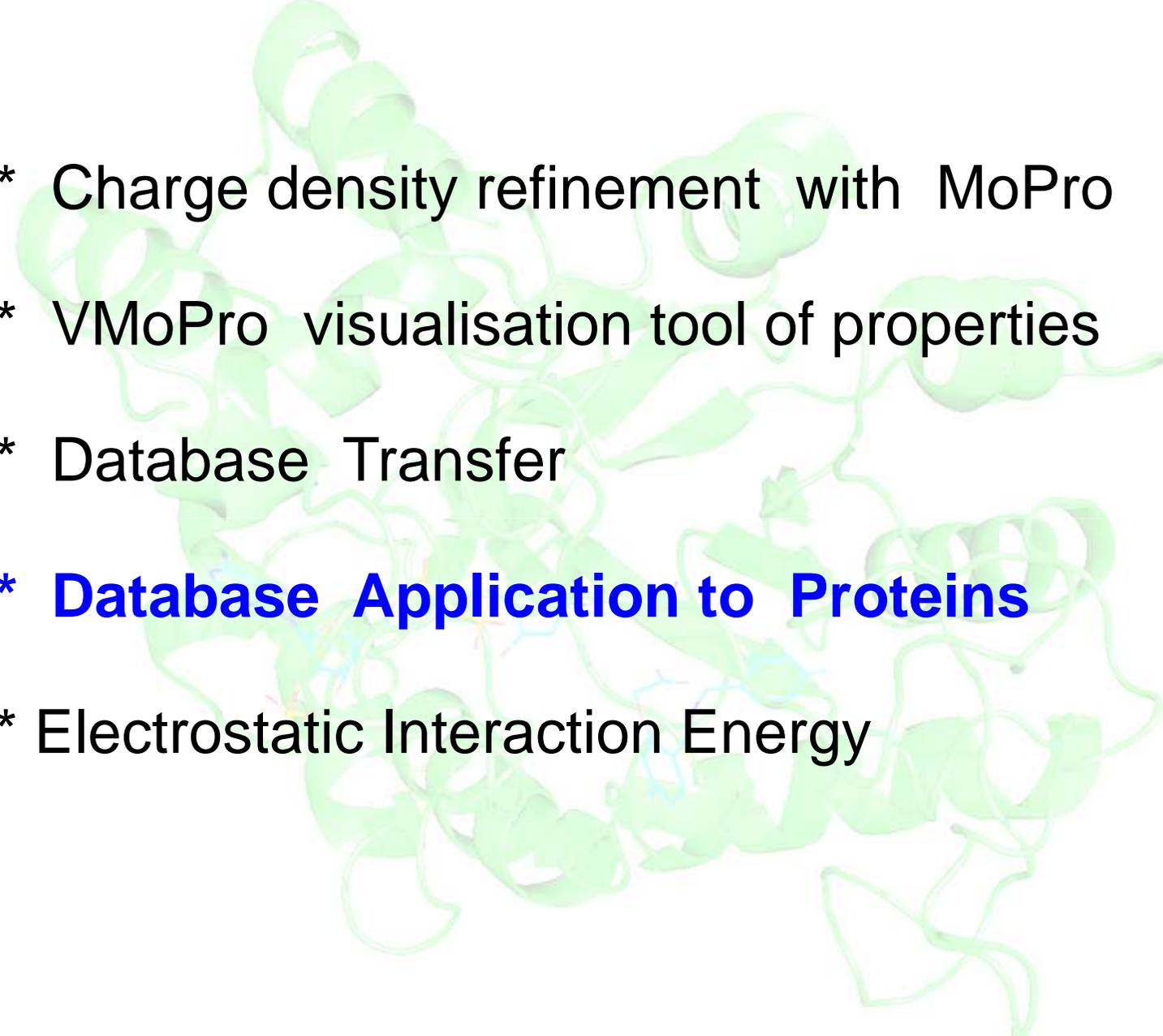
- significantly **lowers** the conventional **R-factor** (1% or more)
- **improves** the determination of **bonds and angles** to within 0.002-0.003 Å and 0.09-0.17° of values obtained from a complete multipolar refinement of high-resolution datasets
- **improves** the determination of **phase** angles by 2-6° compared to the standard independent atom refinement (IAM)
- **removes** majority of the bonding features from the **residual** Fourier difference maps
- **improves** atomic **displacement parameters** (ADPs) and results of the Hirshfeld rigid-bond test

Volkov et al Acta Cryst D, 2007, D63, 160



Main applications of the databases published so far

- Electron Density Transfer & Refinement of small molecules
- increasing precision of the refined Flack parameter (Dittrich, Strumpel *et al.*, 2006)
- used as a starting point in refinement of the constrained multipolar parameters of Proteins (Jelsch *et al.*, 2000; Guillot *et al.*, 2008)
- calculation of the electrostatic interaction energy (Li *et al.*, 2006; Dominiak *et al.*, 2007; Dominiak *et al.*, 2009; Fournier *et al.*, 2009)
- modelling of ED of disordered groups & detecting disorder (Dittrich *et al.*, 2007; Bąk *et al.*, 2009; Dittrich, Warren *et al.*, 2009)
- calculation of electrostatic potential of macromolecules (Muzet *et al.*, 2003; Liebschner *et al.*, 2009; Dittrich, Weber *et al.*, 2009; Dittrich *et al.*, 2010)

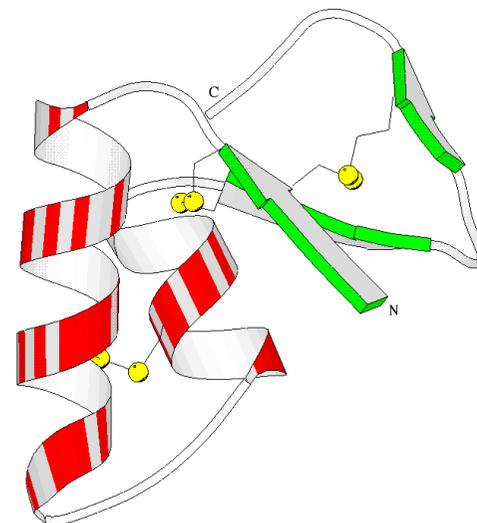
- 
- * Charge density refinement with MoPro
 - * VMoPro visualisation tool of properties
 - * Database Transfer
 - * **Database Application to Proteins**
 - * Electrostatic Interaction Energy

Protein Crambin

0.54 Å resolution

Database Transfer & Refinement

average polypeptide
Electron Density



Peptide

ab initio calculation

Hartree-Fock

self-consistent field

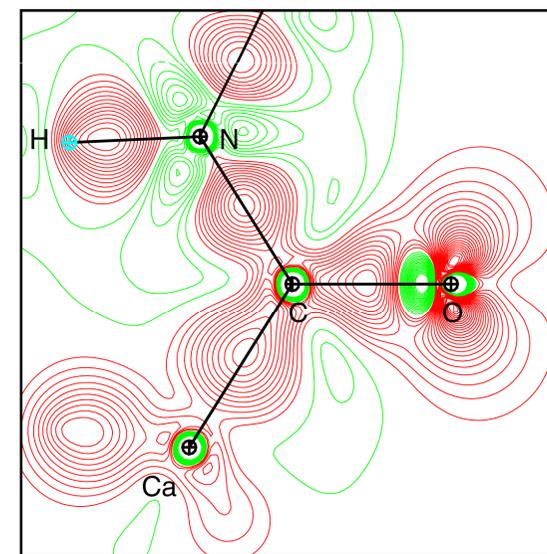
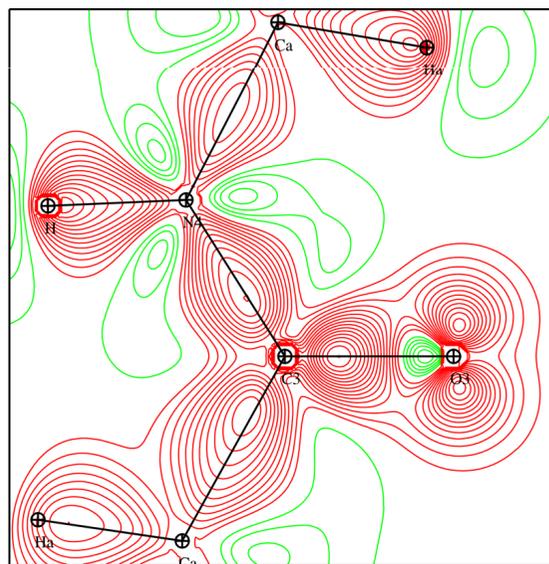
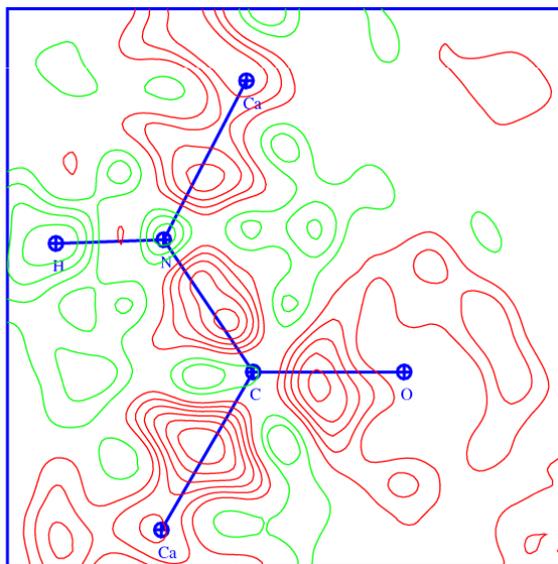
triplezeta-plus-

(C,N,O-*d* and H-*p*)-

polarization-function

Gaussian basis set.

Spherical Residual & Static Deformation

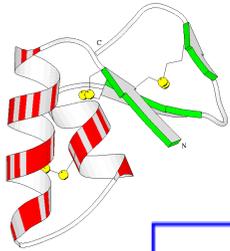


Jelsch *et al.*, P.N.A.S. 2000, 97.

+/- 0.05 e⁻/Å³

Corr = 88% |Δρ| = 0.18 & 0.20 e/Å³

Crambin Residual Electron Density



Spherical

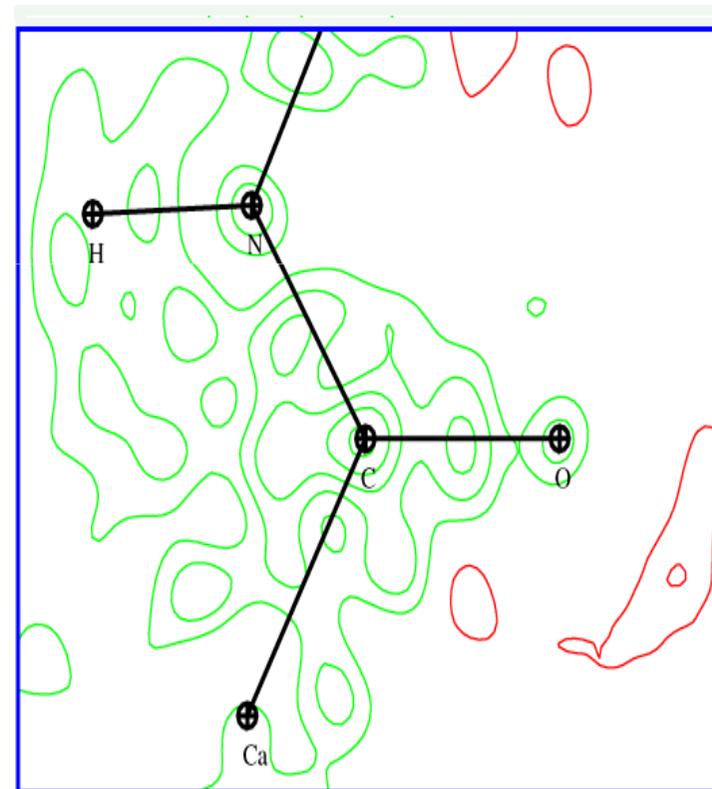
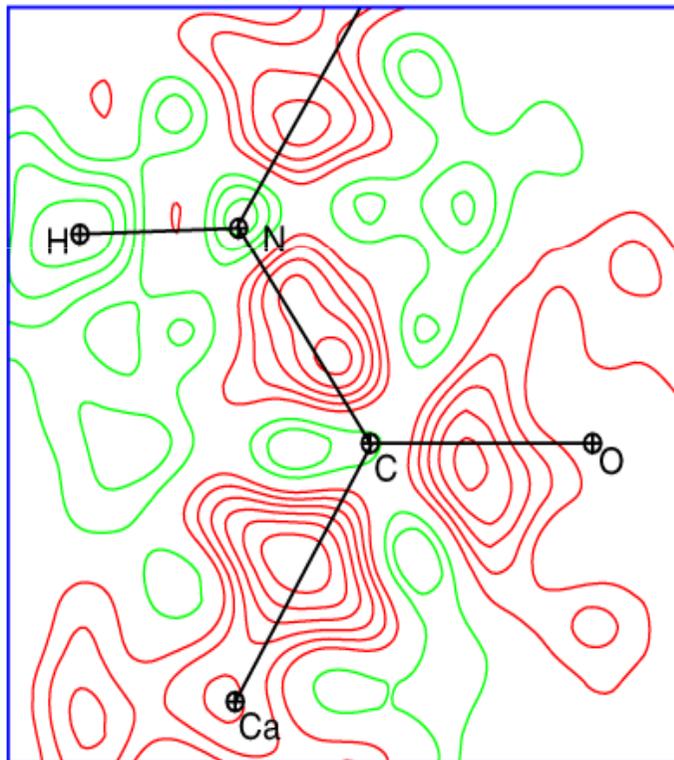
Atom Model

Multipolar

Database

Transfer

& Refinement



+/- 0.02 e⁻/Å³

Average 34 peptides

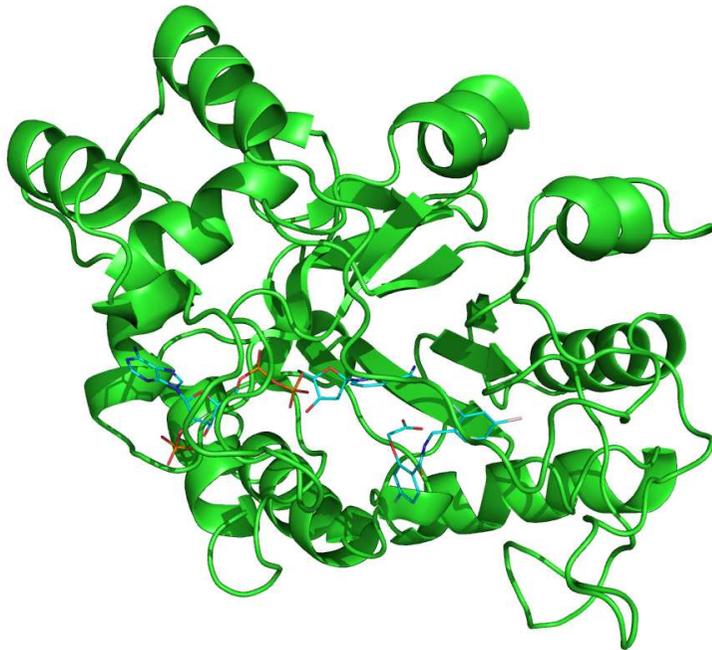
Human Aldose Reductase

Résolution 0.65 Å

Collab. Podjarny *et al.*

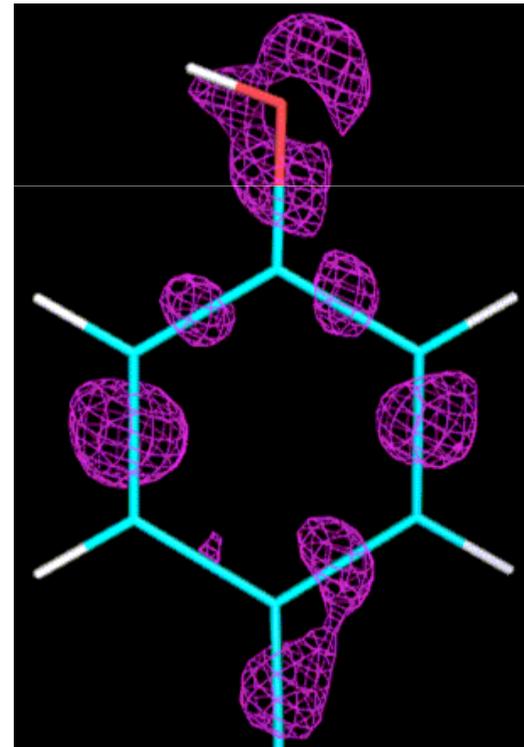
IGBMC Strasbourg

Complications Diabetis



Spherical Atom Model

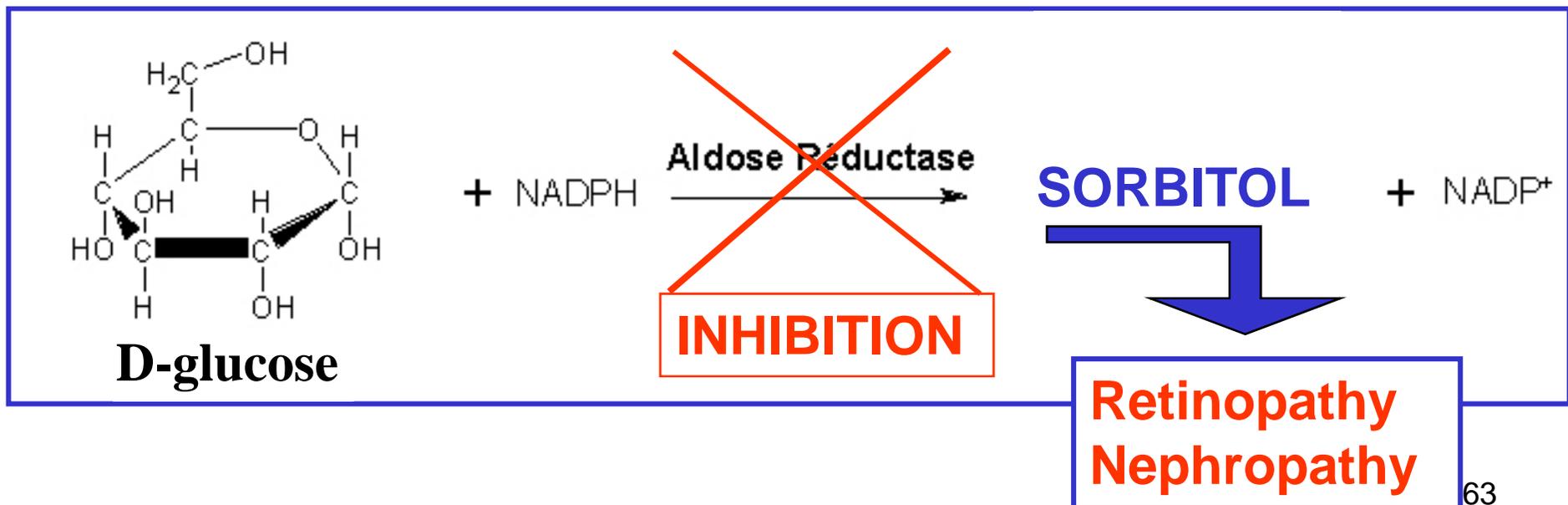
Residual electron density



The Human Aldose Reductase

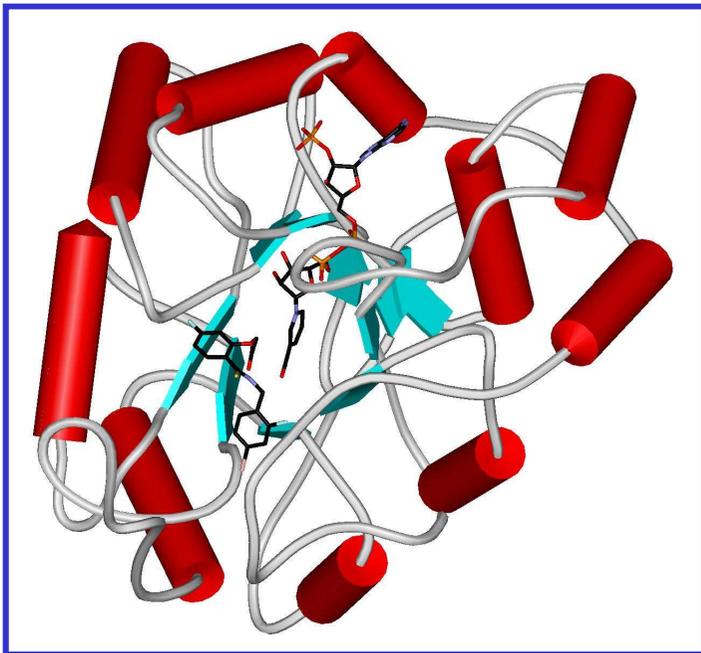
Involved in Diabetes complications

- ◆ Normal conditions : glycolysis (hexokinase adds phosphate)
- ◆ Hyperglycemic conditions : the polyol pathway

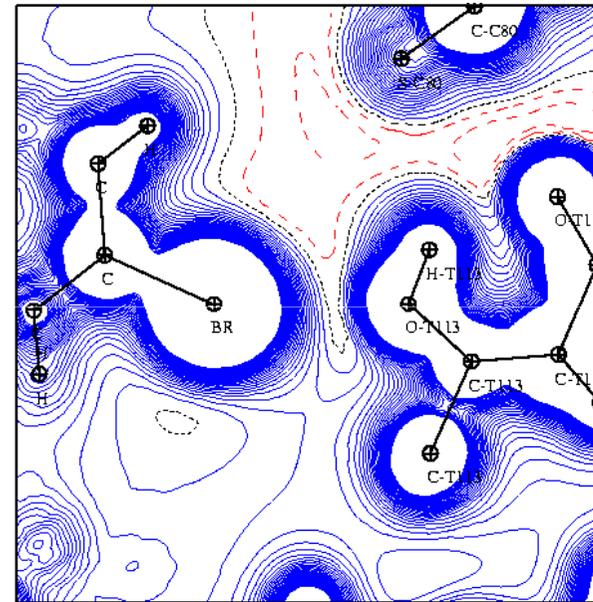


Aldose Réductase Humaine

Enzyme & NADP⁺ & Inhibiteur



Ligand IDD - Protéine



Complementarity

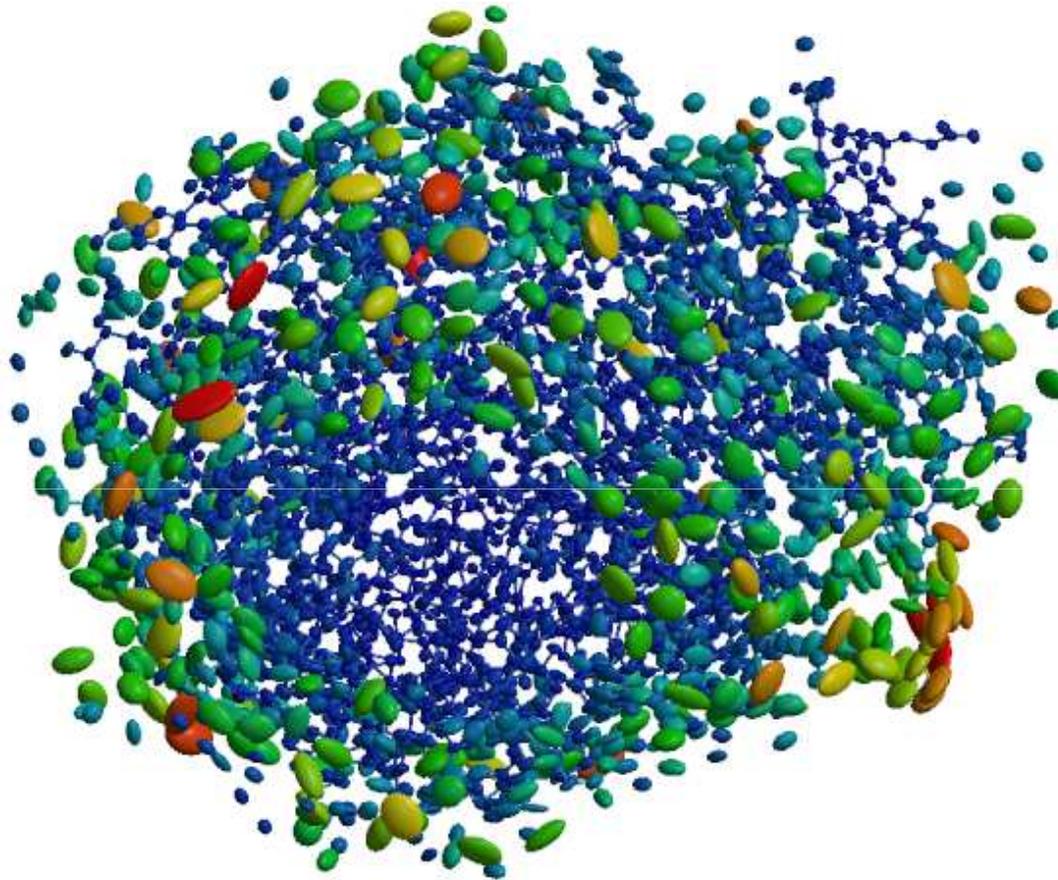
Electrostatic Potential

& Deformation Density

Muzet et al. P.N.A.S. 2003

Thermal ellipsoids

h. Aldose Reductase



(Blue) $2.41 < B_{eq} < 51 \text{ \AA}^2$ *(Red)*

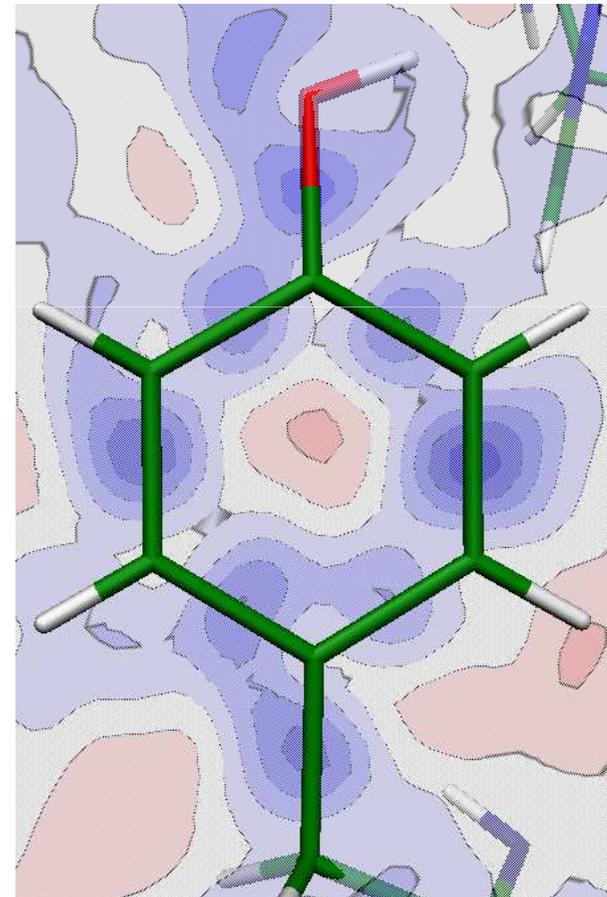
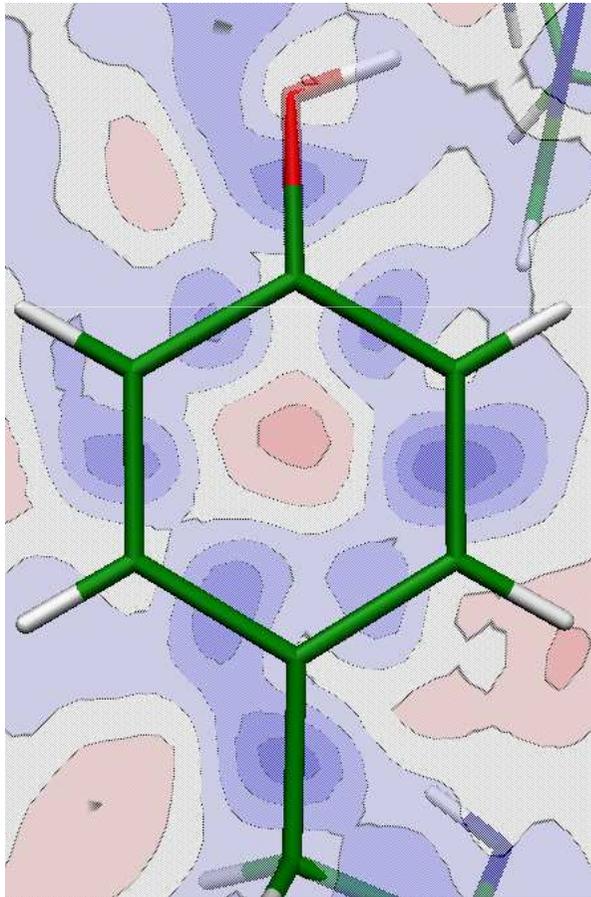
50% probability level

Residual electron density Aldose Reductase

spherical atom

standard
refinement

high order
refinement.



tyr48

-0.5 e/Å³



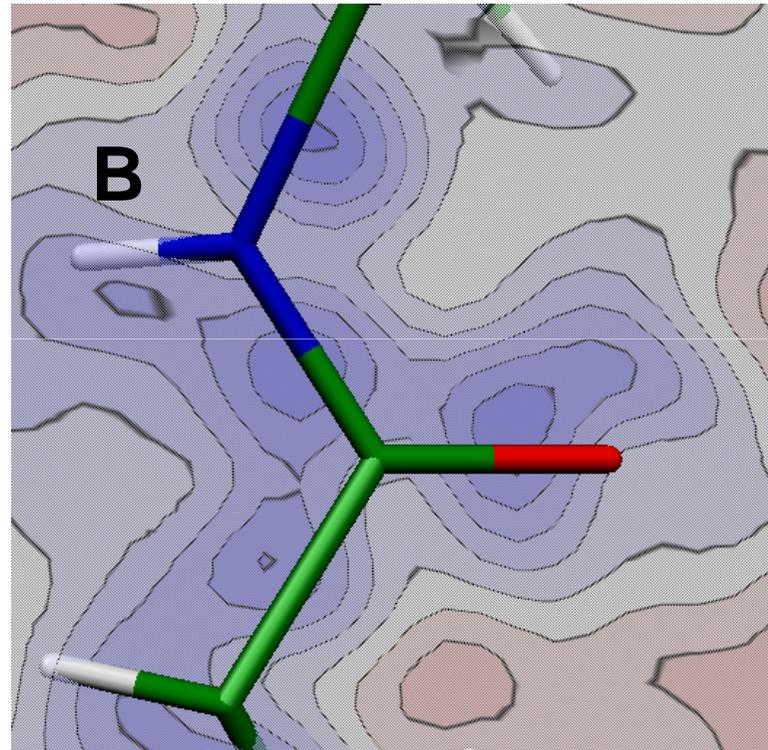
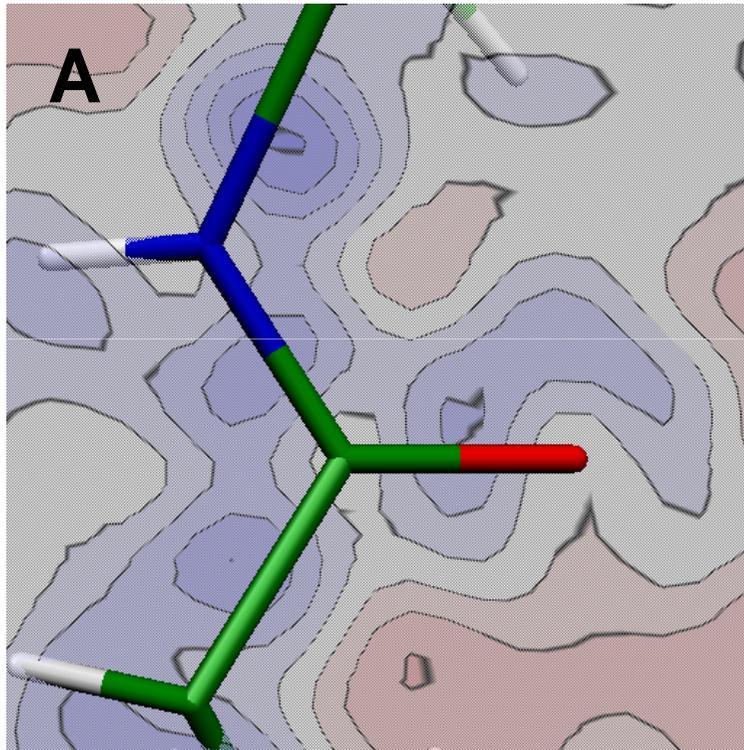
+0.5 e/Å³⁶⁶

Residual electron density following transfer

A: standard spherical refinement.

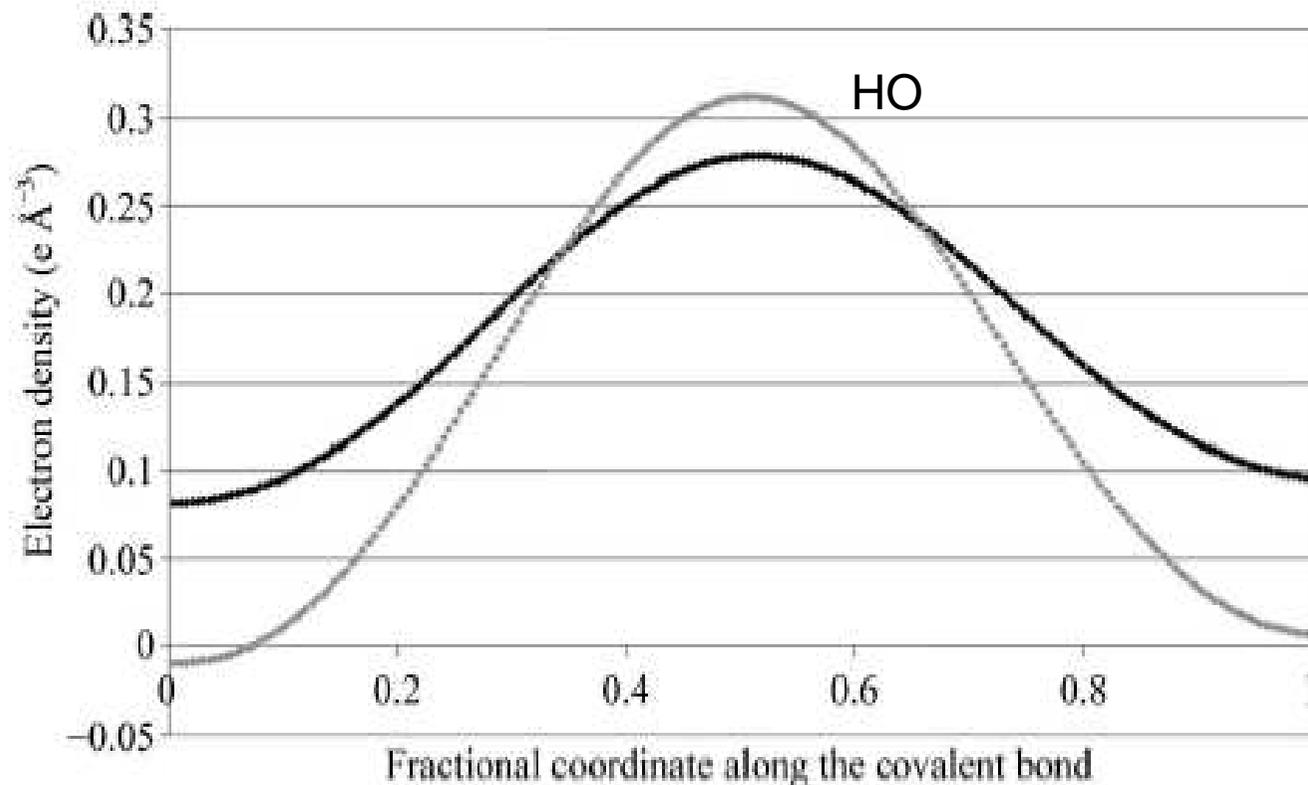
Lys262

B: high order refinement.



-0.45 e/Å³

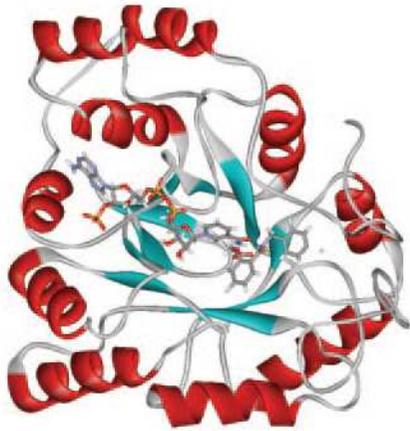
+0.45 e/Å³



Average residual electron-density profile along covalent bonds between non-H atoms of the subsystem refined against high-resolution data: black curve, after IAM refinement; grey curve, after IAM HO refinement.

Main Chain Constrained Multipolar Refinement

Protein Human Aldose Reductase



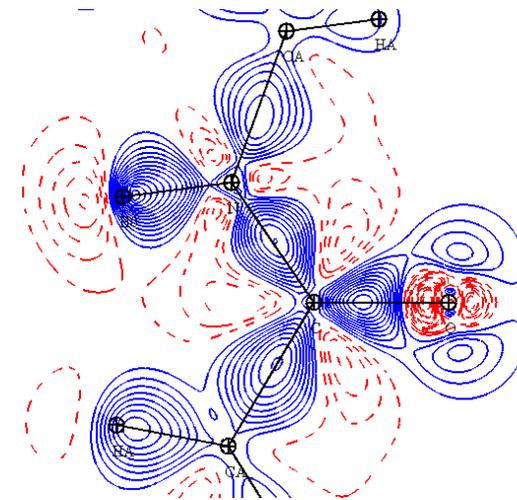
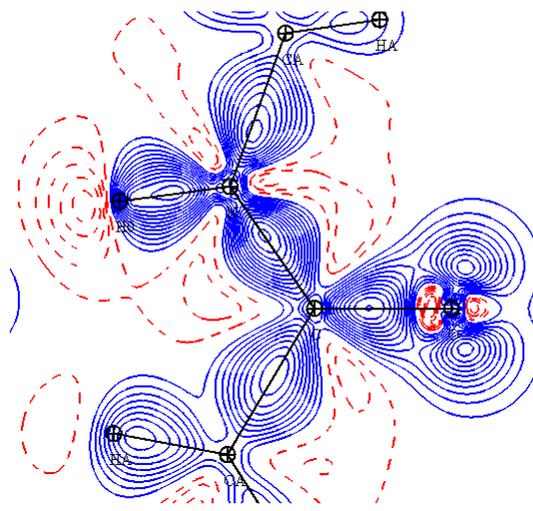
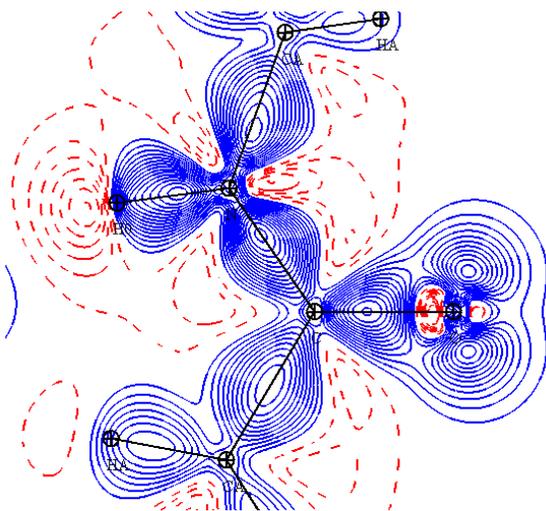
0.66 Å resolution

$\Delta\rho$ contour
+/- 0.05 e/Å³

**DATABANK
TRANSFER**

**DATABANK
TRANSFER +
REFINEMENT**

**REFINEMENT
from $\Delta\rho = 0$**



Aldose Reductase Statistical Improvement

Transfer, all ordered protein atom, except IDD594

	Spherical	Transfer	Transfer & Refine Constrained Multipoles	Refine
$R(F)$ (%)	9.28	8.79	8.71	8.86
$R_{\text{free}}(F)$	9.45	9.16	9.12	9.30



Multipolar refinement

Aldose Reductase

Main Chain Valence Electron populations

	Transfer	Trf + Ref	Ref
Cα	4.12	4.06(2)	4.02(2)
C	3.89	3.92(2)	3.97(2)
O	6.31	6.30(2)	6.15(2)
N	5.32	5.24(2)	5.09(2)
Hα	0.81	0.89(3)	0.92(3)
H0	0.69	0.76(3)	0.85(3)

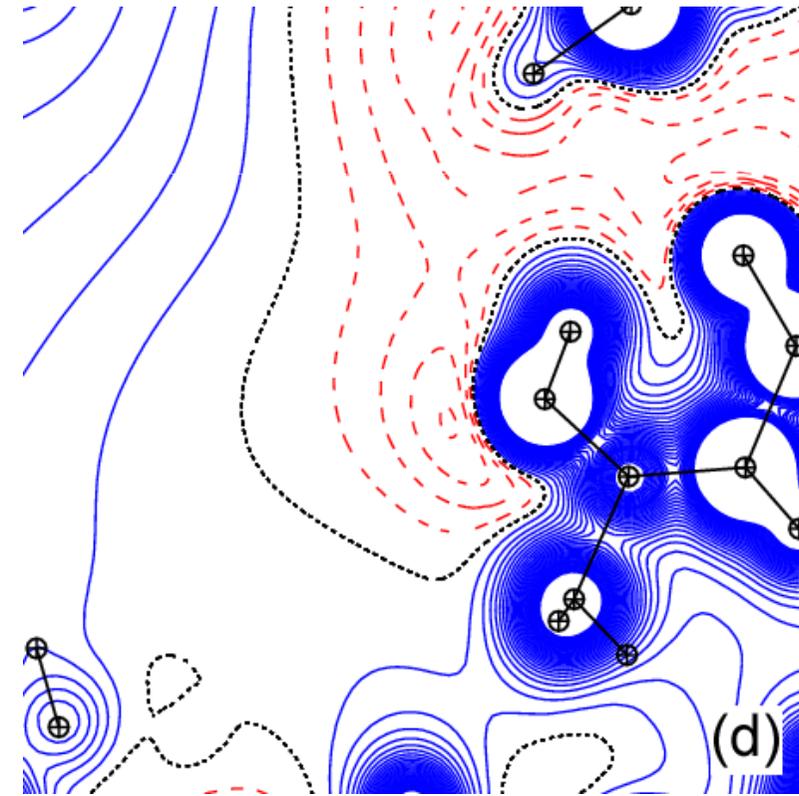
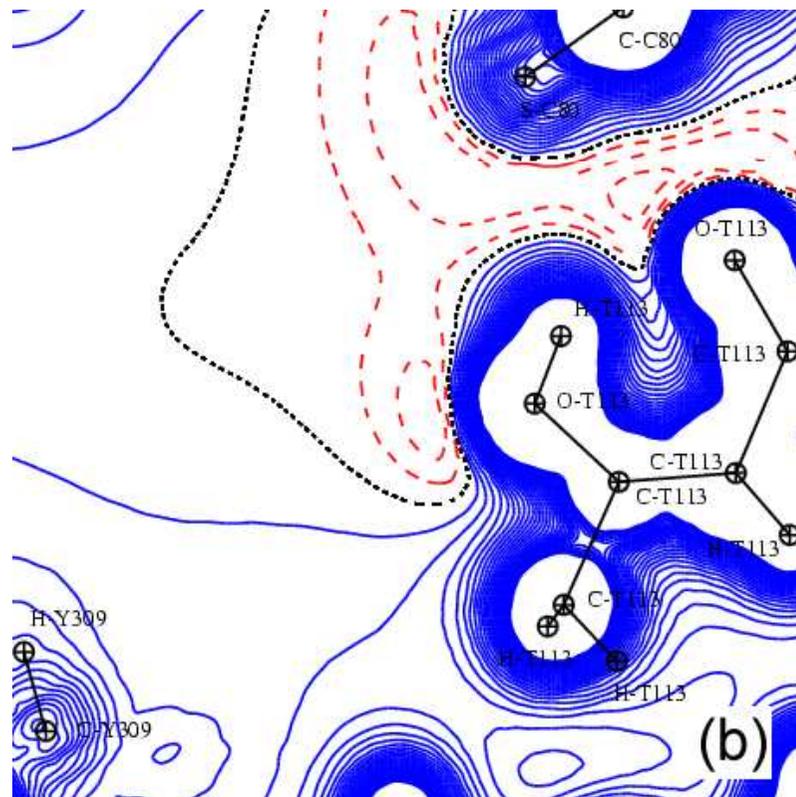
Electrostatic potentials : Inhibitor binding

Aldose reductase

Active site Bromine anchor point

DFT

Experimental



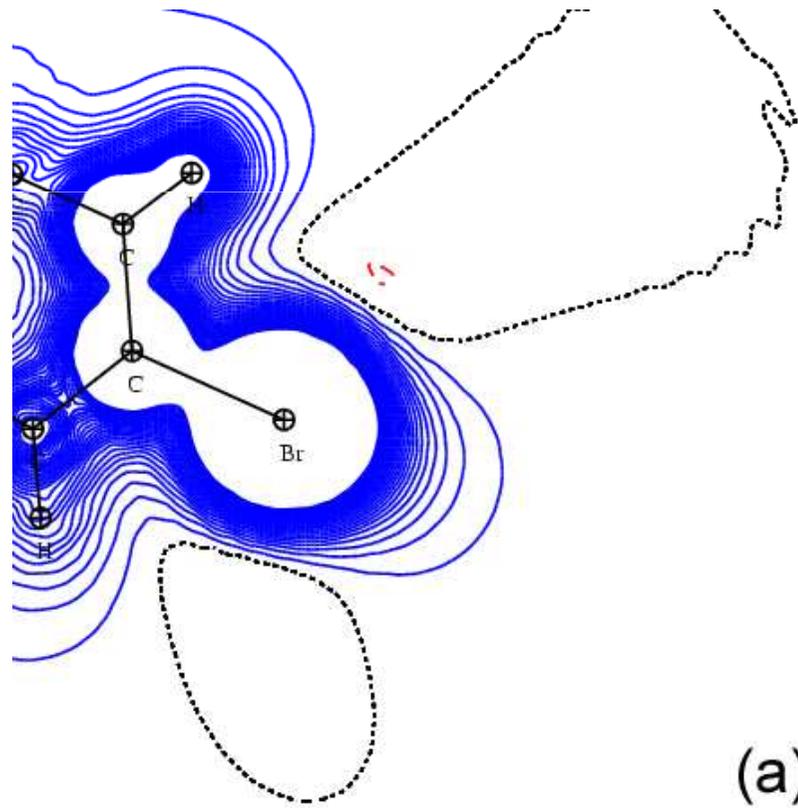
0.05 e.Å⁻¹

Electrostatic potentials : Inhibitor binding

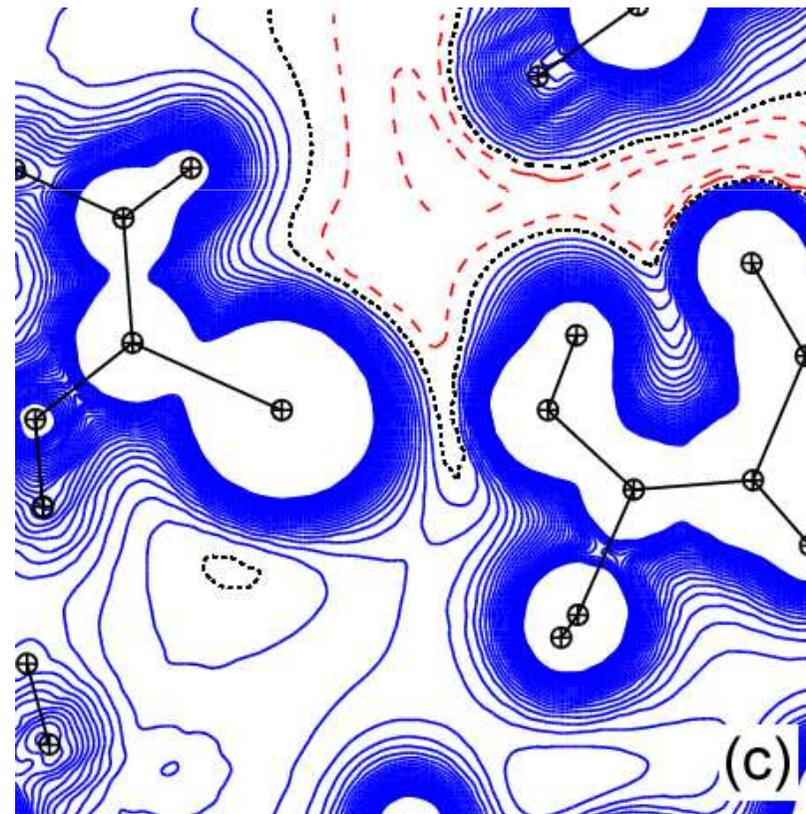
Complex Active site DFT calculation

inhibitor : Bromine

BR ... Og(THR)

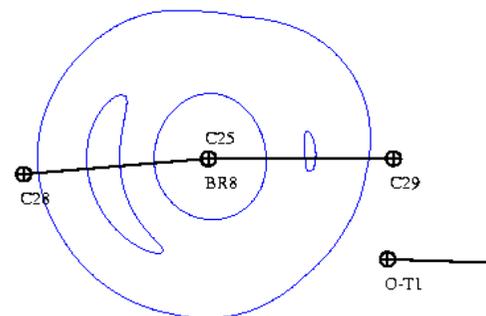
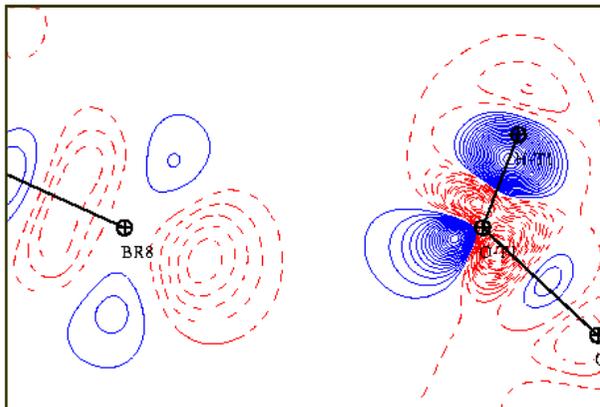


(a)

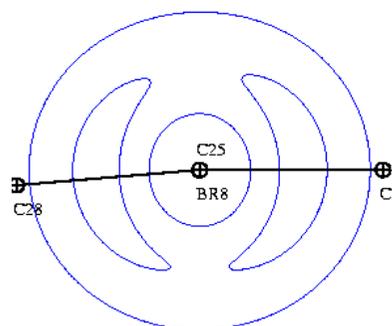
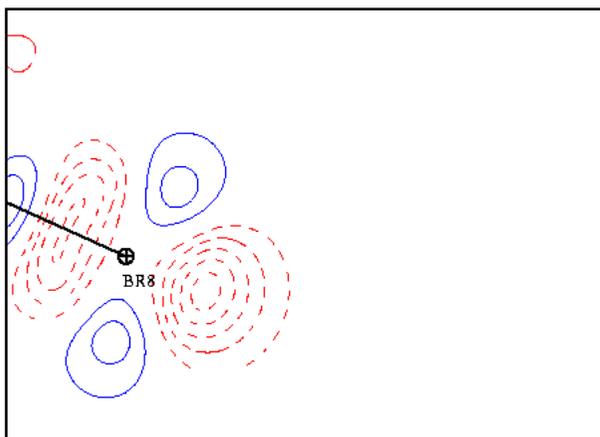


(c)

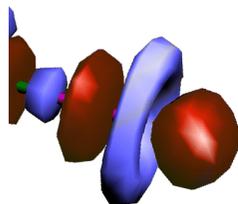
Theoretical Deformation Electron Density DFT



Br...OG1-Thr113
inhibitor aldose reductase NADP+



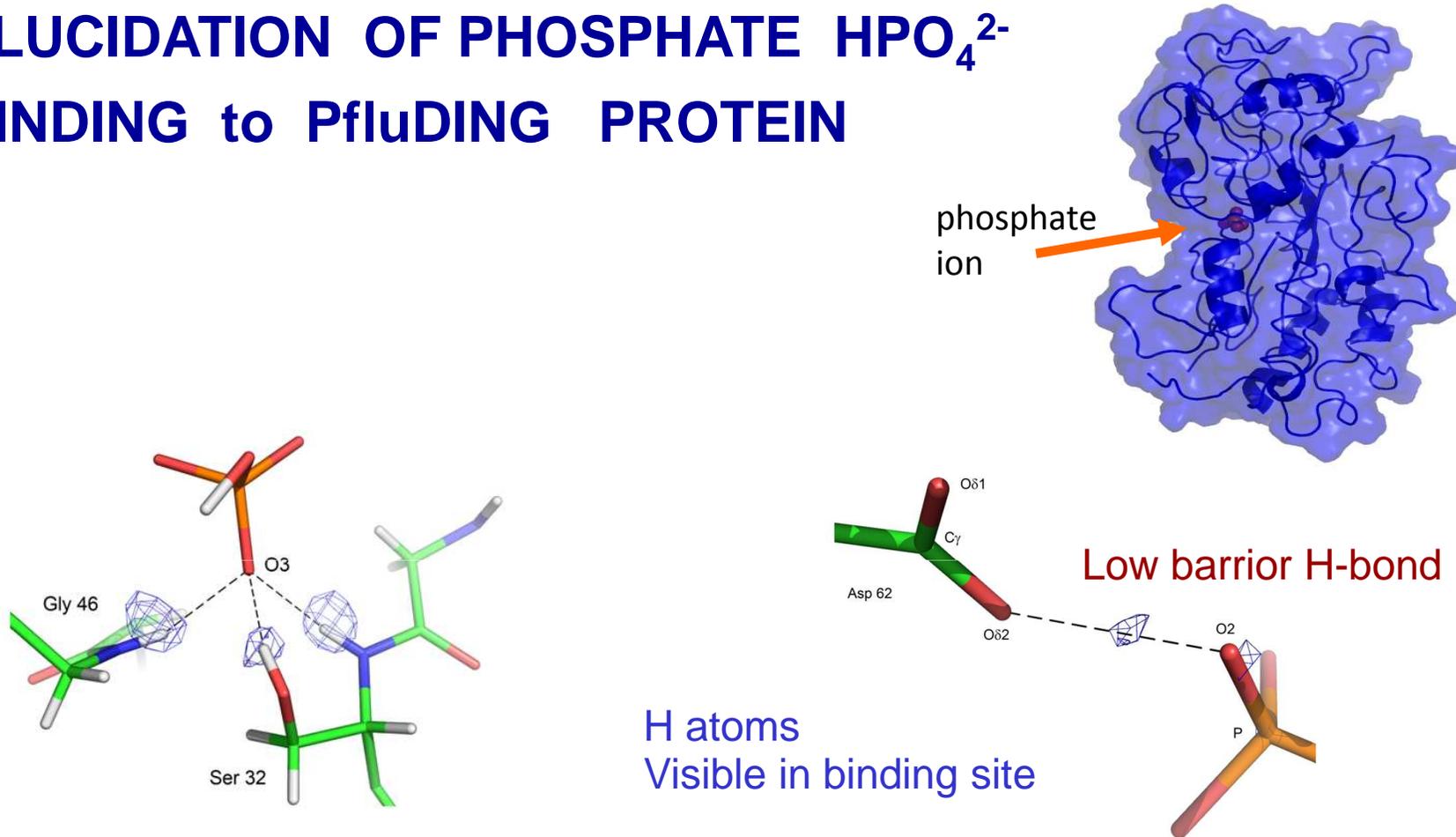
Inhibitor alone



+/- 0.05 e-/Å³

SIESTA software

ELUCIDATION OF PHOSPHATE HPO_4^{2-} BINDING to PfluDING PROTEIN

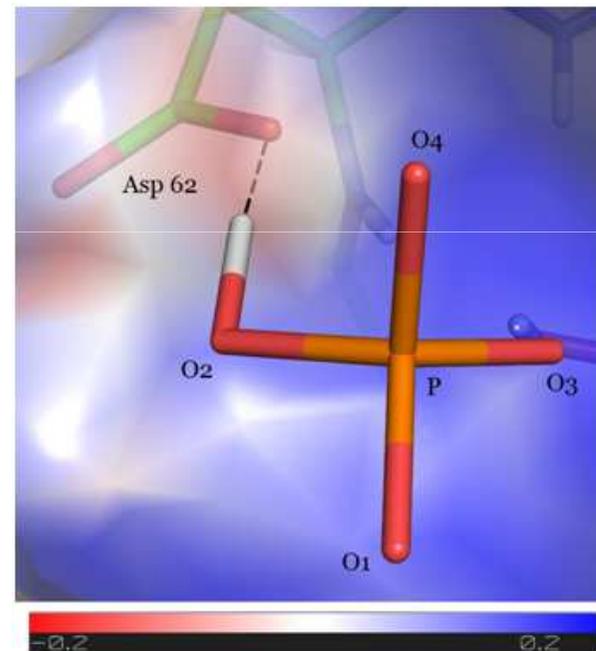


PfluDING is a bacterial protein isolated from *Pseudomonas fluorescens*. The three-dimensional structure was obtained at sub-Ångstrom resolution (0.88Å and 0.98Å) at two different pH (4.5 and 8.5).

ELUCIDATION of PHOSPHATE HPO_4^{2-} BINDING to PfluDING PROTEIN

Contrary to previous theories on phosphate binding proteins, ELMAM multipolar database electrostatic potential calculations show that the binding cleft has a positive electrostatic potential

The PfluDING structures reveal that the protein is specific for the dibasic form of phosphate (notably HPO_4^{2-} vs. SO_4^{2-}).



Electrostatic potential

Liebschner *et al.*, JACS, 2009

- * Charge density refinement with MoPro
- * VMoPro visualisation tool of properties
- * Database Transfer
- * Application to proteins
- * **Electrostatic Interaction Energy**

Electrostatic Interaction Energy

Integration $E_{\text{electrostatic}} = \iiint_V \rho_1 \cdot \Phi_2 \cdot dv$

ρ
electron
density
from :

- * refinement vs. Xray diffraction data
- * refinement vs. theoretical data
- * experimental databank transfer
- * theoretical databank transfer

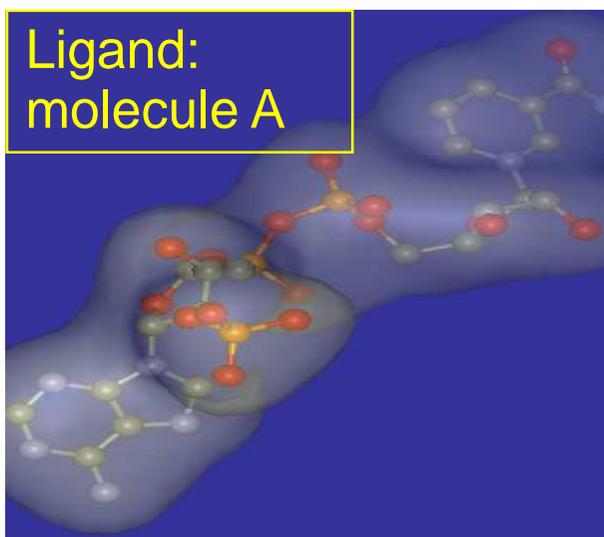
Electrostatic Interaction Energy

(1) $E_{total, electrostatic} = \sum_{grid} w_i \cdot \rho_A(\mathbf{r}_i) \cdot V_B(\mathbf{r}_i)$ **VMoPro**

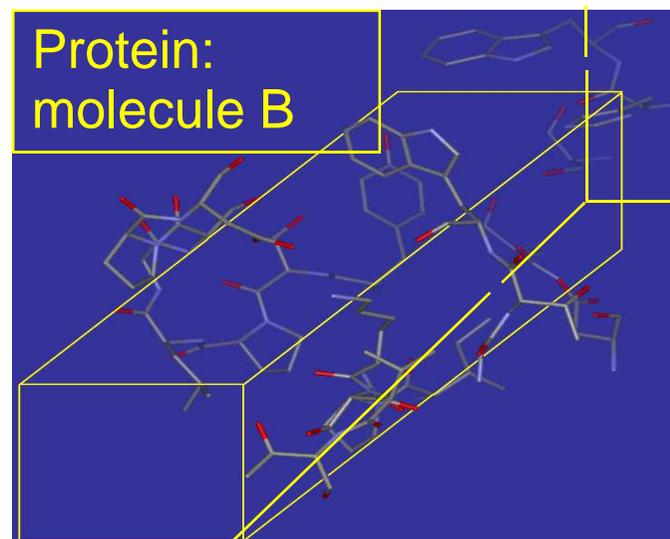
- * High Order Numerical Grid Integration (Taylor formulas 5th order)
- * Zooming on regions with large variations

(2) SP : spherical integration

(3) BU : spherical integration / Buckingham summation



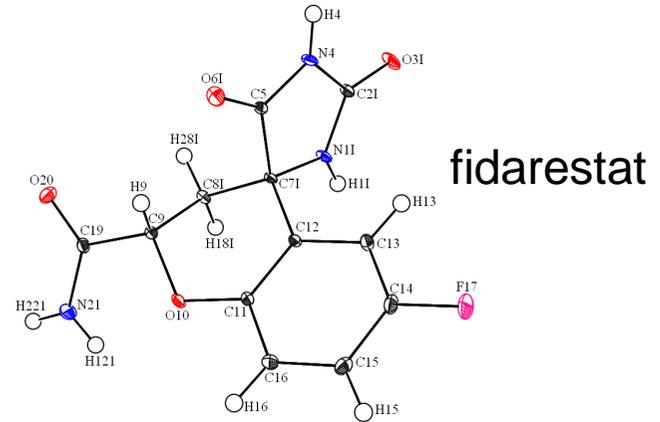
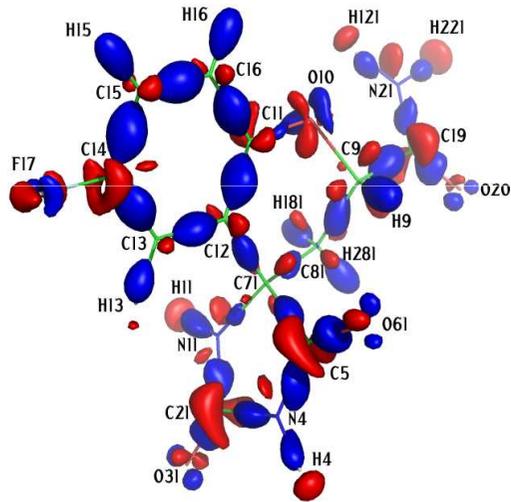
Charge density $\rho_A(\mathbf{r})$



Electrostatic potential $V_B(\mathbf{r})$ ⁷⁹

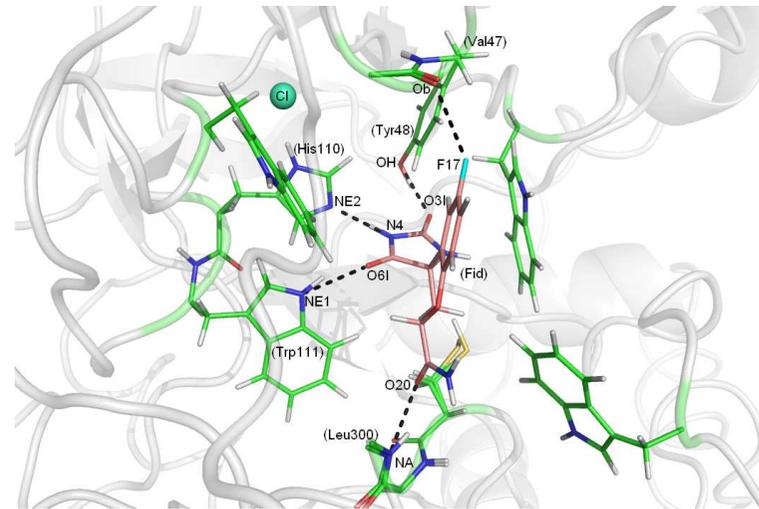
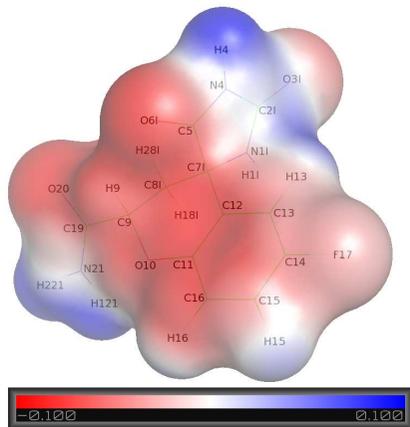
Protein / Ligand Electrostatic interaction energy.

Experimental deformation
electron density
resolution = 0.50 Å

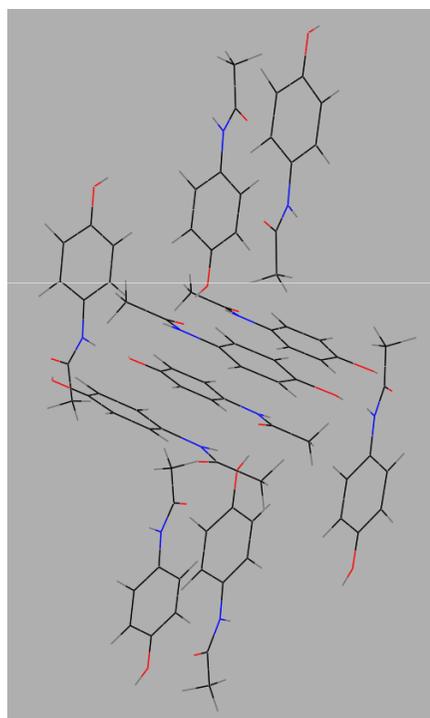


Fidarestat Inhibitor /
Human Aldose Reductase

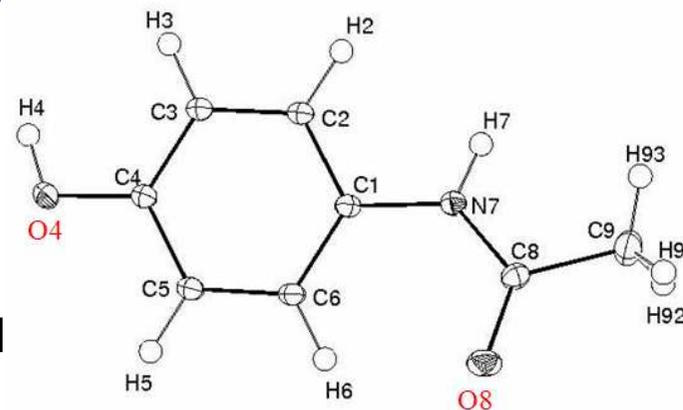
Electrostatic
Potential on
van der Waals
surface



Electrostatic Interaction Energy between dimers in the crystal packing



Paracetamol



Dimer #	Atom 1	Atom 2	Distance (Å)	Symmetry	E_{det} kcal/mol
1	O4	H7	1.9275	$X-\frac{1}{2} ; -Y+\frac{1}{2} ; Z-\frac{1}{2}$	-15.23
	H7	O4	"	$X+\frac{1}{2} ; -Y+\frac{1}{2} ; Z+\frac{1}{2}$	"
2	O8	H4	1.6966	$X-\frac{1}{2} ; -Y+\frac{1}{2} ; Z+\frac{1}{2}$	-11.15
	H4	O8	"	$X+\frac{1}{2} ; -Y+\frac{1}{2} ; Z-\frac{1}{2}$	"
3	H92	O8	2.7062	$-X+\frac{3}{2} ; Y-\frac{1}{2} ; -Z+\frac{3}{2}$	-9.86
	O8	H92	"	$-X+\frac{3}{2} ; Y+\frac{1}{2} ; -Z+\frac{3}{2}$	"
4	H92	H4	2.6565	$-X+2 ; -Y ; -Z+1$ (inv)	-5.69
5	H93	H2	2.5015	$-X+\frac{5}{2} ; Y-\frac{1}{2} ; -Z+\frac{3}{2}$	-0.32
	H2	H93	"	$-X+\frac{5}{2} ; Y+\frac{1}{2} ; -Z+\frac{3}{2}$	"
6	H6	H6	2.2263	$-X+1 ; -Y ; -Z+1$ (inv)	-0.01
7	H5	H4	2.7269	$-X+\frac{3}{2} ; Y-\frac{1}{2} ; -Z+\frac{1}{2}$	1.71
	H4	H5	"	$-X+\frac{3}{2} ; Y+\frac{1}{2} ; -Z+\frac{1}{2}$	"

Bouhaida *et al.*
Acta Cryst B 2009

Closest
atoms

Tutorial MoPro

1) Database transfer & structure refinement

molecule with diffraction data at usual resolution

2) Charge density refinement

data at ultra high resolution (0.5 Å)

Acknowledgements to MoPro developpers

Angélique Lagoutte

Sophie Alexandre

Bertrand Fournier

Dorothee Liebschner

Slawomir Domagala

Ignasi Mata

Benoît Guillot



& students programming MoProGUI

Thanks to the organizers Claude Lecomte & Fernando J. Lahoz

Nancy

