

Analyse structurale par la fonction de distribution de paires.

Pierre BORDET

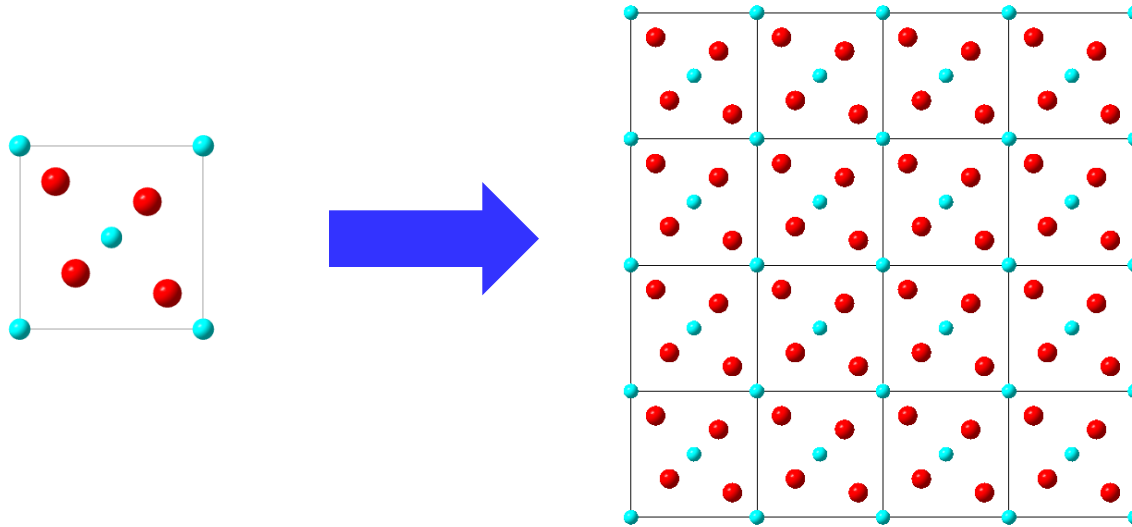
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ÆCIPROCS

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La cristallographie étudie et «utilise » les cristaux pour comprendre la structure des matériaux



Les cristaux sont périodiques et symétriques
c'est pourquoi la diffraction (RX, etc...) est si efficace
pour les étudier

On sait (en général) déterminer la structure d'un monocristal

Or, tous les matériaux ne sont pas naturellement monocristallins

On veut connaître leur structure

=> **idée 1** = en faire des monocristaux
(ex : chimie du solide, petites molécules, bio structurale...)

Mais,

ça ne marche pas toujours,
on veut connaître la structure du matériau « réel » (désordre, poudre, nano...)
on veut l'étudier « in situ », «in operando », etc...

=> **idée 2** = méthodes d'étude structurale de matériaux non monocristallins
=> poudres, amorphes, désordre, multiphases.....

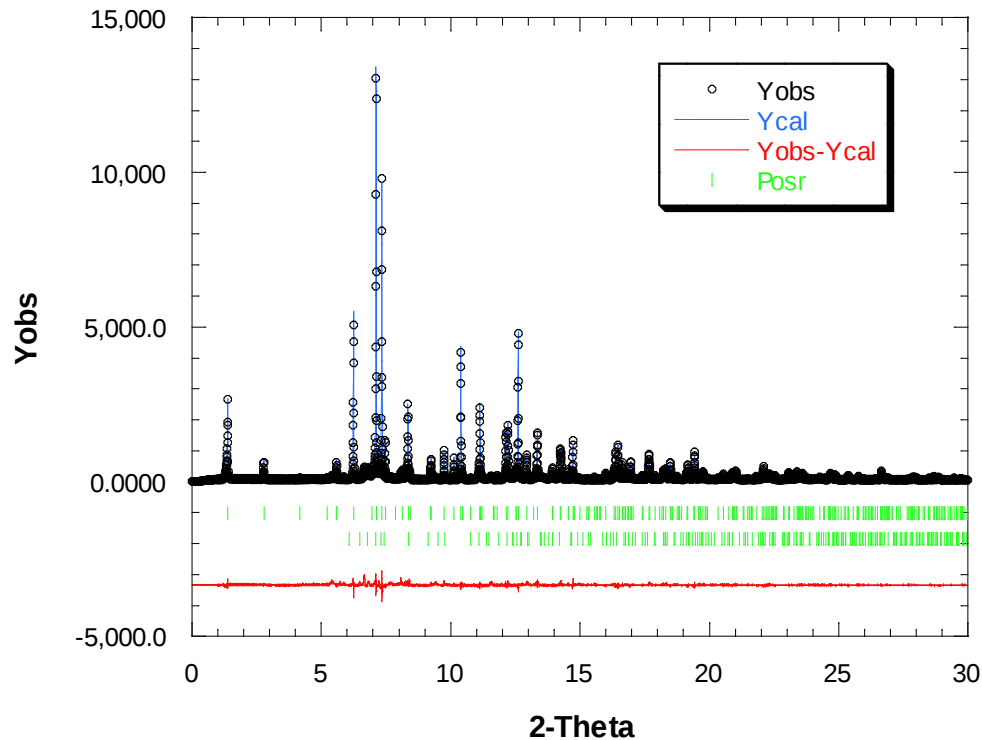
Diffraction, spectroscopies (IR, Raman, RMN), microscopie électronique , SAXS, EXAFS...

Analyse de la diffusion totale par la fonction de distribution de paires

Diffraction de poudres : méthode de Rietveld

$$y_{ci} = y_{bi} + \sum_{\Phi=1}^N S_{\Phi} \sum_{k=k1}^{k2} j_{\Phi k} \cdot Lp_{\Phi k} \cdot O_{\Phi k} \cdot M \cdot |F_{\Phi k}|^2 \cdot \Omega_{i\Phi k}$$

$$F_{hkl} = \sum_{j \in cell} f_j T_j \exp(2i\pi(hx_j + ky_j + lz_j))$$



On ne s'intéresse qu'aux pics de Bragg
= aspect cristallin ordonné.

Tous ce qui est non-cristallin :
« bruit de fond »
« diffusion diffuse »

Pour étudier le matériau réel :
modéliser la diffusion totale

Expériences de diffraction avec un “mauvais” cristal ??

Cristal ordonné + désordre partiel

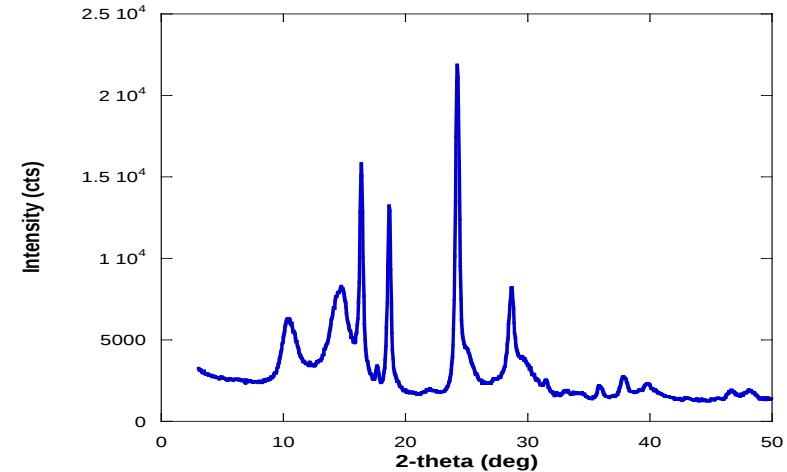
espace direct:

on peut définir une structure

moyenne $\neq$ structure locale ($\Rightarrow$ désordre)

espace réciproque :

présence de pics de Bragg + fond diffus



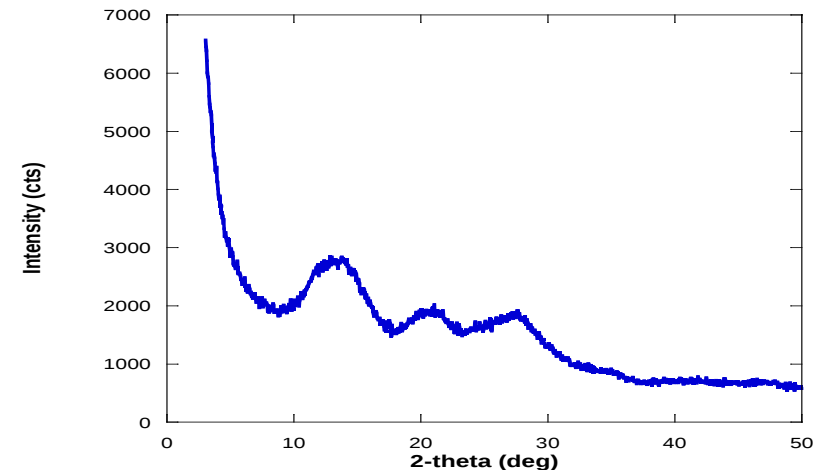
Domaines nano-cristallins

espace direct:

structure bien définie dans des
domaines très petits (qq nm) $\neq$ amorphe

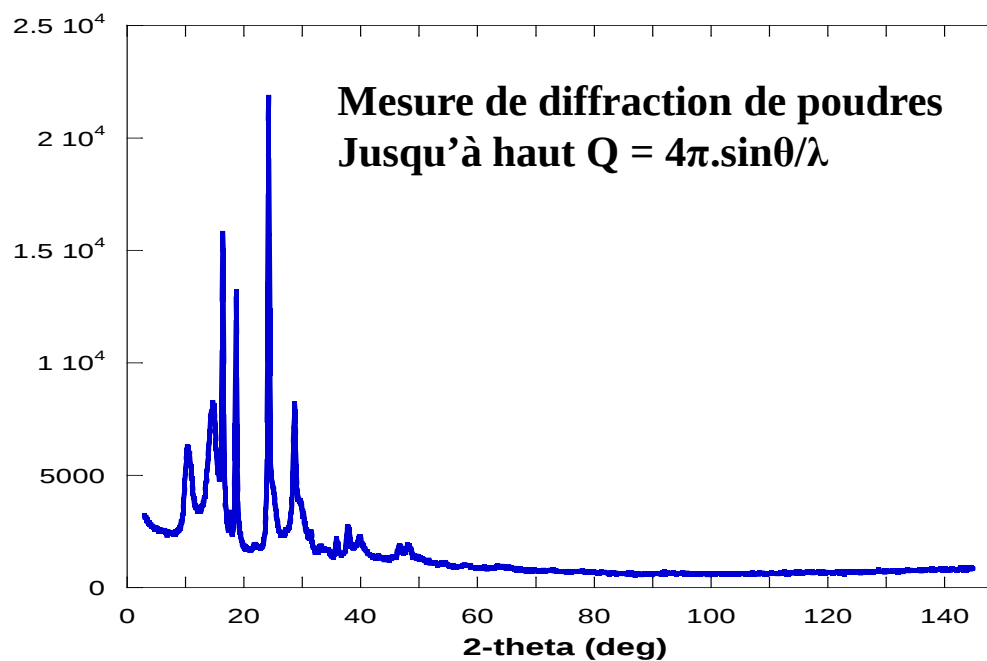
espace réciproque:

pics de Bragg larges ou absents, selon
la taille des domaines



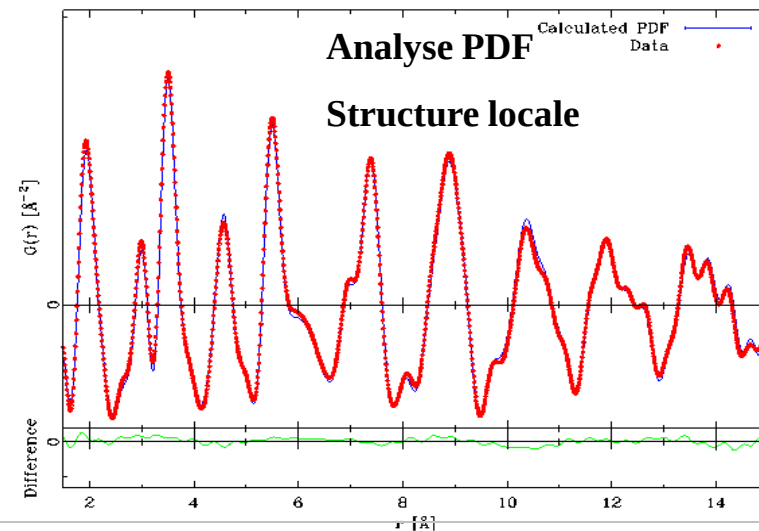
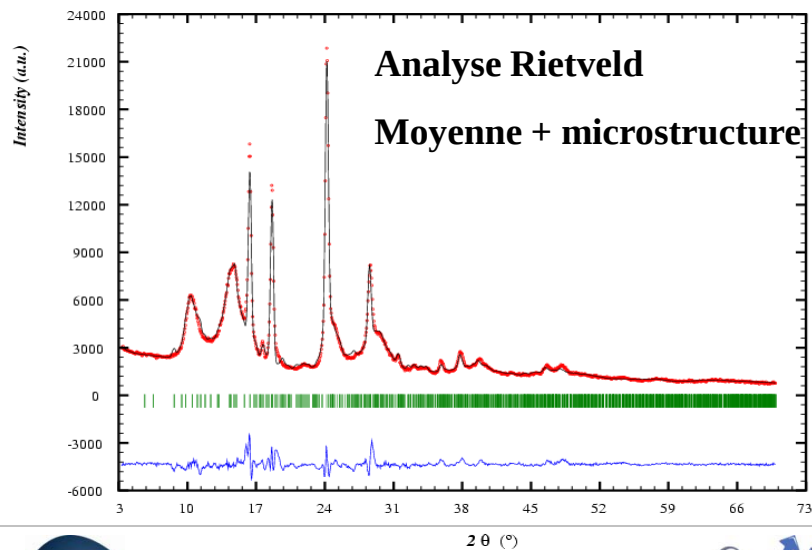
Espace
Réciproque

Intensity (cts)



Espace direct

Diffusion Totale



Intensité diffusée = section efficace différentielle élastique (échantillon quelconque)

$$\frac{d\sigma}{d\Omega} = I(\vec{Q}) = \left\langle A(\vec{Q}) A^*(\vec{Q}) \right\rangle = \sum_{j=1}^N \sum_{k=1}^N f_j f_k^* \left\langle e^{i\vec{Q} \cdot (\vec{r}_j - \vec{r}_k)} \right\rangle$$

< > : moyenne temporelle,
 $\vec{Q}$: vecteur diffusion
 f : facteur de diffusion

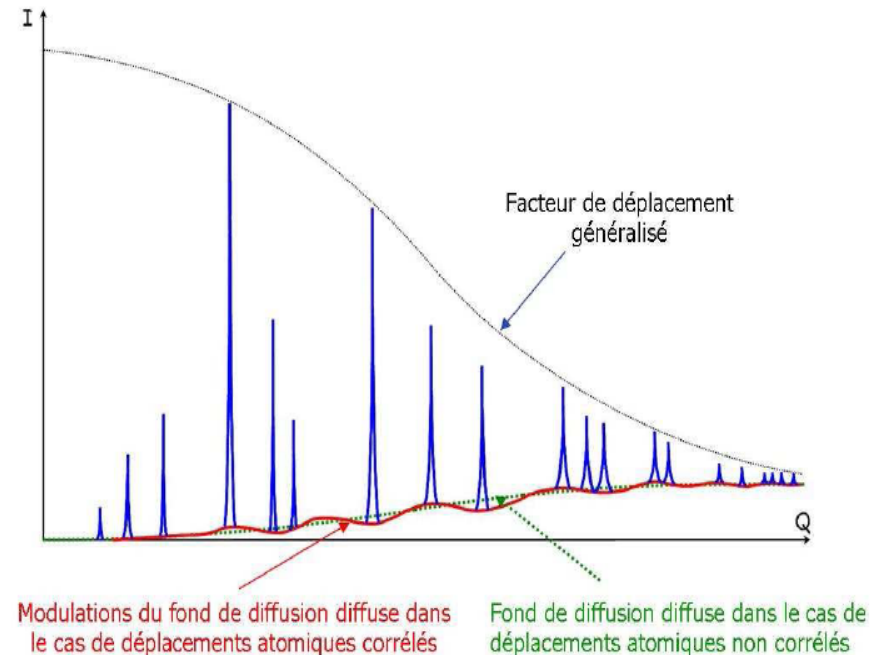
Si on peut définir une structure moyenne ($\vec{r} = \vec{R} + \vec{u}$)

$$I(\vec{Q}) = I_B(\vec{Q}) + I_D(\vec{Q})$$

avec
$$\begin{cases} I_B(\vec{Q}) = (2\pi)^3 \frac{N_m}{V_m} \sum_{hkl} |F_{hkl}(\vec{Q})|^2 \delta(\vec{Q} - \vec{G}_{hkl}) \\ F_{hkl}(\vec{Q}) = \sum_j f_j e^{2\pi i(hx_j + ky_j + lz_j)} \left\langle e^{i\vec{Q} \cdot \vec{u}_j} \right\rangle \end{cases}$$
 Bragg

$$I_D(\vec{Q}) = \sum_j \sum_k f_j f_k^* e^{i\vec{Q} \cdot (\vec{R}_j - \vec{R}_k)} \left(\left\langle e^{i\vec{Q} \cdot (\vec{u}_j - \vec{u}_k)} \right\rangle - \left\langle e^{i\vec{Q} \cdot \vec{u}_j} \right\rangle \left\langle e^{-i\vec{Q} \cdot \vec{u}_k} \right\rangle \right),$$

$$I_D(\vec{Q}) = \sum_j |f_j|^2 \left(1 - \left\langle e^{i\vec{Q} \cdot \vec{u}_j} \right\rangle \left\langle e^{-i\vec{Q} \cdot \vec{u}_j} \right\rangle \right) + \sum_j \sum_{k \neq j} f_j f_k^* e^{i\vec{Q} \cdot (\vec{R}_j - \vec{R}_k)} \left(\left\langle e^{i\vec{Q} \cdot (\vec{u}_j - \vec{u}_k)} \right\rangle - \left\langle e^{i\vec{Q} \cdot \vec{u}_j} \right\rangle \left\langle e^{-i\vec{Q} \cdot \vec{u}_k} \right\rangle \right)$$



$$I(Q) = \vec{A} \cdot \vec{A}^* = \sum_{j,k=1}^N f_j f_k^* e^{i\vec{Q}(\vec{r}_j - \vec{r}_k)}$$

Diffusion : cinématique, statique

$$I(Q) = N \cdot \sum_j |f_j|^2 + \sum_{j \neq k} f_j f_k^* \frac{\sin(Q \cdot r_{jk})}{Q \cdot r_{jk}}$$

Intégration isotrope (poudre, liquide...):
autodiffusion + fonction d'interférence = formule de Debye

$$S(Q) - 1 = \frac{I(Q)}{N(\sum_j f_j)^2} - \frac{(\sum_j |f_j|^2)}{(\sum_j f_j)^2} = \frac{1}{N} \sum_{j \neq k} \frac{f_j f_k^*}{(\sum_j f_j)^2} \frac{\sin(Q \cdot r_{jk})}{Q \cdot r_{jk}}$$

$S(Q)$: fonction de structure de diffusion statique totale

$$S(Q) - 1 = \rho_0 \int_0^\infty \sum_{j \neq k} \frac{f_j f_k^*}{(\sum_j f_j)^2} \delta(r - r_{jk}) \frac{\sin(Q \cdot r)}{Q \cdot r} 4\pi r^2 dr$$

$$S(Q) - 1 = \int_0^\infty 4\pi r \rho_0 \sum_{j \neq k} \frac{f_j f_k^*}{(\sum_j f_j)^2} \delta(r - r_{jk}) \frac{\sin(Q \cdot r)}{Q} dr$$

$$S(Q) - 1 = \int_0^\infty 4\pi r \rho_0 (g(r) - 1) \frac{\sin(Q \cdot r)}{Q} dr \quad g(r) = \sum_{j \neq k=1}^N \frac{f_j f_k^*}{(\sum_j f_j)^2}$$

$g(r)$: fonction de distribution de paires

$$S(Q) - 1 = \int_0^\infty G(r) \frac{\sin(Q \cdot r)}{Q} dr \quad G(r) = 4\pi r \rho_0 (g(r) - 1) = 4\pi r (\rho(r) - \rho_0)$$

$\rho(r) = \rho_0 \cdot g(r)$: densité de paires
 ρ_0 : densité numérique

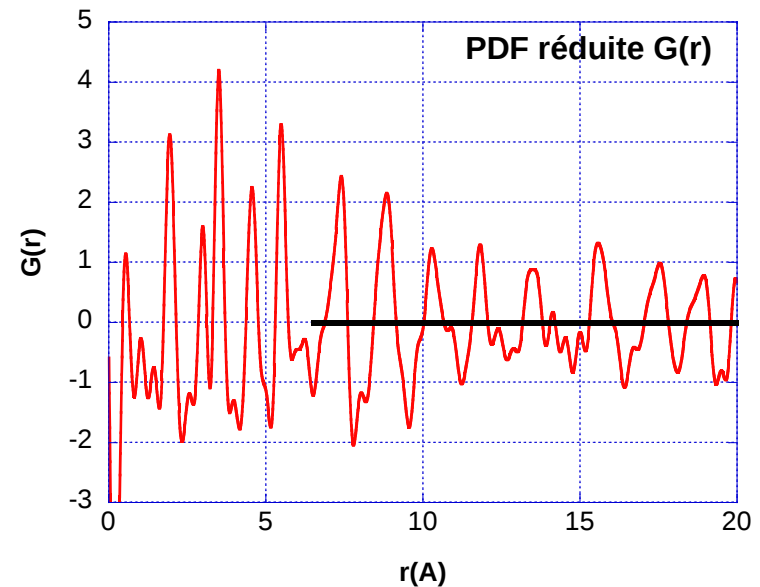
$$G(r) = \frac{1}{r} \sum_{j \neq k=1}^N \frac{f_j f_k^*}{(\sum_j f_j)^2} \cdot \delta(r - r_{jk}) - 4\pi \rho_0$$

$G(r)$: fonction de distribution de paires réduite

$$G(r) = 4\pi r (\rho(r) - \rho_0) = \frac{2}{\pi} \int_0^\infty Q \cdot (S(Q) - 1) \cdot \sin(Qr) \cdot dQ$$

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ,$$

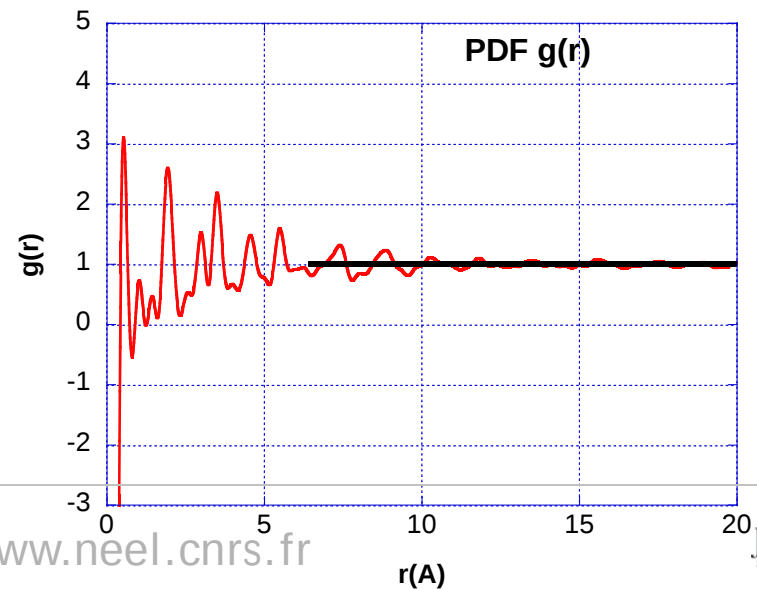
G(r) : fonction de distribution de paires réduite = $TF \{F(Q)=Q.[S(Q)-1]\}$
 $\rightarrow 0$ qd $r \rightarrow \infty$; amplitude indépdt de r , e.s.d.constant avec r



$$G(r) = 4\pi r \rho_0 (g(r) - 1) \quad g(r) = 1 + G(r)/4\pi r \rho_0$$

$g(r)$: fonction de distribution de paires = $TF \{S(Q)\}$

$\rightarrow 1$ qd $r \rightarrow \infty$; amplifie bas r , e.s.d.croît avec r

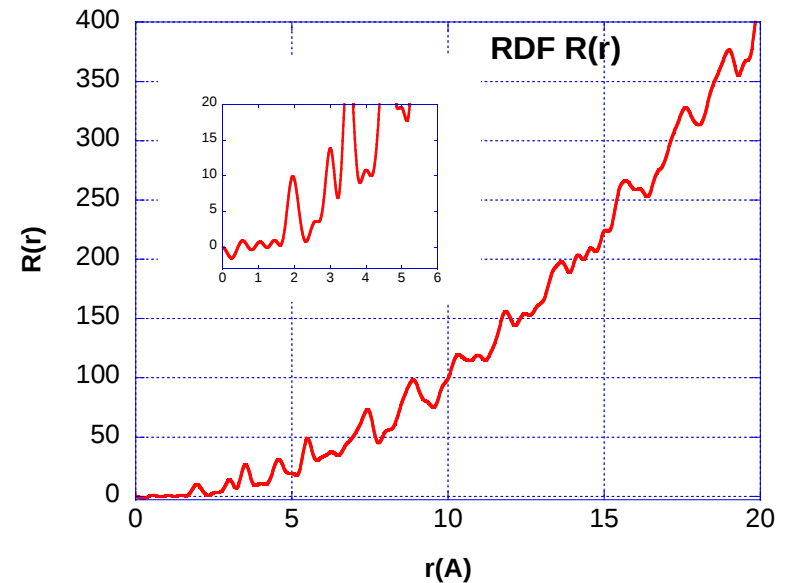


$$R(r) = 4\pi r^2 \rho_0 g(r)$$

R(r) : fonction de distribution radiale

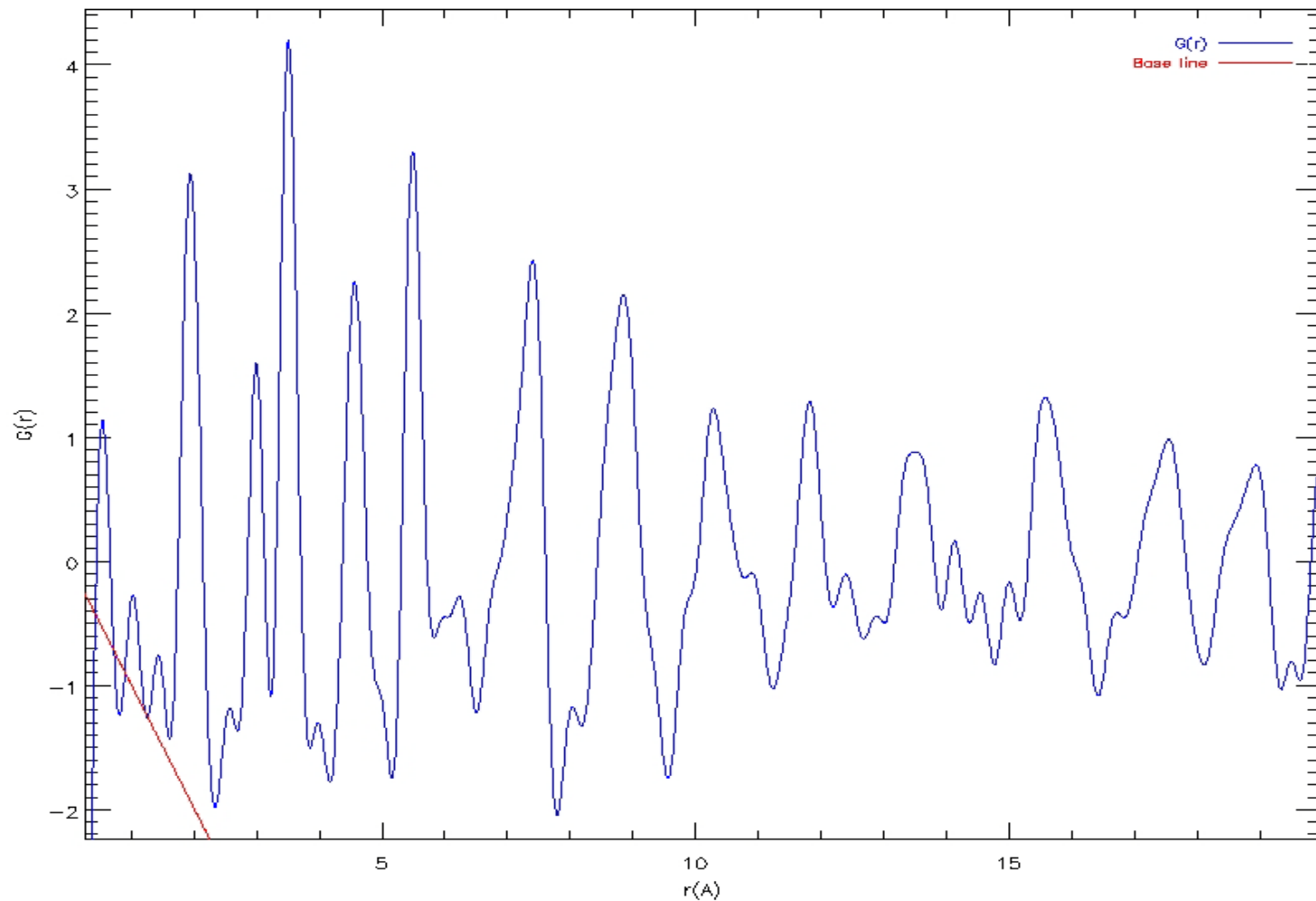
Croît comme r^2

$$Nc = \int_{r1}^{r2} R(r) dr$$



$$G(r) = 4\pi r(\rho(r) - \rho_0) = \frac{2}{\pi} \int_0^\infty Q \cdot (S(Q) - 1) \cdot \sin(Qr) \cdot dQ$$

$$G(r) = \frac{1}{r} \sum_{j \neq k} \frac{f_j f_k^*}{(\sum_j f_j)^2} \cdot \delta(r - r_{jk}) - 4\pi\rho_0 \quad (\text{unité: } \text{\AA}^{-2})$$



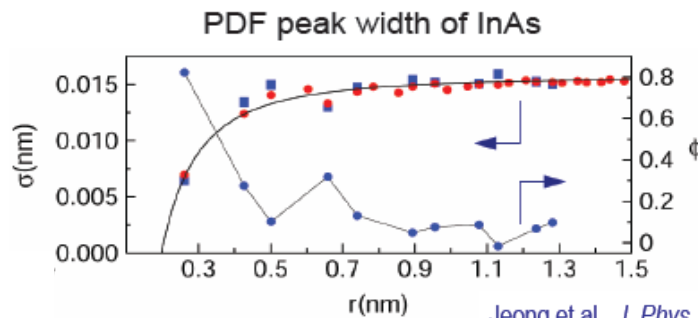
Largeurs des pics de la PDF

Reflètent la distribution des distances interatomiques dans le matériau
 ≠ diffraction !!

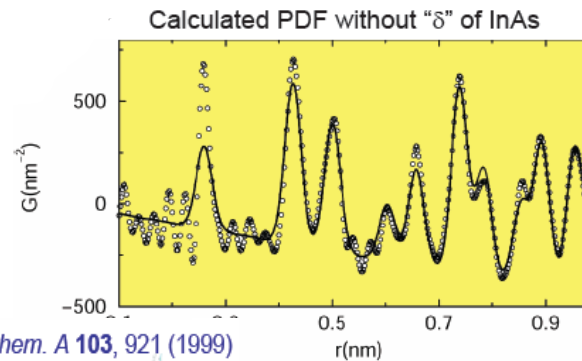
+ **corrections** :

$$\sigma_{ij} = \sigma'_{ij} \sqrt{1 - \frac{\delta_1}{r_{ij}} - \frac{\delta_2}{r_{ij}^2} + Q_{broad}^2 r_{ij}^2}$$

δ_1, δ_2 effets de corrélations de déplacements (HT, BT)



Jeong et al., *J. Phys. Chem. A* **103**, 921 (1999)



Q_{broad} : élargissement dû à la résolution en Q

Q_{damp} : diminution gaussienne de la hauteur

des pics de la PDF due à la résolution en Q (FWHM)

$$B(r) = e^{-\frac{(rQ_{damp})^2}{2}}$$

Debye-Waller : Déplacement relatif ≠ DW cristallographique

Comparer les 2 informe sur les corrélations de déplacement

$$\underbrace{\sigma^2_{ab}}_{PDF} = \underbrace{\sigma^2_a}_{Diffrac.} + \sigma^2_b - 2\sigma^2_a\sigma^2_b.\rho$$

$\rho = +1$ → corrélation positive
 $\rho = 0$ → non corrélé
 $\rho < 0$ → anti-corrélé

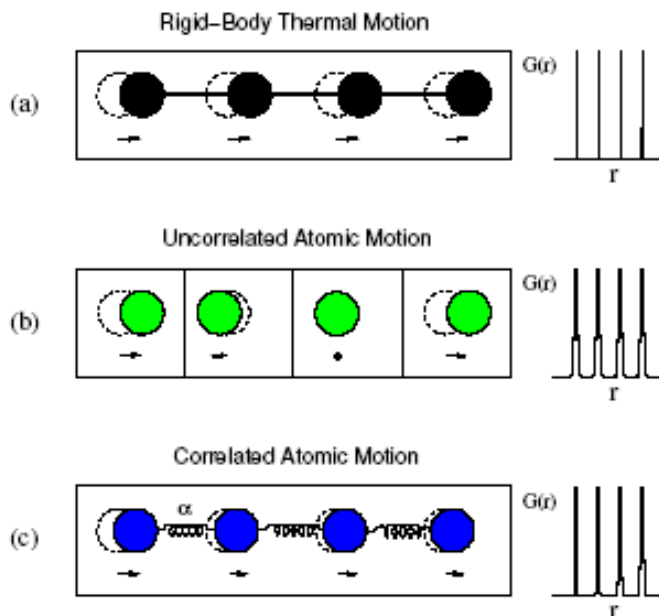
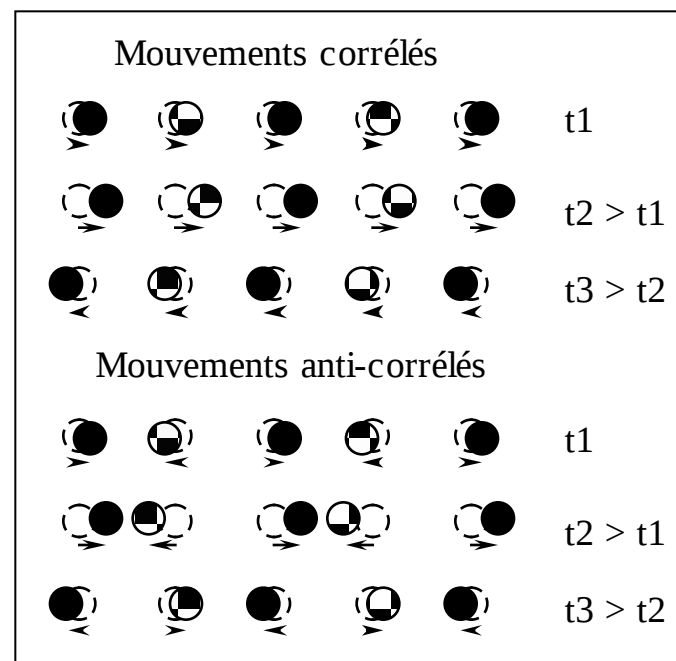


FIG. 1: Schematic diagram showing an instantaneous snapshot of atomic positions in (a) rigid-body model (b) Einstein model (c) Debye model. In (a) and (b) all PDF peaks have the same width independent of atom separation. In (c) the PDF peak width increases up to the root mean-square displacement as the atomic separation increases. α is a spring constant.



A quoi ça peut bien servir ???

Utilisation de la pdf dans l'étude de composés partiellement ordonné et de poudres nanocristallines

Experimentalement, à partir d'un diffractogramme de poudres:

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ$$

r = distance interatomique

$\rho(r)$ = densité de paires, ρ_0 : densité numérique moyenne

$S(Q)$ = intensité diffusée cohérente normalisée,

$Q = 4\pi \sin(\theta)/\lambda$

A partir d'un modèle de structure:

$$G_{calc}(r) = \frac{1}{r} \sum_i \sum_j \left[\frac{b_i b_j}{\langle b \rangle^2} \delta(r - r_{ij}) \right] - 4\pi r \rho_0,$$

r_{ij} = distance interatomique

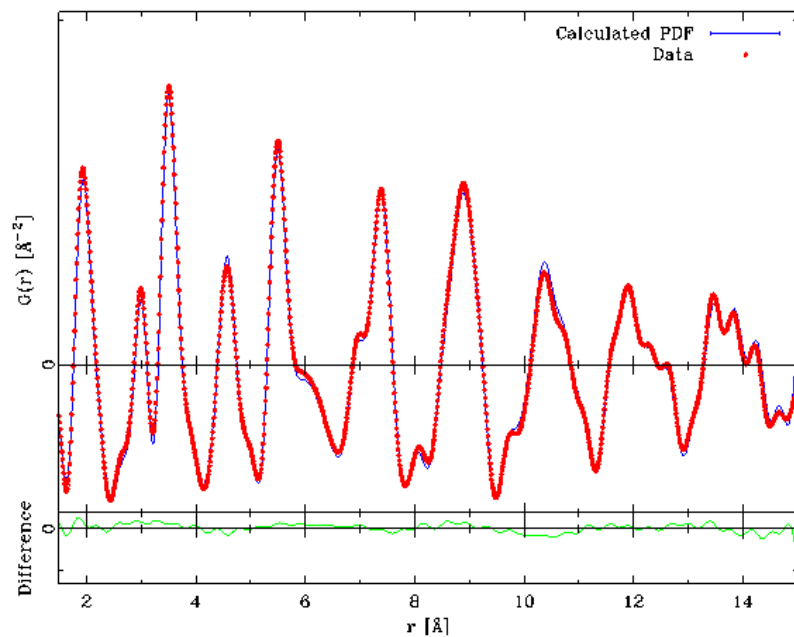
b_i : pouvoir diffusant

=> « **Rietveld** » dans l'espace direct (PDFFIT Proffen et al., Appl. Cryst., 1999)

=> **RMC sur PDF** (DISCUS, Proffen et al., Appl. Cryst., 1997)

ou **S(Q)** (RMCPow, Møllergaard et al., Acta Cryst. A 1999)

ou les deux (RMCProfile, Keen et al., JPCM 2005)



Proffen, S. J. L. Billinge, T. Egami and D. Louca, Z. Kristallogr. 218 (2003) 132–143

Intérêts de l'analyse pdf :

Complémentaire de l'analyse cristallographique classique:

*independant de Bragg, utilisation de la diffusion cohérente totale
études structurales locales(amorphes, ordre partiel, nano-grains...)*

Exemple :

PDF du C60 (diffraction des neutrons sur poudre).

infos :

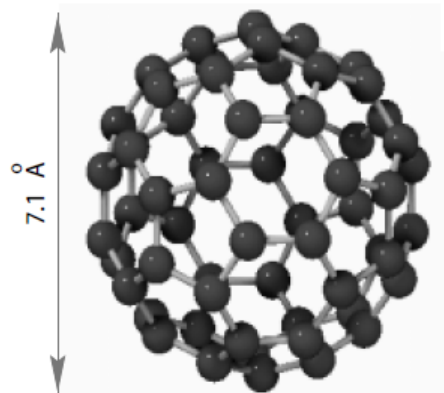
Distances C-C

Diametre des molécules

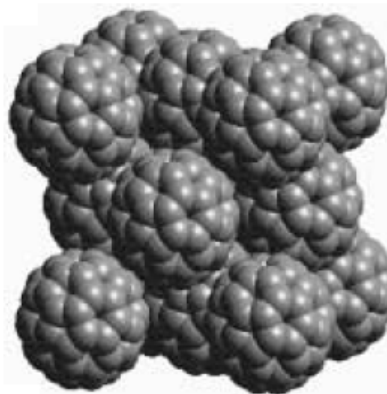
Arrangement cristallin

*Les molécules tournent
incohérentes*

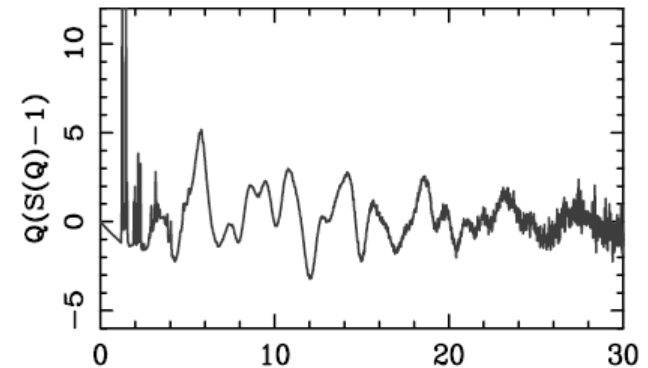
Th. Proffen, S. J. L. Billinge, T. Egami and D. Louca,
Z. Kristallogr. 218 (2003) 132–143



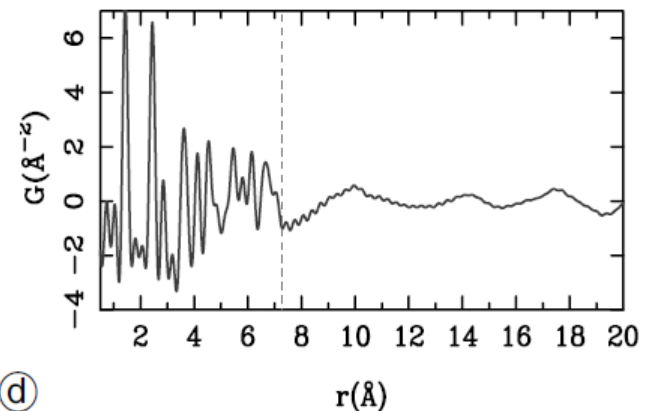
(a)



(b)



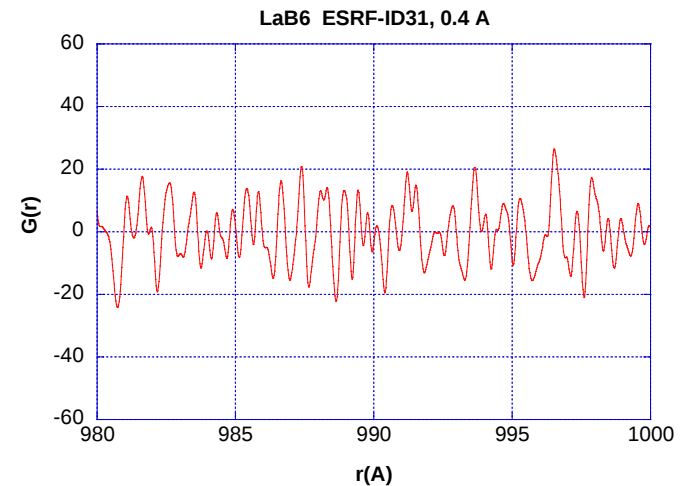
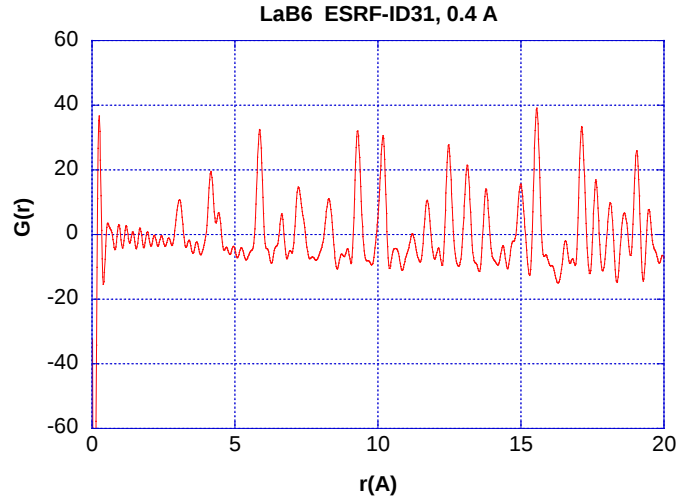
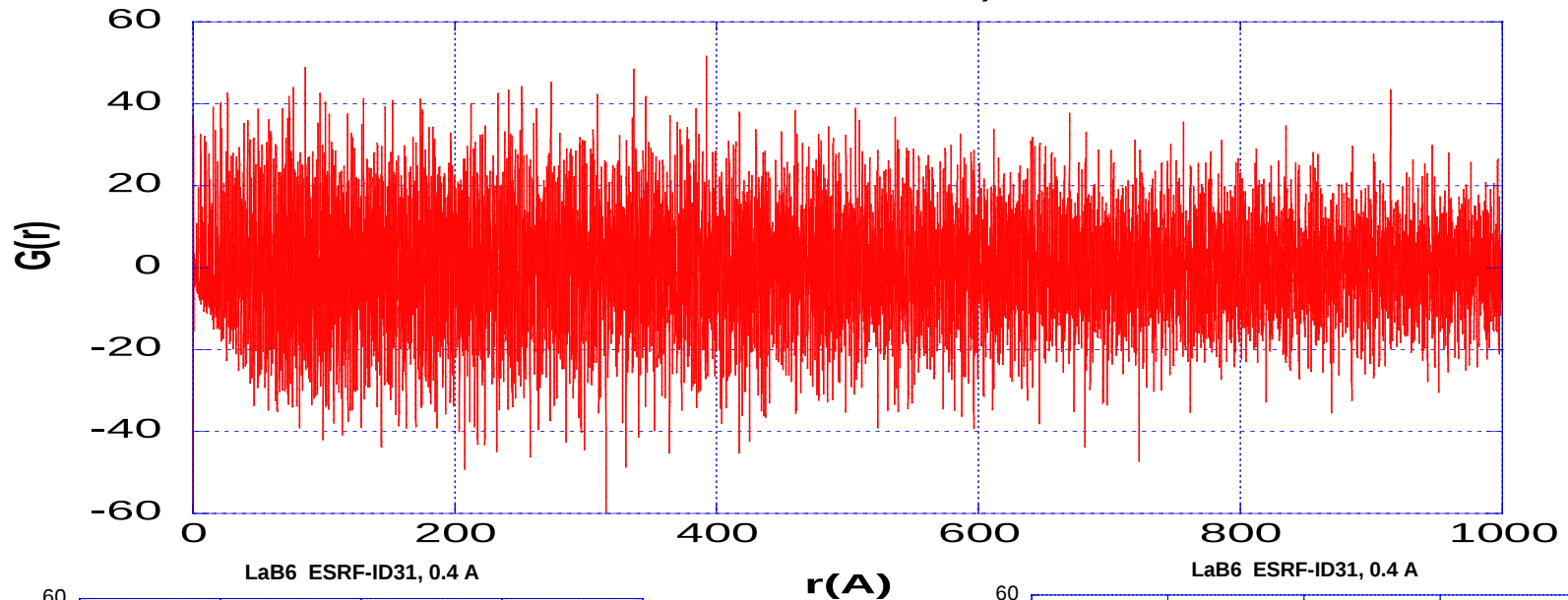
(c)



(d)

PDF = analyse structurale *multi-échelle*

LaB6 ESRF-ID31, 0.4 A



Nécessite une très haute résolution spatiale

Etudes structurales de matériaux nano-cristallins



Différentes températures de recuit

=> différents contenus en eau et cristallinité

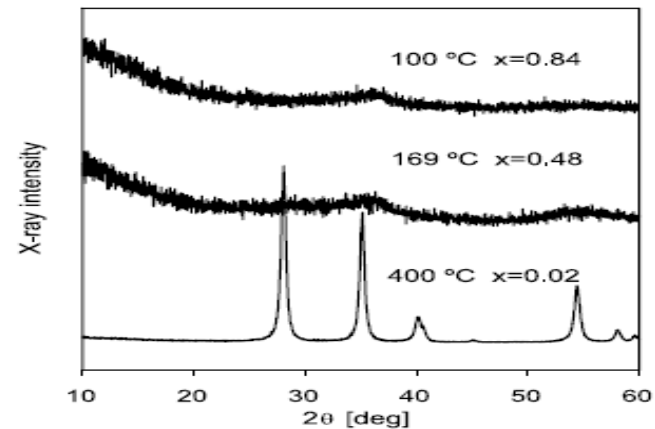
Dérivée de la PDF

=> limite des domaines cohérents

XPD

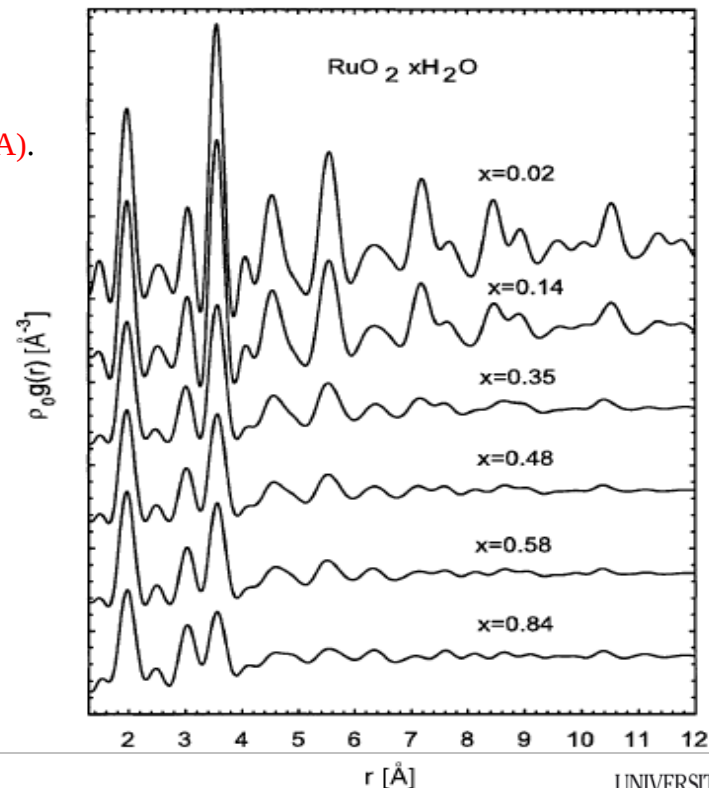
(lab)

CuK α



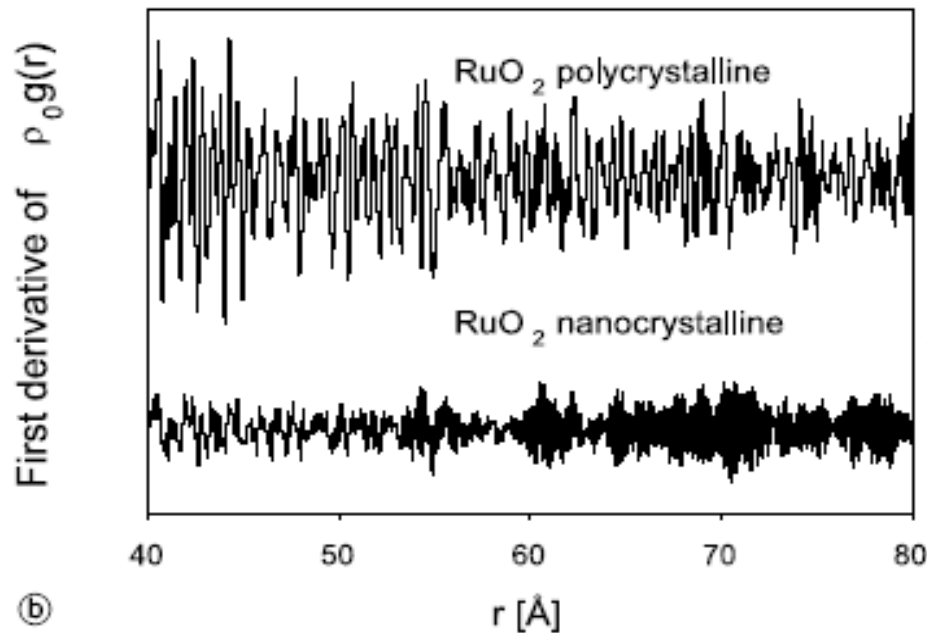
PDF

XPD (X7A).



PDF

Neutron
(Argonne)



W. Dmowski and K. E. Swider-Lyons, Z. Kristallogr. 219 (2004) 136–142

Comment la mesurer ??

C'est (presque) une mesure de diffraction de poudres classique

Mais nécessité de mesures à hauts Q et fortes statistiques

=> **Utilisation des grands instruments**

Neutrons

facteur de diffusion constant (b) => signal à très hauts Q

contraste entre éléments (O, Z voisins, isotopes...)

réacteurs à hauts flux, ex : ILL-D4, $\lambda=0.7, 0.5, 0.35 \text{ \AA}$ => $Q_{\text{max}} \approx 33 \text{ \AA}^{-1}$,

sources à spallation, ex : ISIS-GEM, LANL-NPDF (dédiée), $Q_{\text{max}} > 45 \text{ \AA}^{-1}$

Synchrotrons rayons X

signal décroît avec $f(2\theta)$

très hauts flux jusqu'à très hautes énergies ($\approx 100 \text{ keV}$)

faisceau parallèle + crystal analyseur-> élimine les contributions élastiques

détecteurs 2D: expériences in-situ, résolues en temps

Instruments de laboratoire

Diffracto de poudres de labo optimisé pour hauts Q et statistique

$\lambda\text{MoK}\alpha$ (0.71Å) $\Rightarrow Q_{\text{max}} \approx 17\text{\AA}^{-1}$

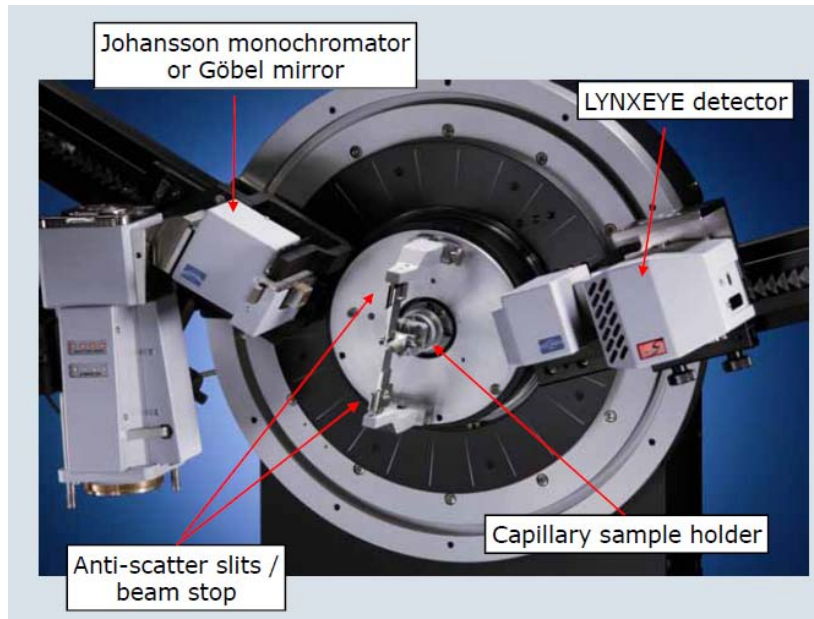
$\lambda\text{AgK}\alpha$ (0.56Å) $\Rightarrow Q_{\text{max}} \approx 22\text{\AA}^{-1}$

Monochromatisation modérée

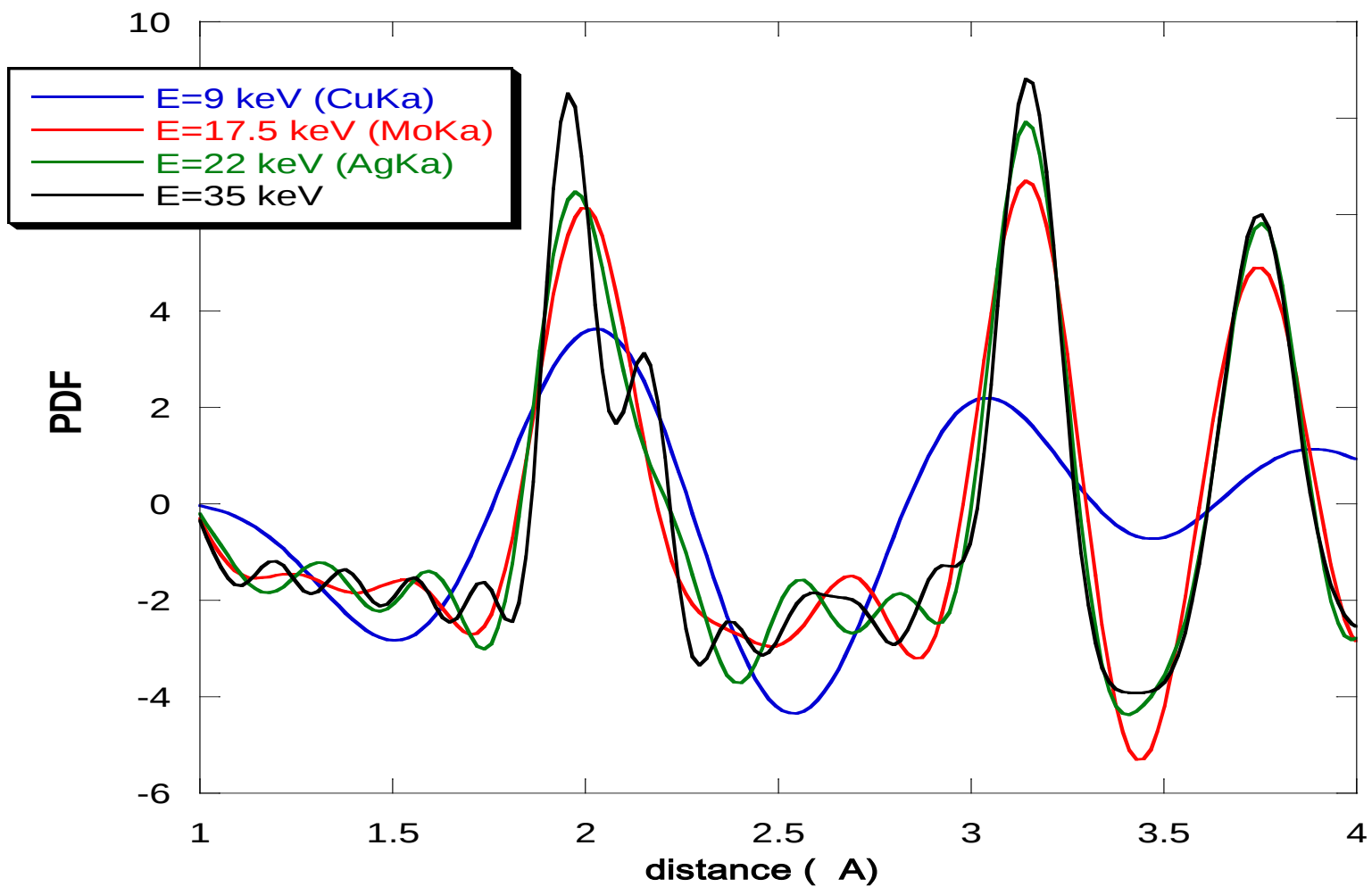
(e.g. filtre - graphite primaire - multicouches)

PSD (*haute énergie !!*)

Debye-Scherrer ou Bragg-Brentano



Effet de Q_{max}



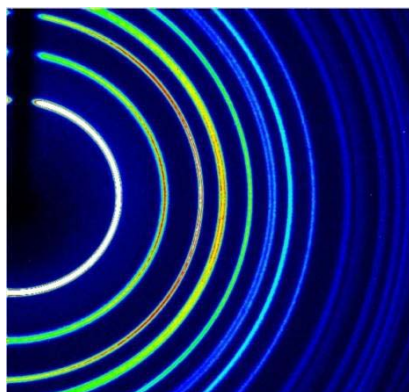
Utilisation d'une camera ApexII et d'une microsource Ag-I μ S pour la mesure de la PDF



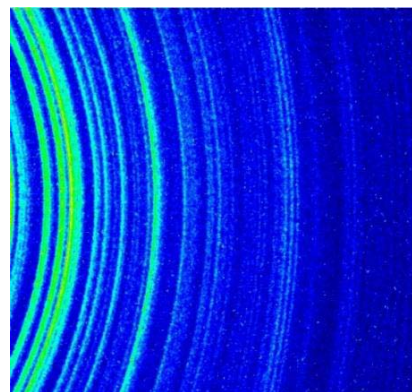
KappaCCD + camera ApexII, *eval*CCD



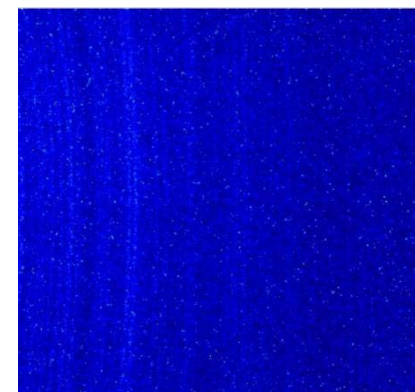
$\theta=0$



$\theta=9$

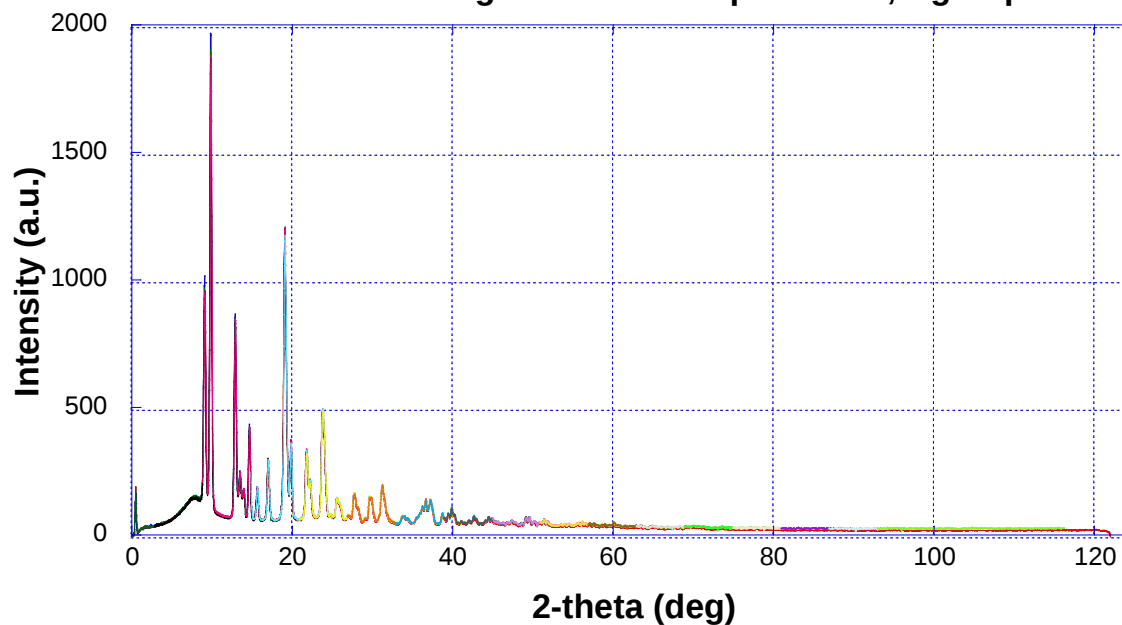


$\theta=25$



$\theta=41$

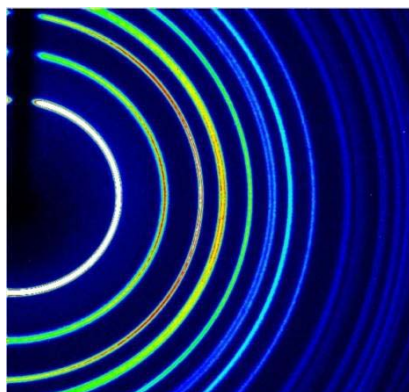
Powder diffractogram from 2D ApexII data, AgKalpha



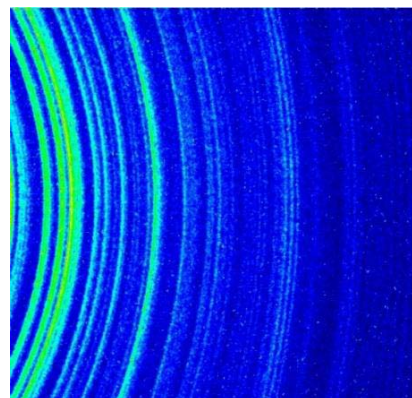
36 images mesurées tous les 3 , 5min/image



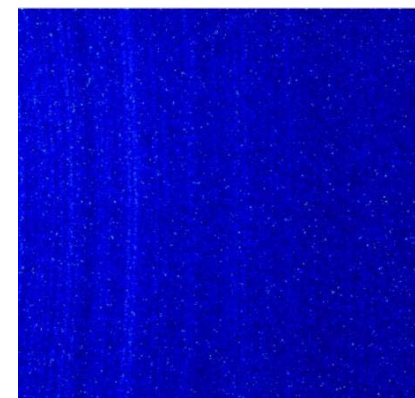
$\theta=0$



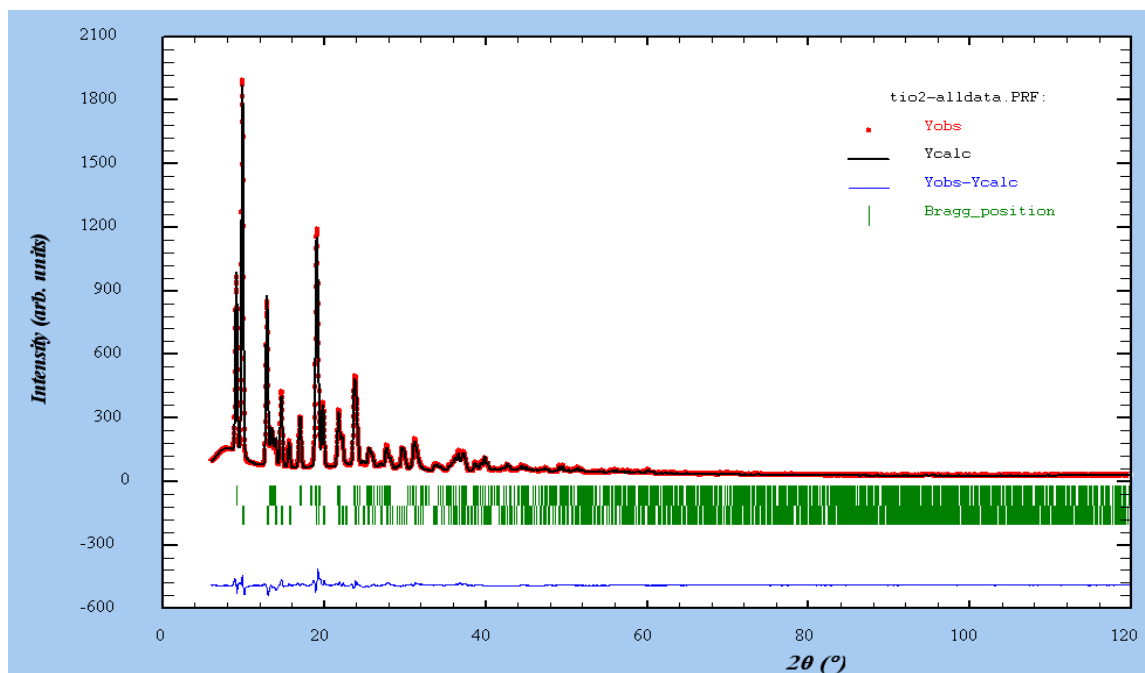
$\theta=9$



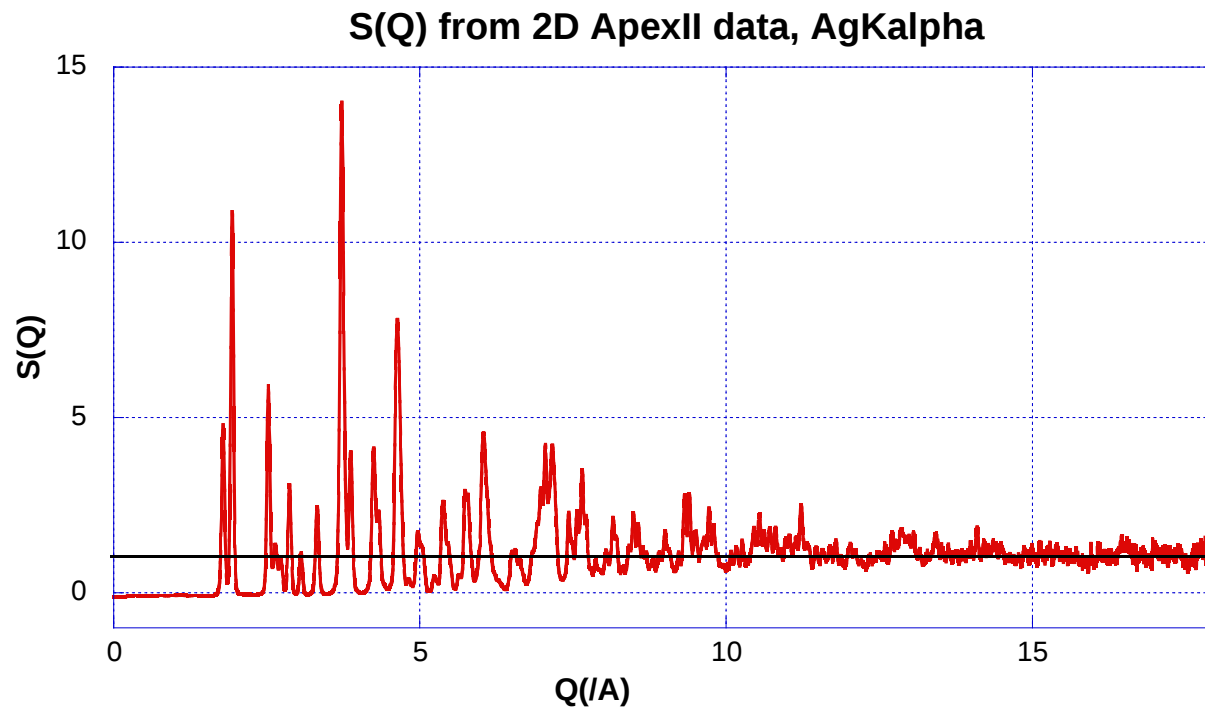
$\theta=25$



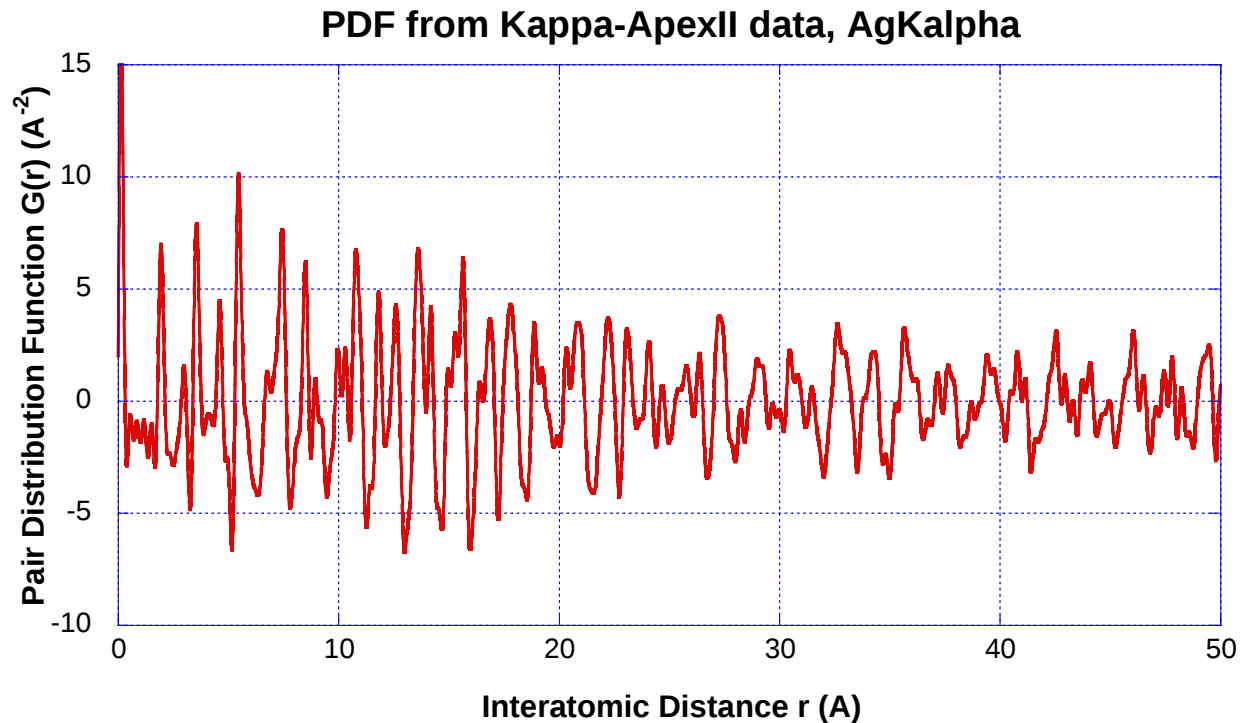
$\theta=41$



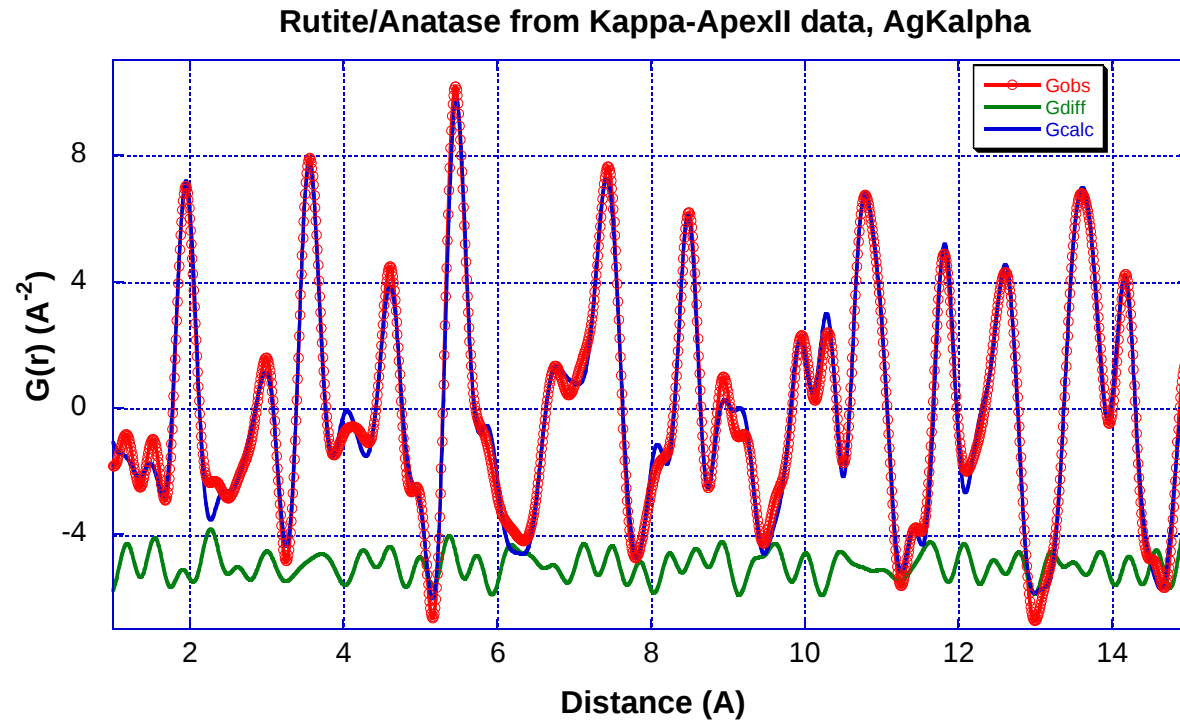
Fit de la PDF, mélange TiO_2 Rutile + Anatase



Fit de la PDF, mélange TiO_2 Rutile + Anatase



Fit de la PDF, mélange TiO_2 Rutile + Anatase



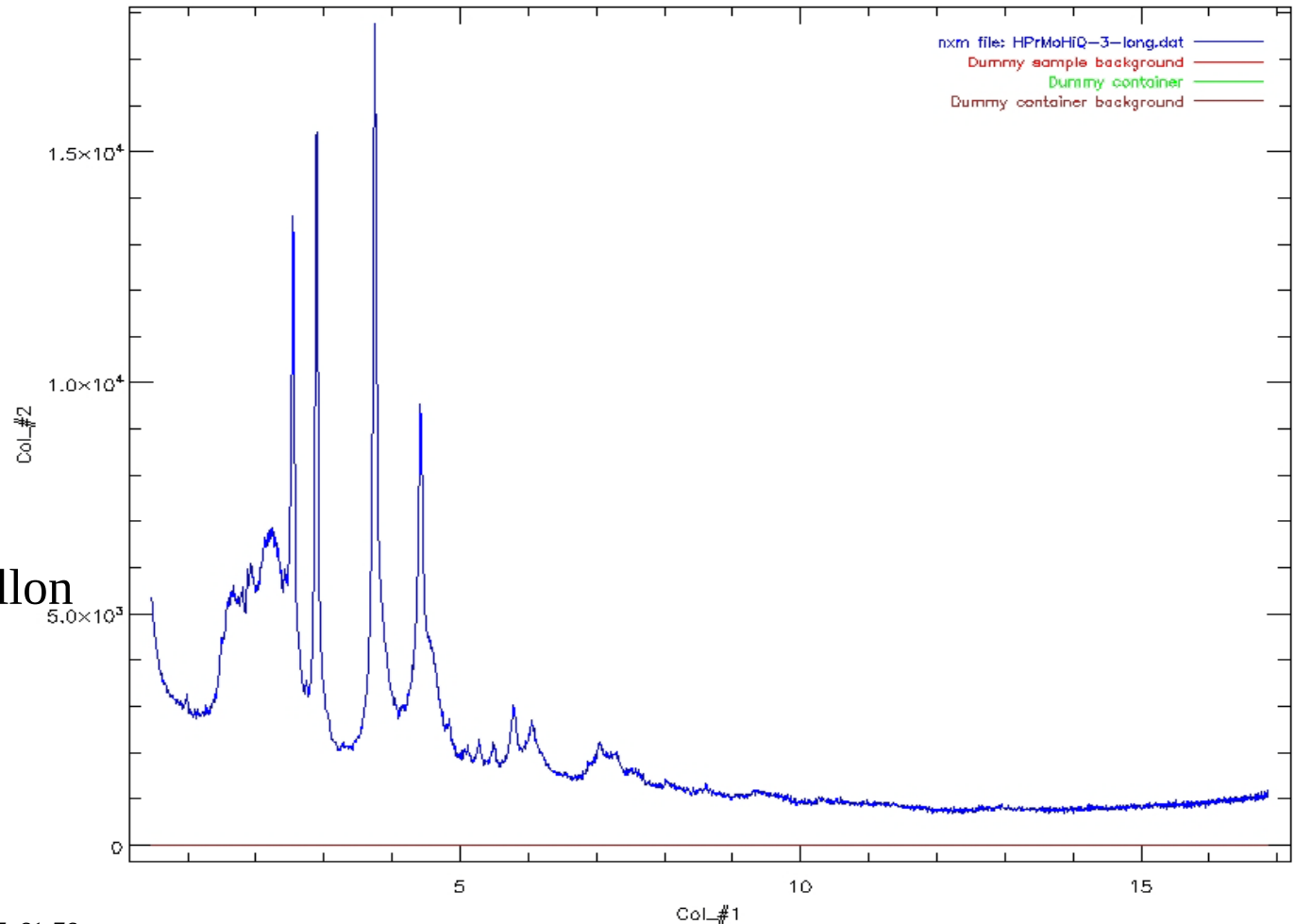
***Comment traiter le diagramme
pour en extraire la PDF ??***

Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ,$$

I(Q)
X'pert
Bragg-Brentano
X'celerator
 $\lambda\text{MoK}\alpha$
Miroir Göbel

Pas de porte échantillon



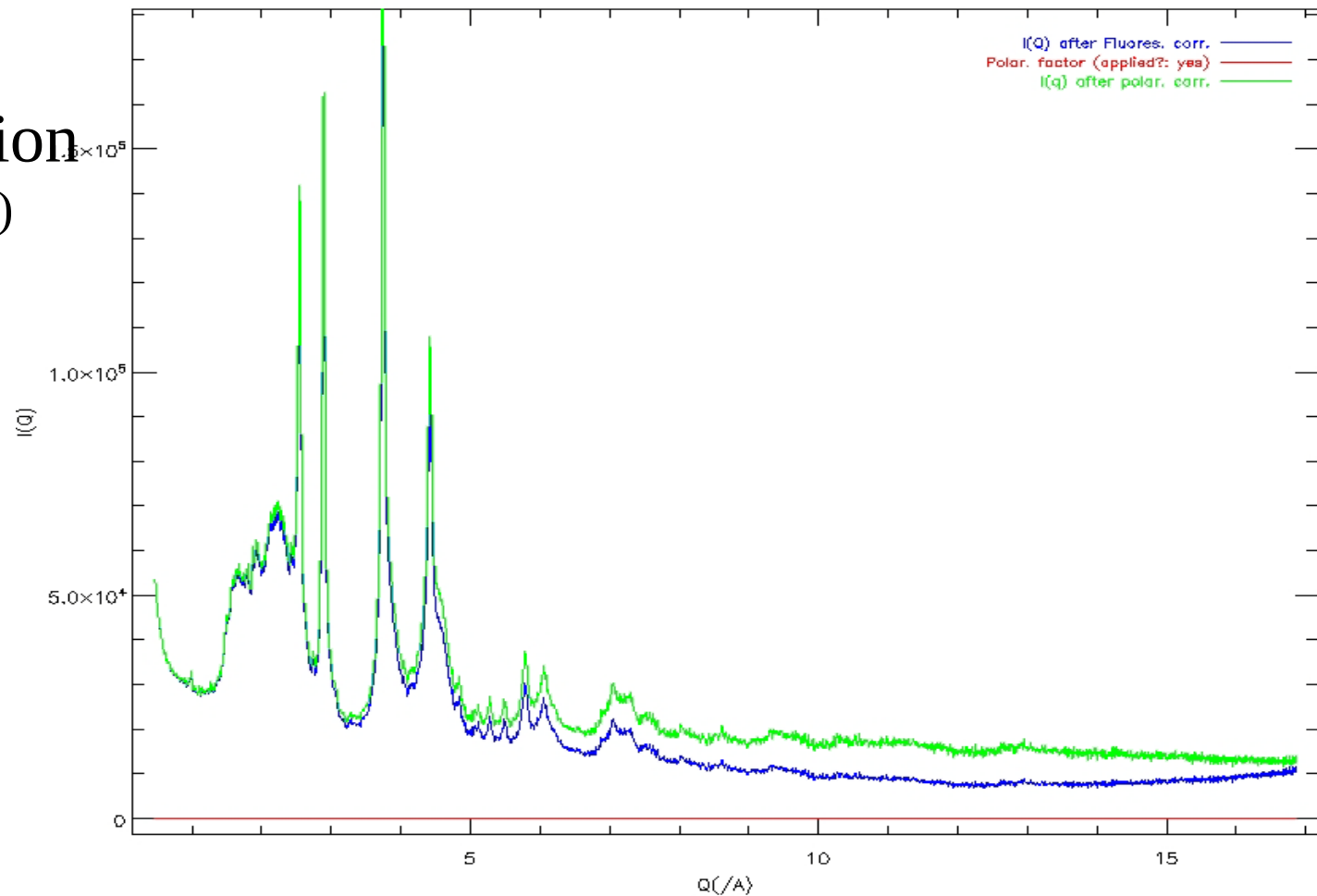
B.J. Thijsse, J. Appl. Cryst. (1984). 17, 61-76

Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$P = (1 + x \cos^2 2\theta) / (1 + y)$$

$x = \cos^2 2\alpha_c$ ou $\cos 2\alpha_c$ Mono. mosaic ou parfait; primaire : $x=y$; diffracté, $y=1$

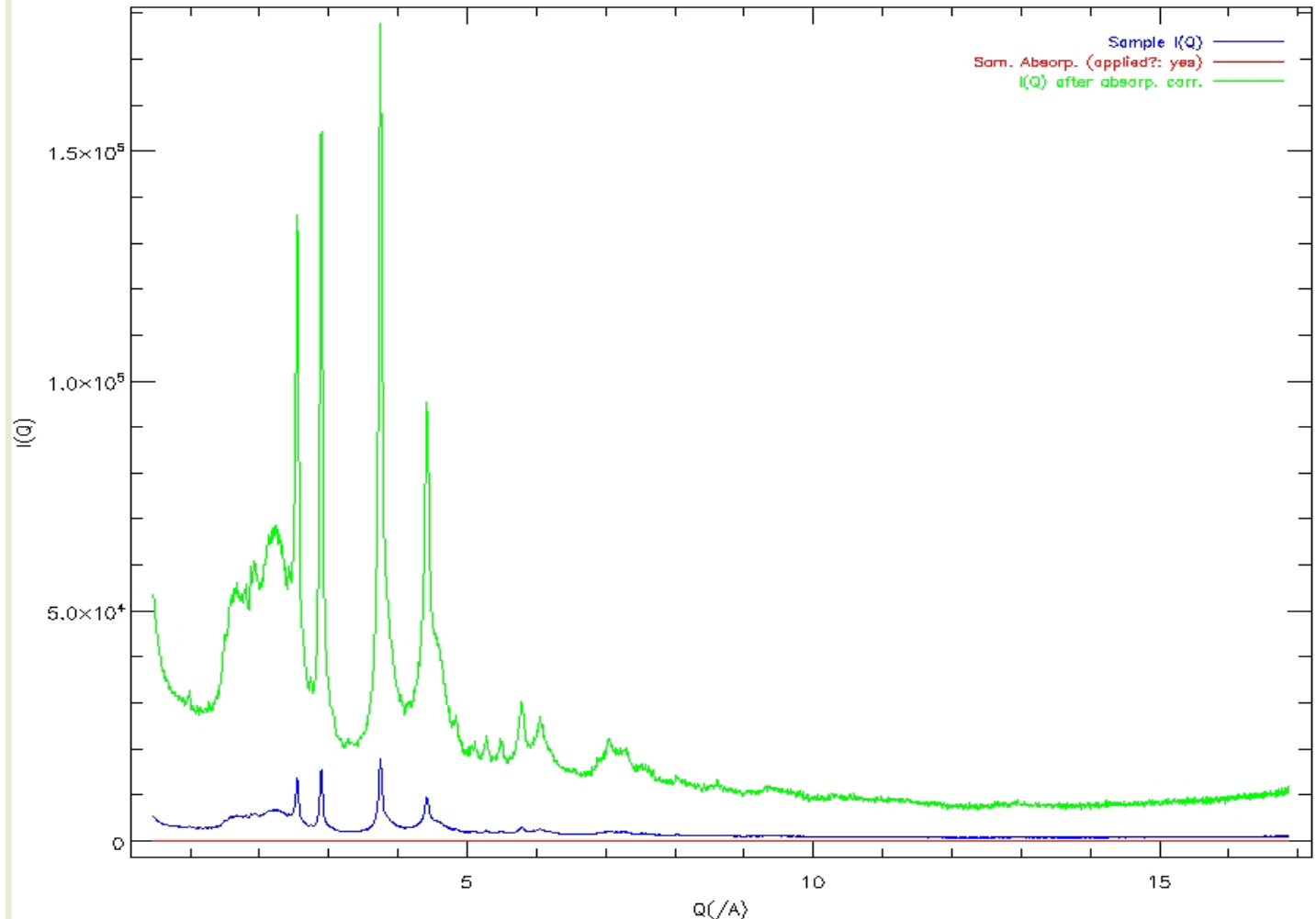
Polarisation
(pas Lorentz)



Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$A_{refl} = [1 - \exp(-2\mu t / \sin \theta)] / 2\mu$$

Absorption



Obtenir la PDF expérimentale (cas des rayons X B.B.)

Compton

$$I_a^{\text{incoh}}(Q) = \left(\frac{\lambda}{\lambda'}\right)^2 \sum_{j=1}^n c_j Z_j \frac{(b_j Q)^{a_j}}{1 + (b_j Q)^{a_j}} \quad (A2)$$

with n the number of atomic species, Z_j the atomic number of species j , and a_j and b_j semi-empirical expressions given by

$$a_j = 2.6917 Z_j^{-1} + 1.2450 \quad (A3)$$

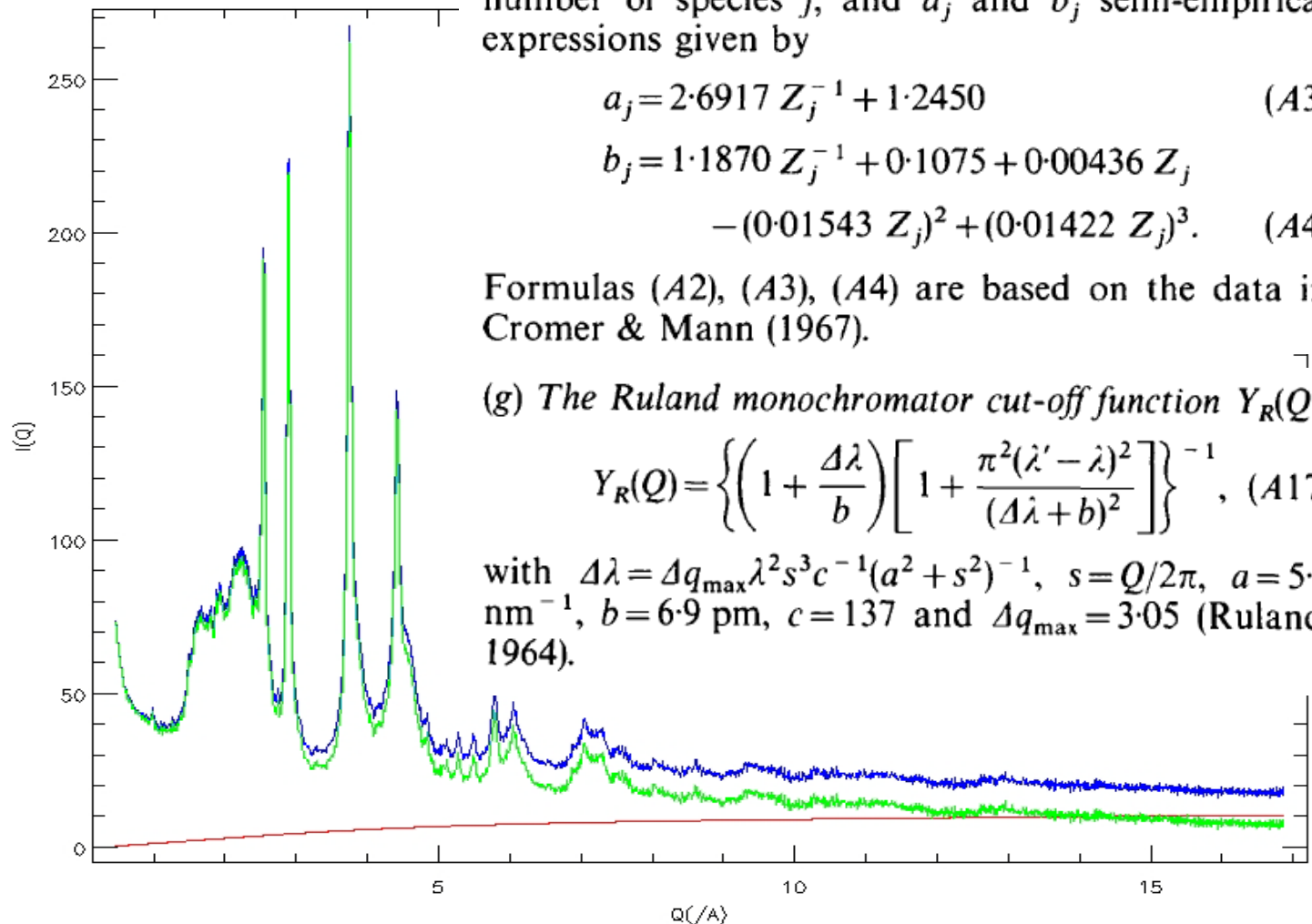
$$b_j = 1.1870 Z_j^{-1} + 0.1075 + 0.00436 Z_j - (0.01543 Z_j)^2 + (0.01422 Z_j)^3. \quad (A4)$$

Formulas (A2), (A3), (A4) are based on the data in Cromer & Mann (1967).

(g) The Ruland monochromator cut-off function $Y_R(Q)$

$$Y_R(Q) = \left\{ \left(1 + \frac{\Delta\lambda}{b} \right) \left[1 + \frac{\pi^2(\lambda' - \lambda)^2}{(\Delta\lambda + b)^2} \right] \right\}^{-1}, \quad (A17)$$

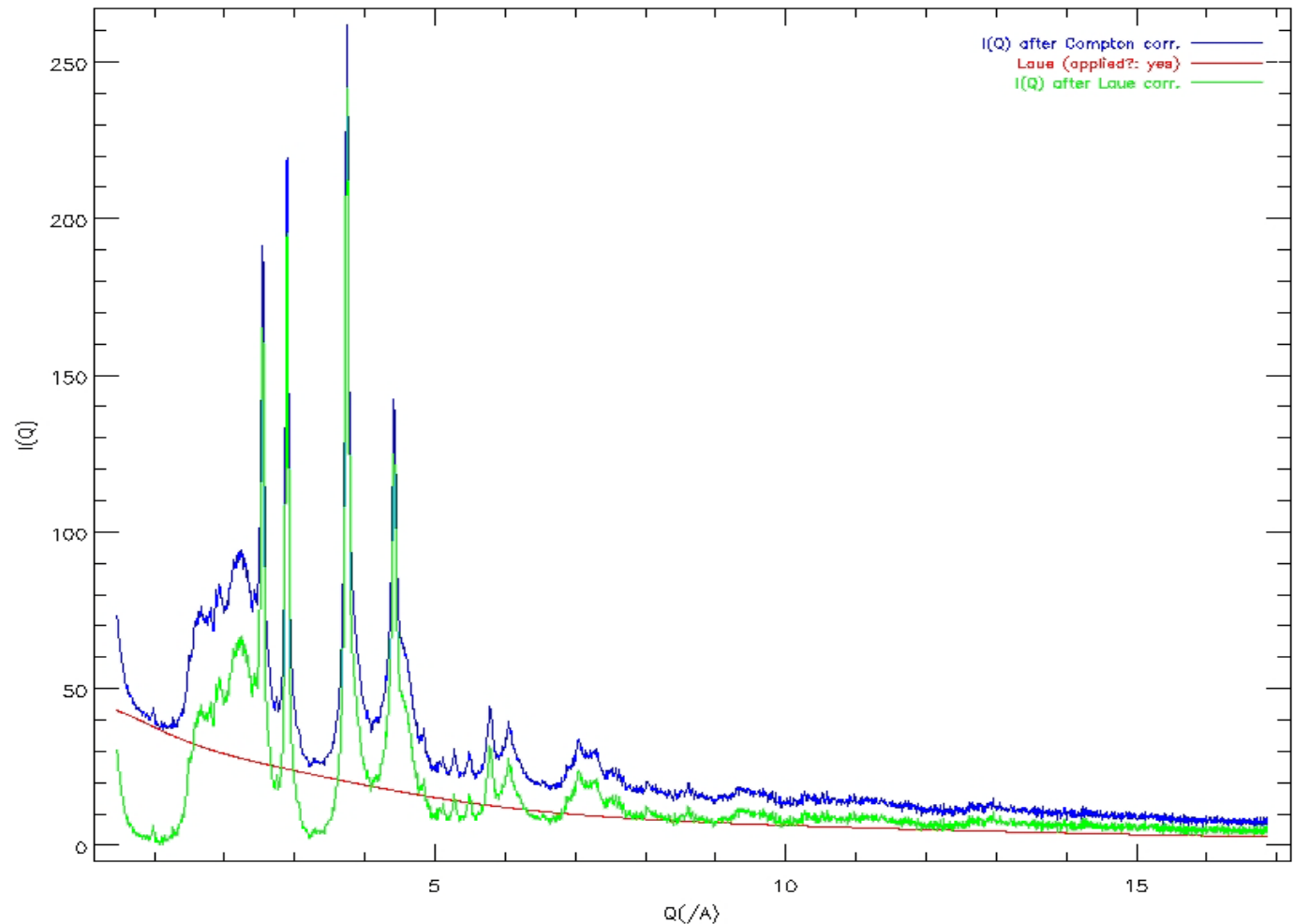
with $\Delta\lambda = \Delta q_{\text{max}} \lambda^2 s^3 c^{-1} (a^2 + s^2)^{-1}$, $s = Q/2\pi$, $a = 5.3 \text{ nm}^{-1}$, $b = 6.9 \text{ pm}$, $c = 137$ and $\Delta q_{\text{max}} = 3.05$ (Ruland, 1964).



Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$S(Q) = [I_{eu}^{coh} - (\langle f^2 \rangle - \langle f \rangle^2)] / \langle f \rangle^2$$

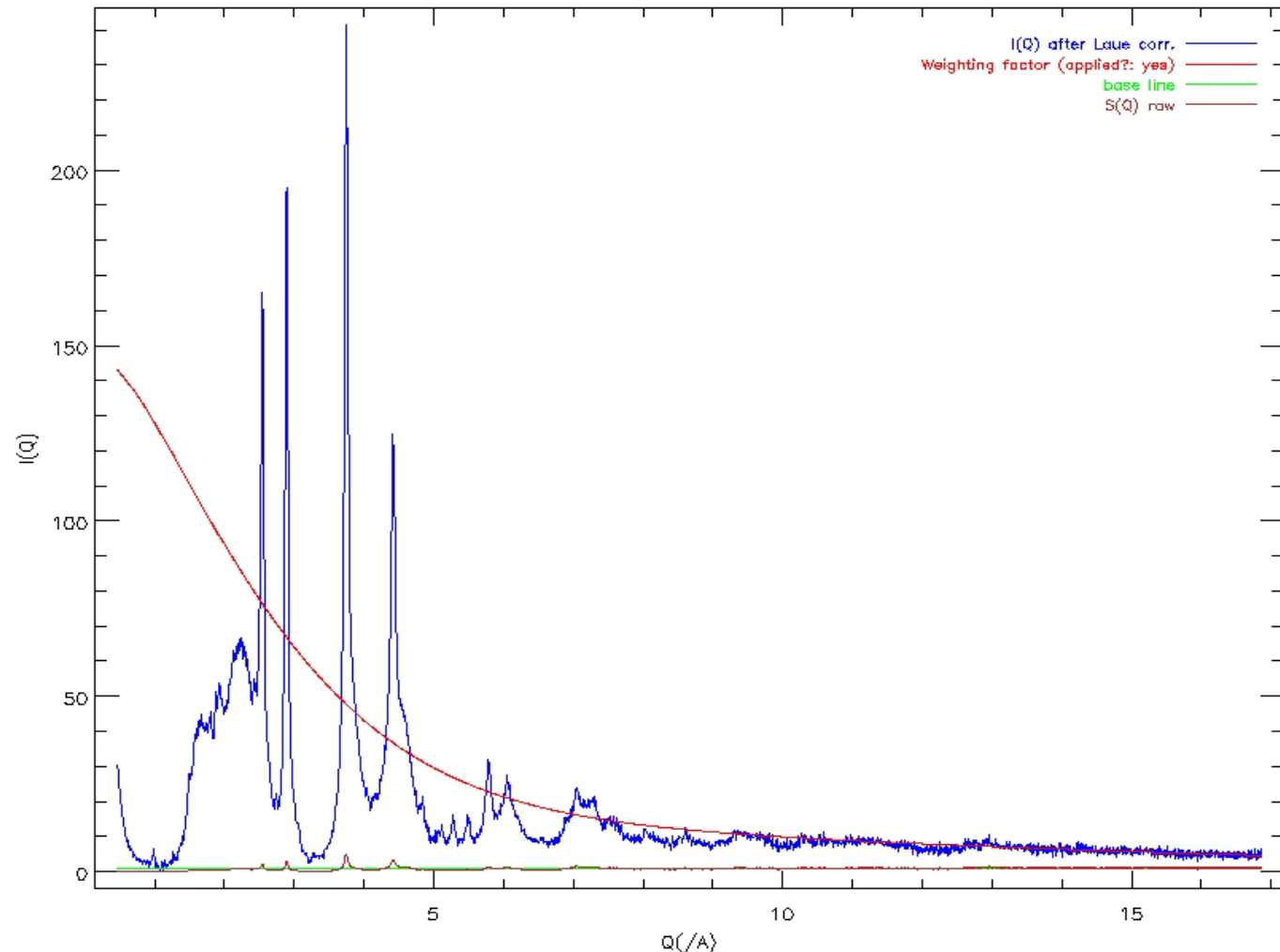
Laue diffuse



Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$S(Q) = [I_{eu}^{coh} - (\langle f^2 \rangle - \langle f \rangle^2)] / \langle f \rangle^2$$

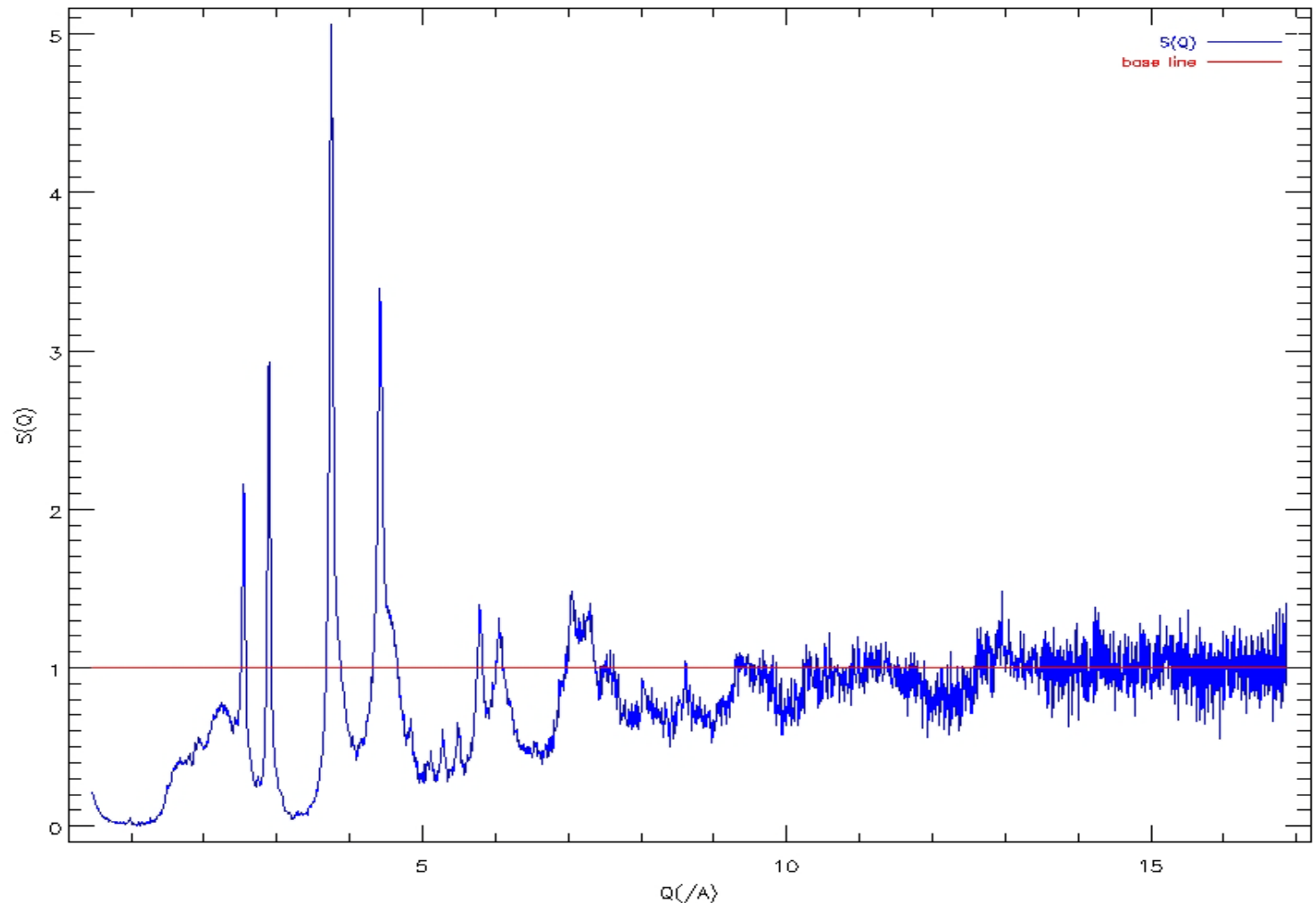
Normalisation
 $\langle f \rangle^2$



Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ,$$

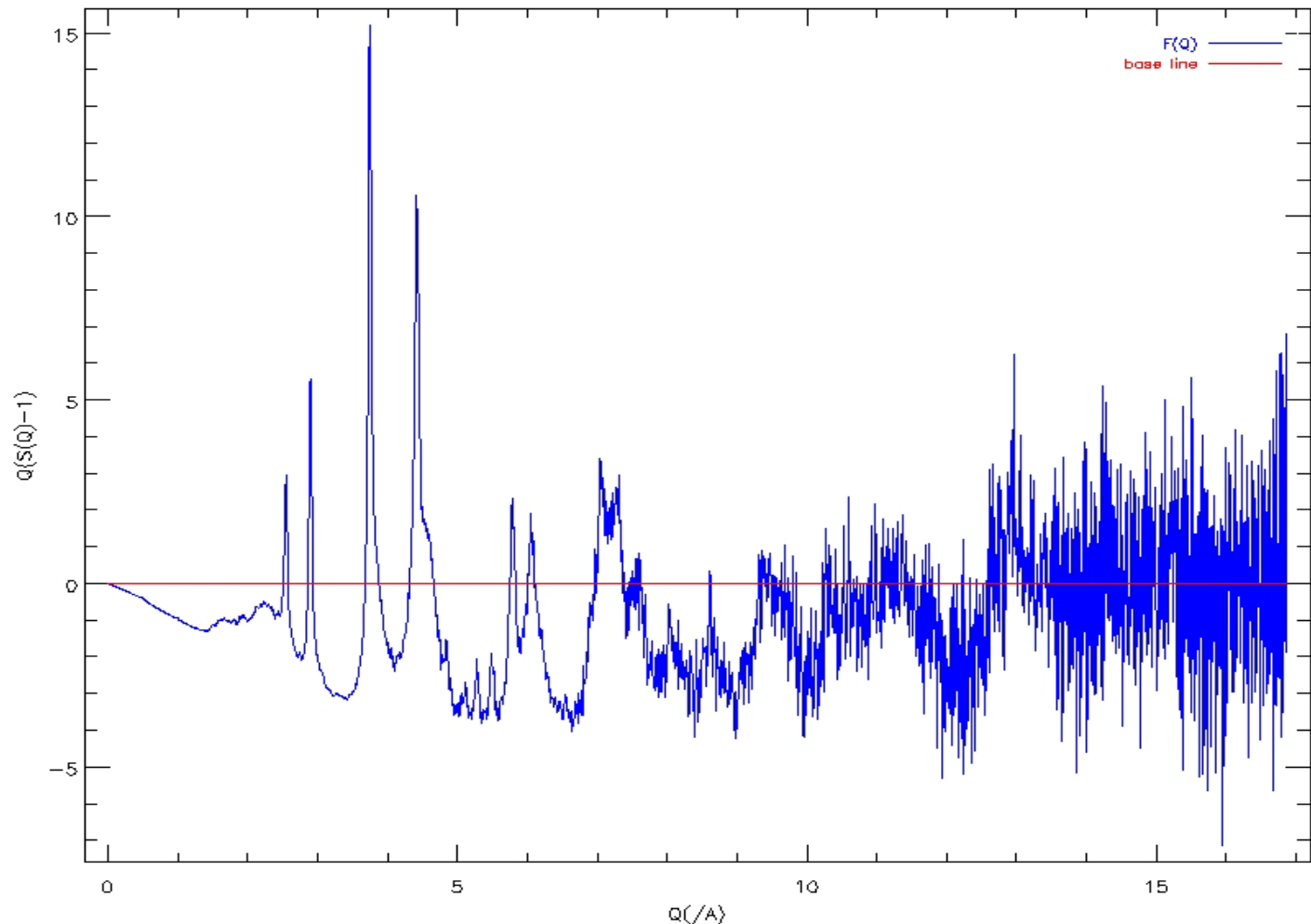
$S(Q)$



Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ,$$

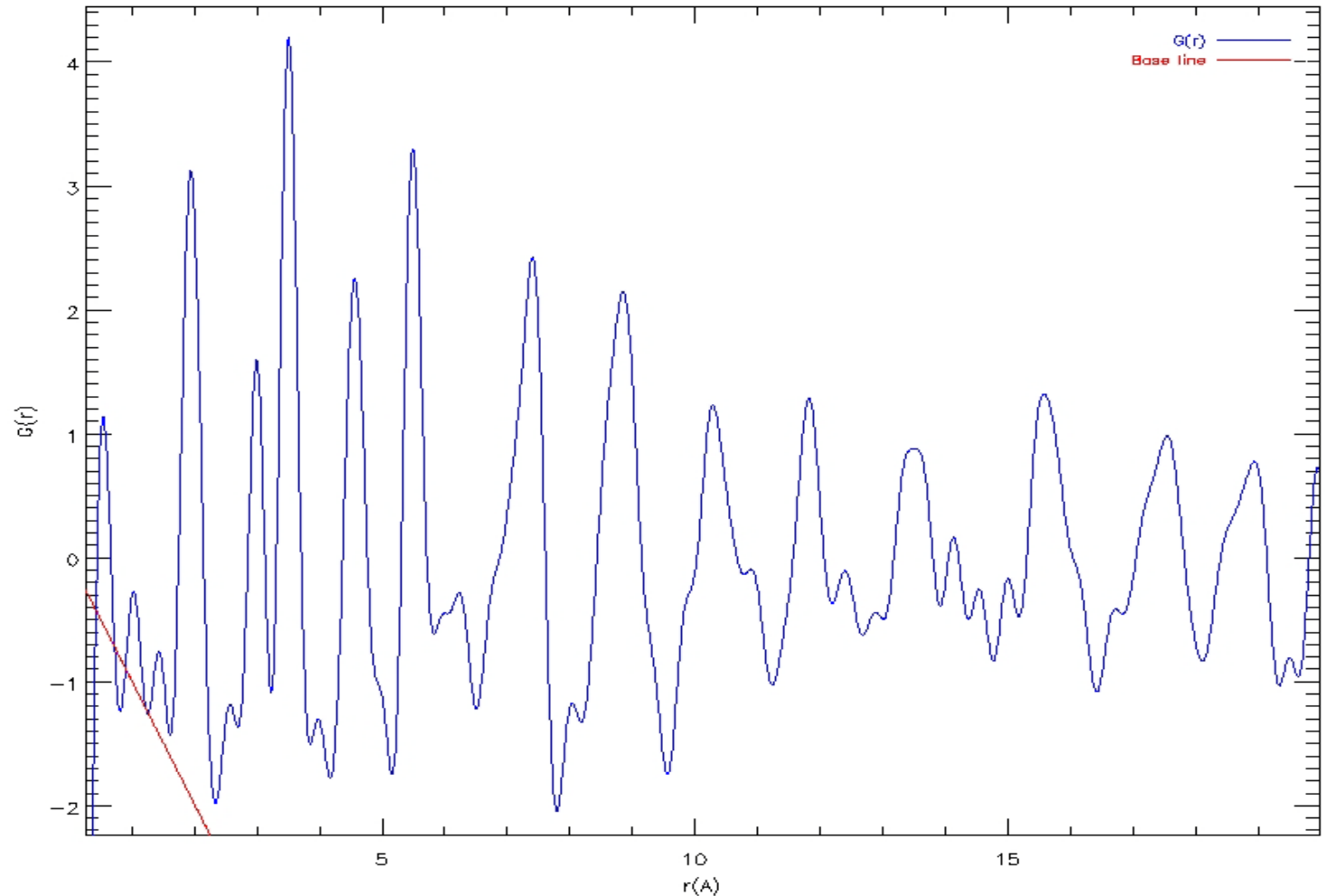
$F(Q)$
 $F(Q) = Q(S(Q) - 1)$

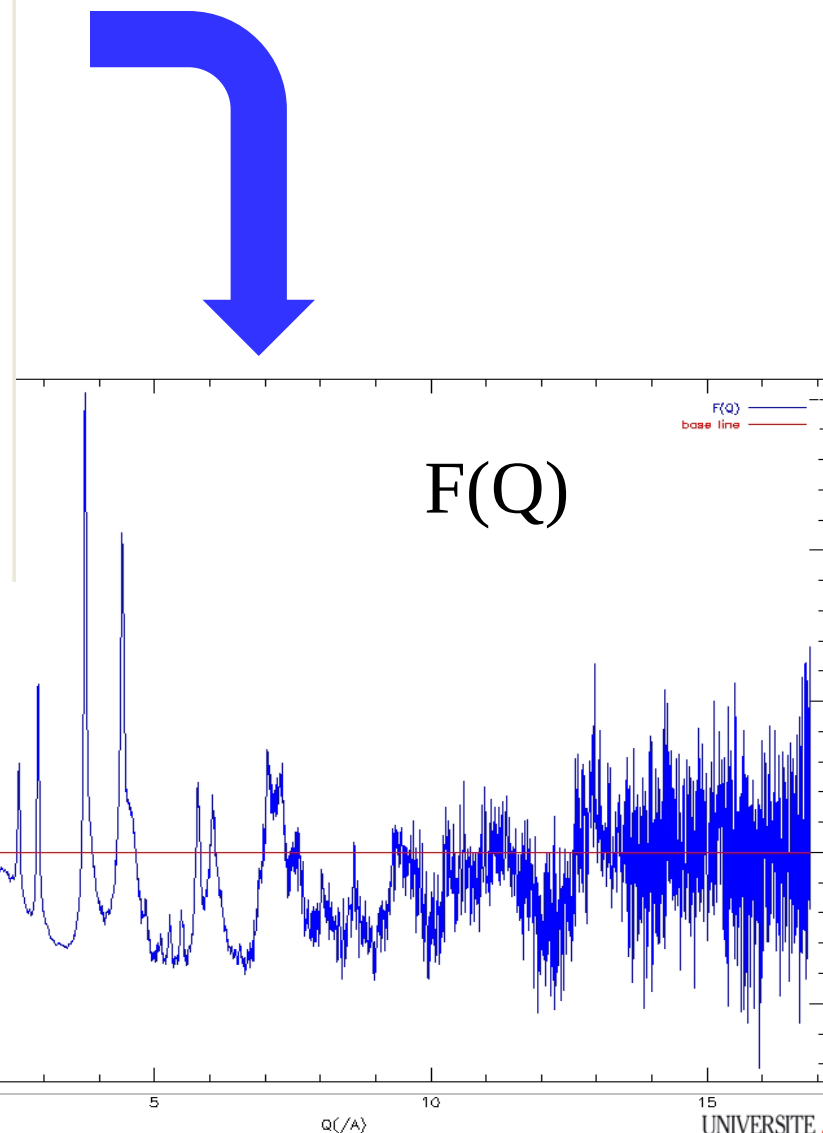
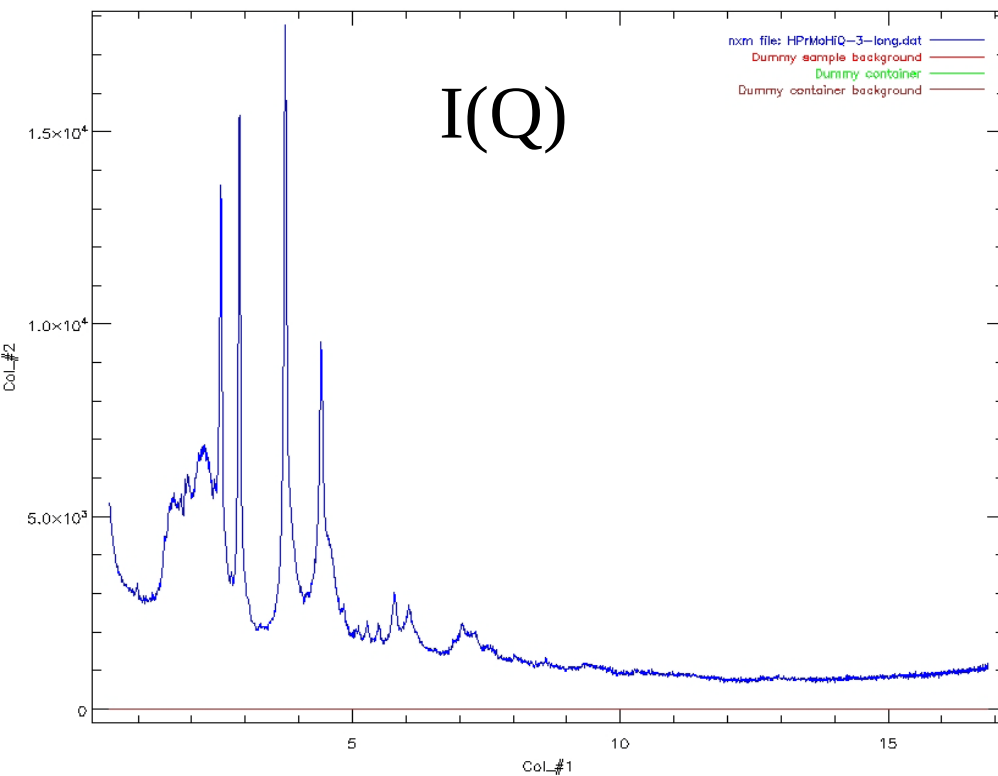


Obtenir la PDF expérimentale (cas des rayons X B.B.)

$$G(r) = 4\pi r[\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^\infty Q[S(Q) - 1] \sin(Qr) dQ,$$

$G(r)$





Mesurer à hauts Q
Fortes statistiques à hauts Q

Exemples

Exemple : hydroxilian pseudo rutile (HPR)

(I.E. Grey, CSIRO, Melbourne)

XRPD :

Cohérence du réseau O

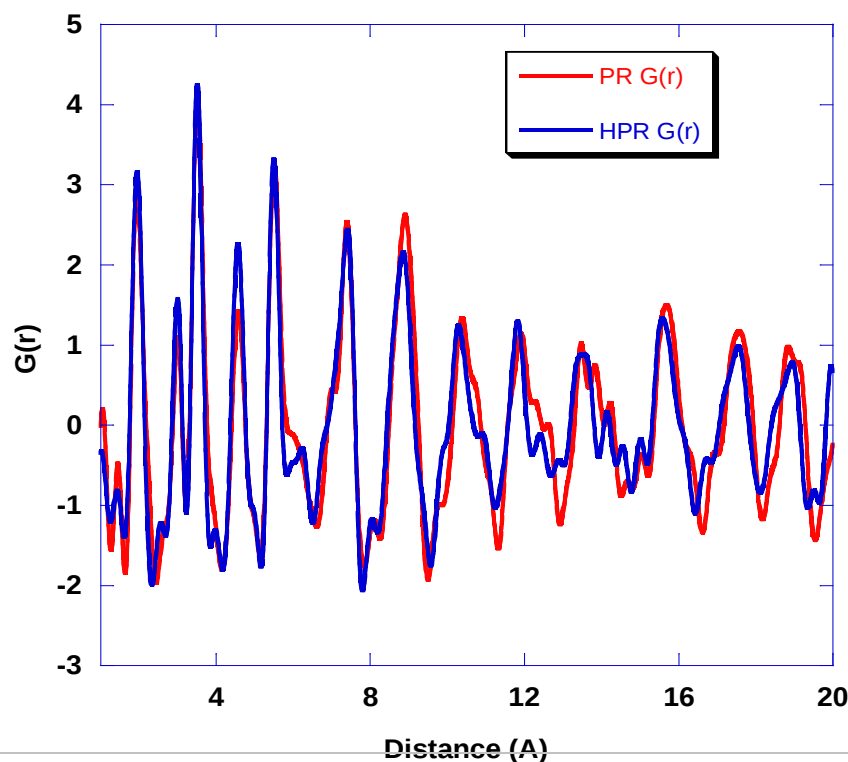
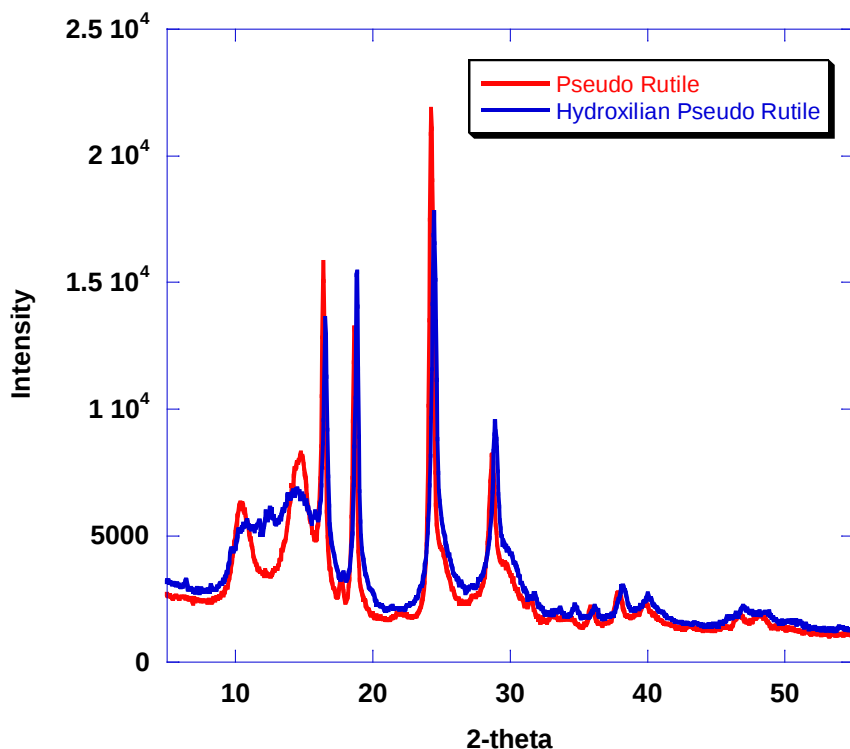
Affinement Rietveld

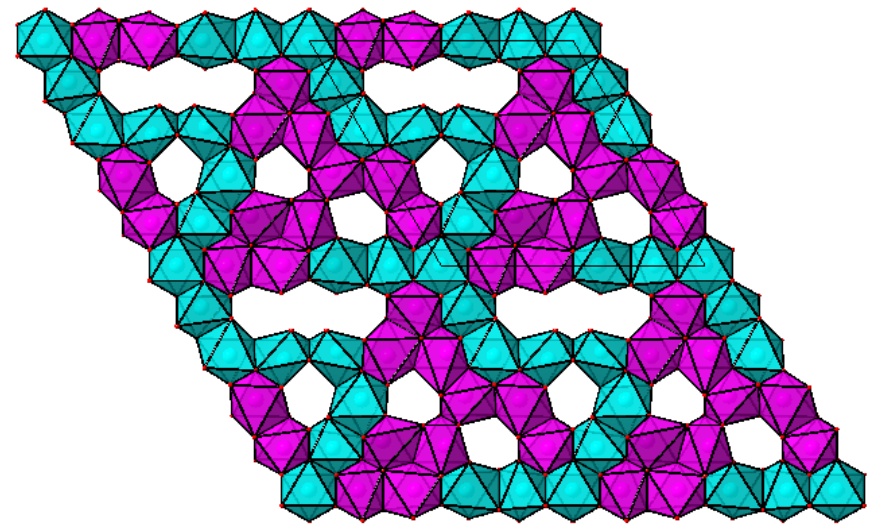
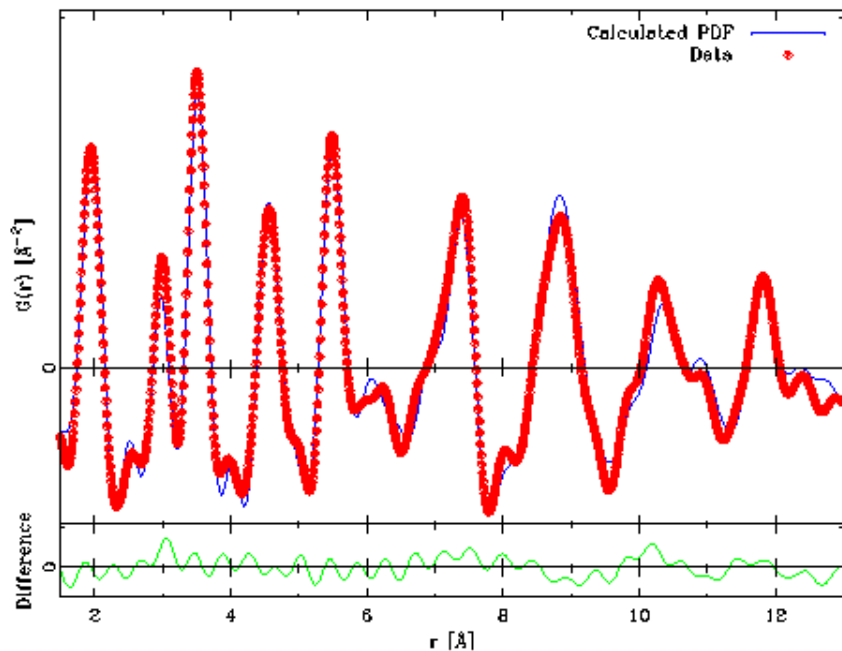
=> Paramètres moyens dans la sous-maille

PDF :

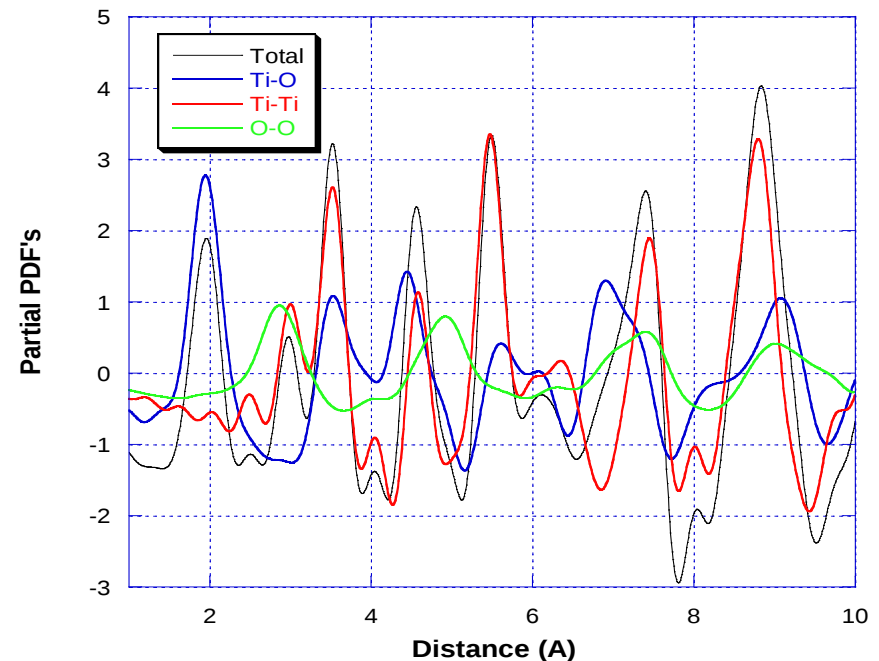
distances bien définies ($\neq$ amorphe)

Les 2 structures locales sont similaires





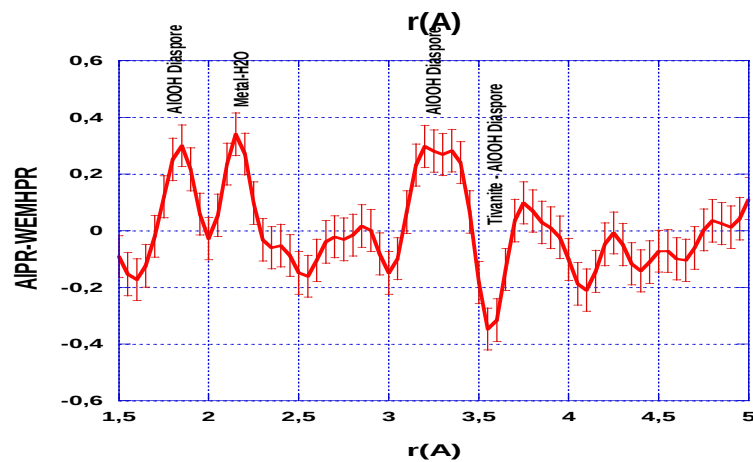
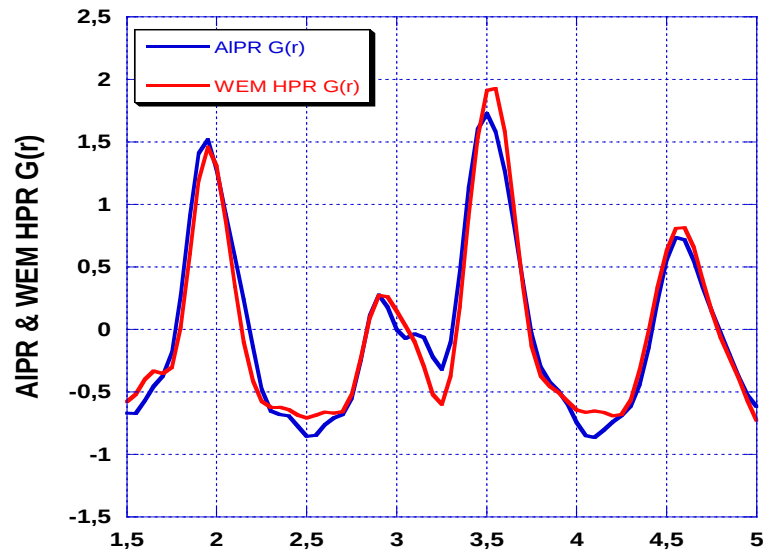
Purple up, cyan down



PdfFit avec contraintes

Le modèle de structure locale est valide
 On peut extraire la distribution des distances
 => image statistique des distortions locales
 Pas de solution unique
 (car pas de structure unique)

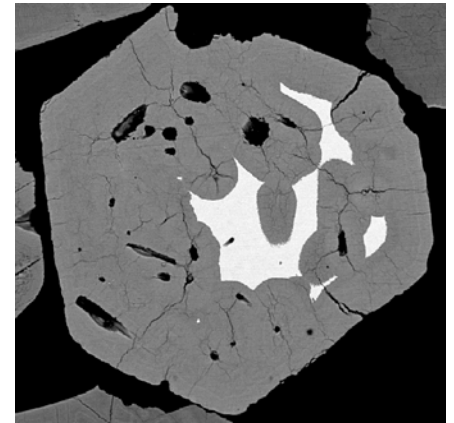
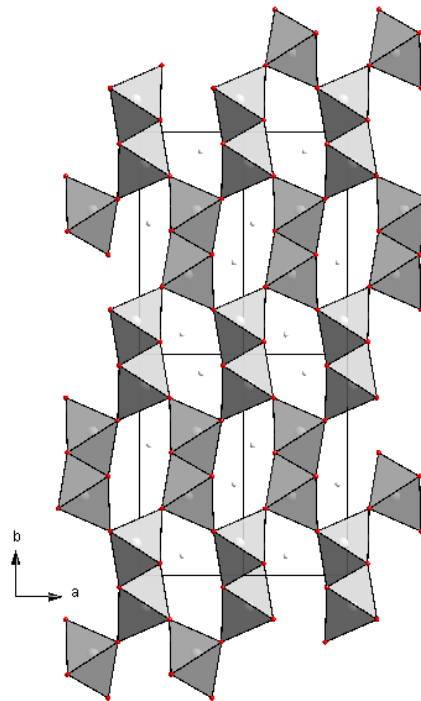
PDF différence entre 2 HPR avec et sans Al



⇒ **AlOOH diaspore.**

⇒ Normalement non stable,
mais HPR=template

⇒ Localisé dans les nanopores des grains.



Exemple : structure locale du TiO_2 nano-cristallin

TiO_2 nano-cristallin pour pile solaires (cellules de Graetzel)

Synthésisé par chimie douce (sol-gel)

recuit => anatase

quelle est la structure locale?

X-ray diffraction de poudres

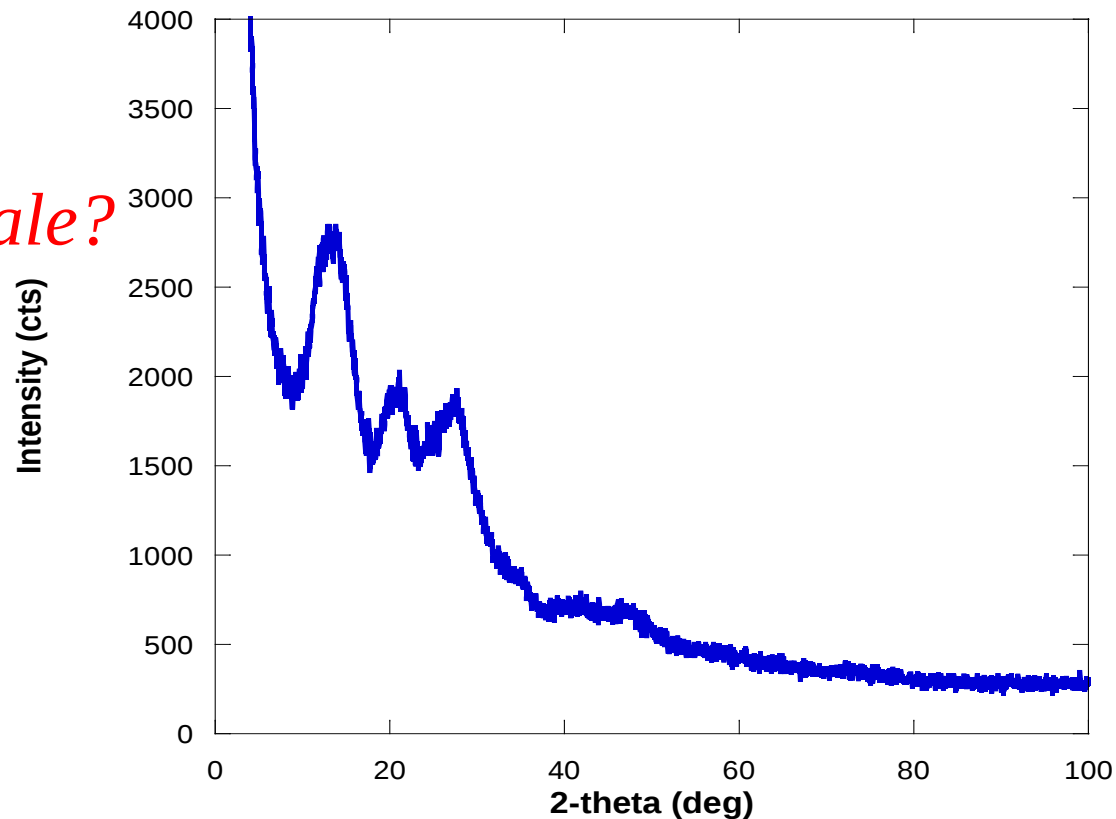
Panalytical X'pert diffract.

Mo graded multilayer optics, $\lambda=0.7107\text{\AA}$

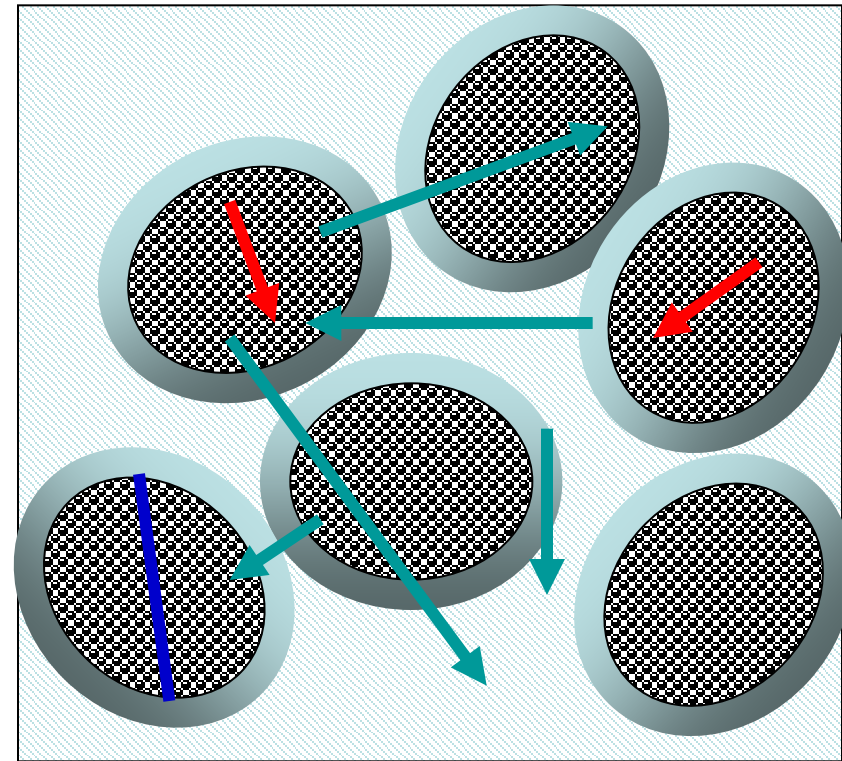
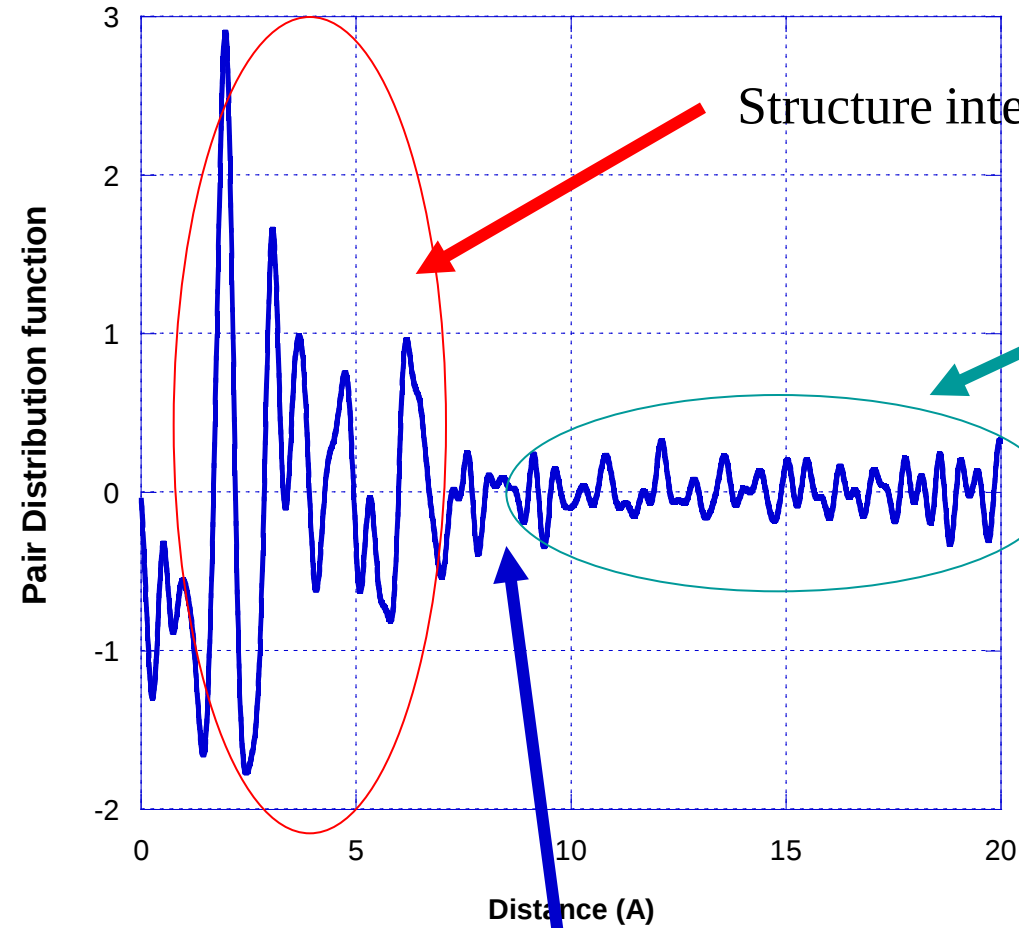
Bragg-Brentano geometry

X'celerator detector

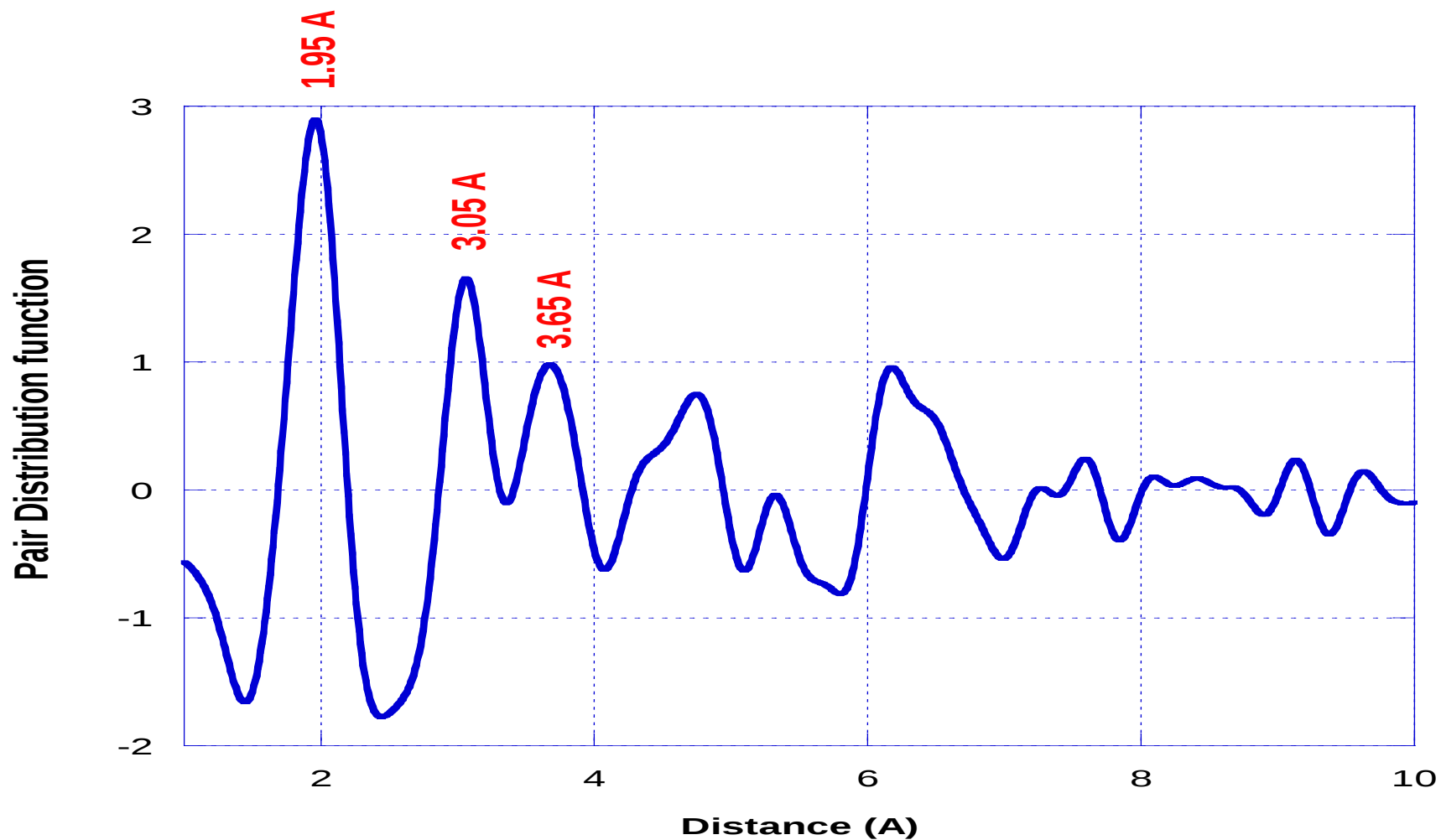
$Q_{\text{max}}=16.8\text{\AA}^{-1}$



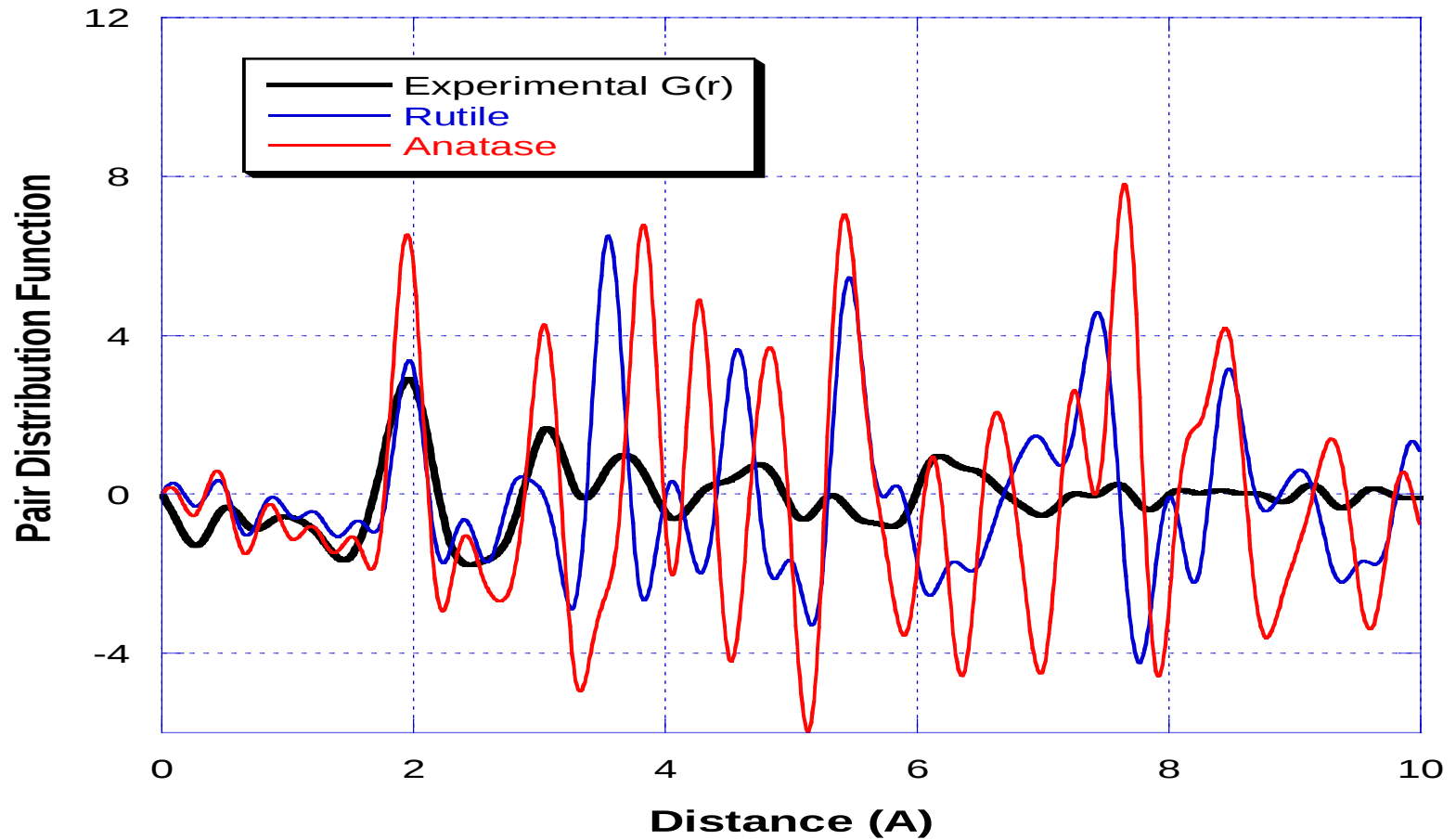
La PDF informe sur la taille des grains
et leur structure interne

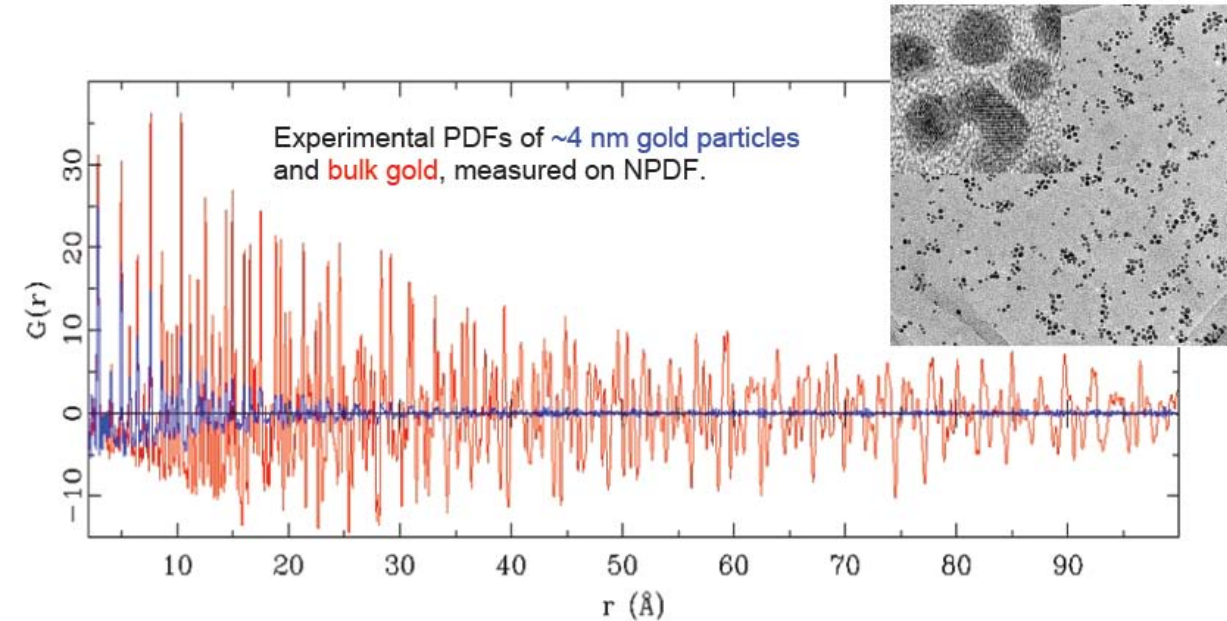


Coordination octaédrique



Localement $\neq$ rutile, anatase





K.L. Page, Th. Proffen, H. Terrones, M. Terrones, L. Lee, Y. Yang, S. Stemmer, R. Seshadri and A.K. Cheetham, **Direct Observation of the Structure of Gold Nanoparticles by Total Scattering Powder Neutron Diffraction**, *Chem. Phys. Lett.* **393**, 385-388 (2004).

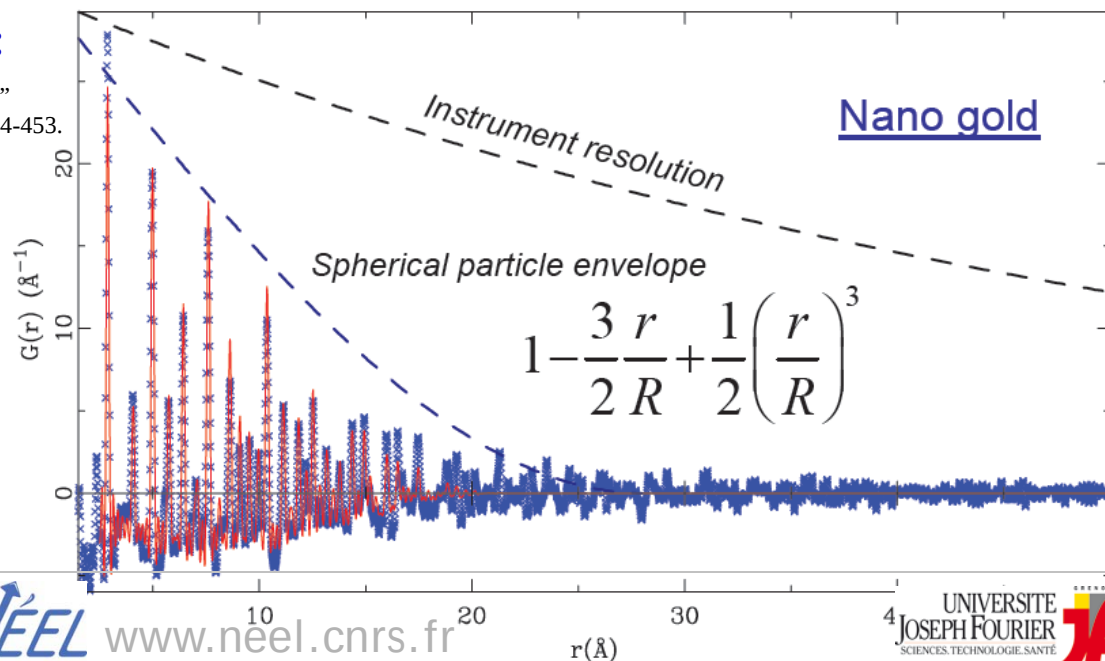
Facteur de forme de la particule:

“Finite Size Effects of Nanoparticles to the Atomic Pair Distribution Functions”
K. Kodama, S. Iikubo, T. Taguchi and S. Shamoto, *Acta Cryst. A* 62 (2006) 444-453.

$$G(r) \approx f(r)G_{\infty}(r)$$

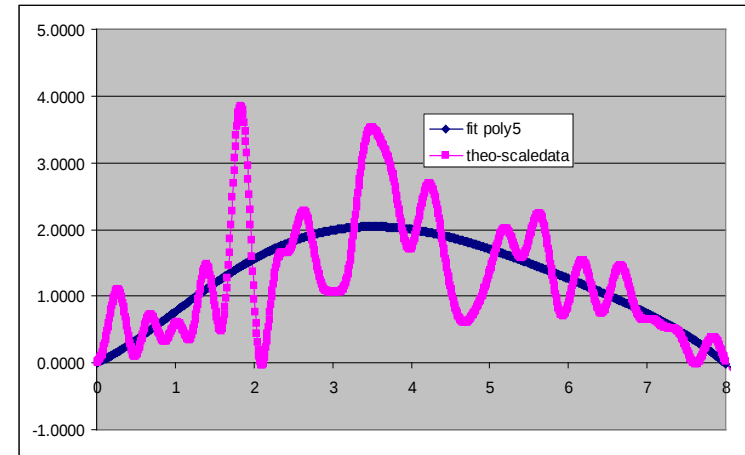
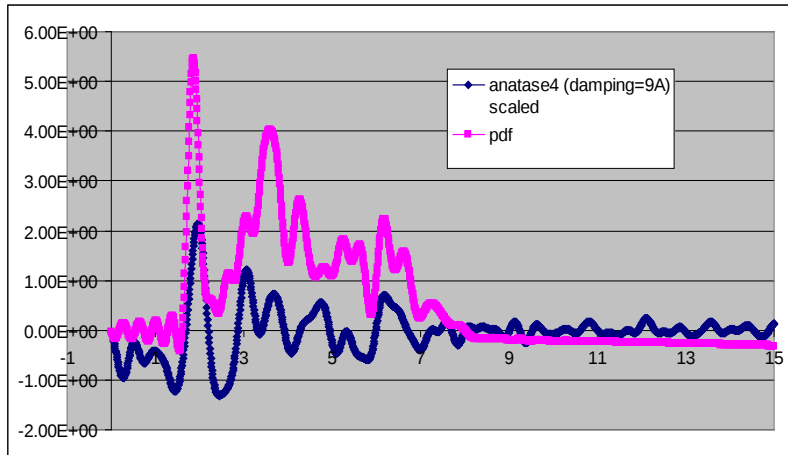
$f(r)$ dépend de la forme (cf SAS)

Pour une sphère: $f(r) = 1 - \frac{3}{2} \frac{r}{R} + \frac{1}{2} \left(\frac{r}{R} \right)^3$

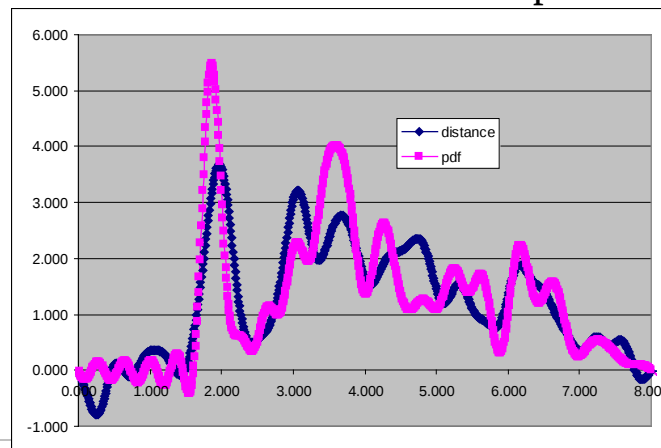


Particules de forme quelconque

La PDF théorique est calculée en plaçant la particule dans une très grande maille pour éviter les contributions inter-particules. Mais la densité moyenne est faussée et non constante.



On calcule la PDF théorique, on soustrait l'expérimentale et on fitte la différence avec un polynome et un facteur d'échelle. La correction est appliquée aux données expérimentales, puis on affine le modèle. On boucle la procédure avec le nouveau modèle.



Modélisation de la structure des clusters

On ne sait pas résoudre ab initio

On produit un modèle raisonnable de la structure avec

connaissance cristallographique

modélisation quantique (énergie de configuration)

infos d'autres techniques (e⁻ microscopie, spectroscopies)

On calcule la pdf et compare à la pdf expérimentale

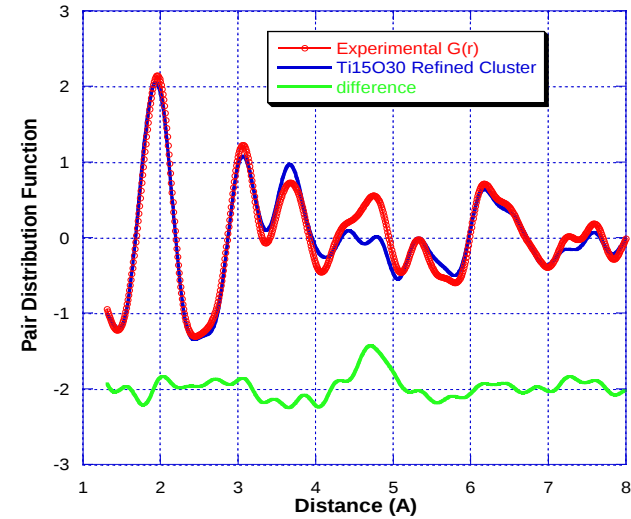
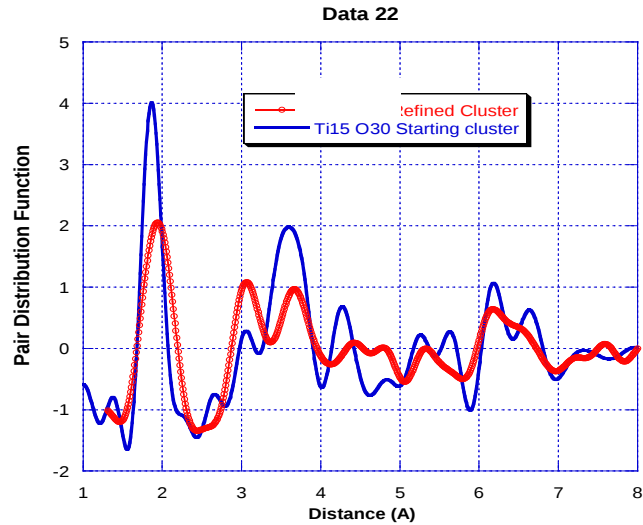
Rejette si trop mauvais

Sinon, affinement dans l'espace direct (PDFFit)

Recalcul de l'énergie de configuration du modèle affiné

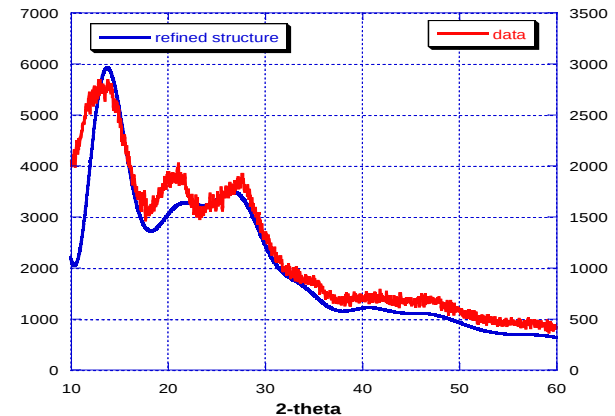
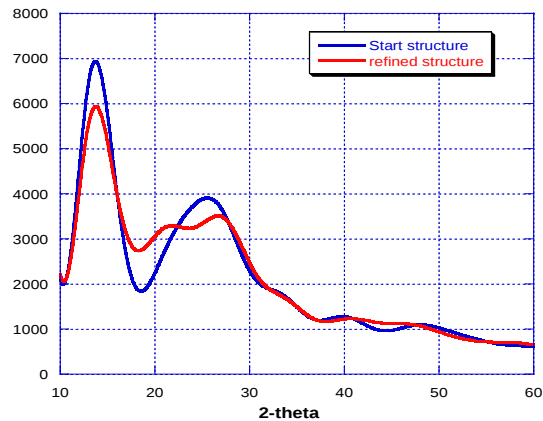
....

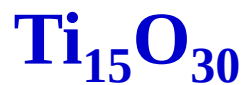
Essai d'affinement PDF dans l'espace direct : $\text{Ti}_{15}\text{O}_{30}$ cluster (S. Hamad et al. (2005))



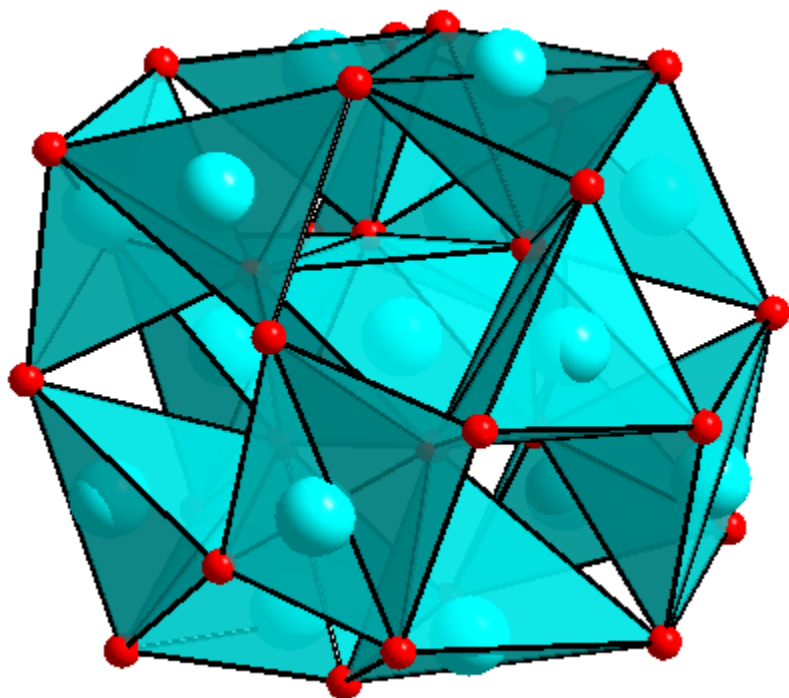
Diffractogramme recalculé avec la formule de Debye

$$I(2\theta) = \sum_{ij} b_i b_j \sin(Qr_{ij}) / Qr_{ij}$$

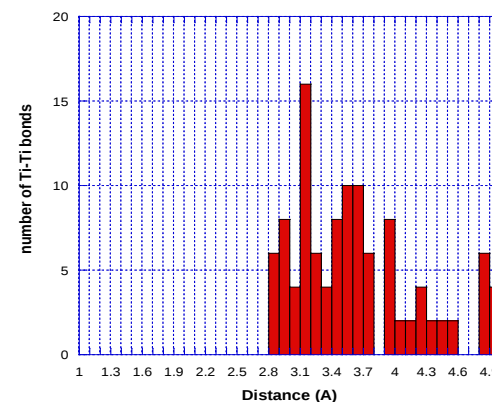
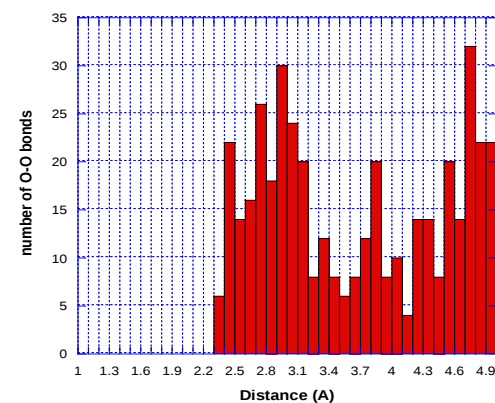
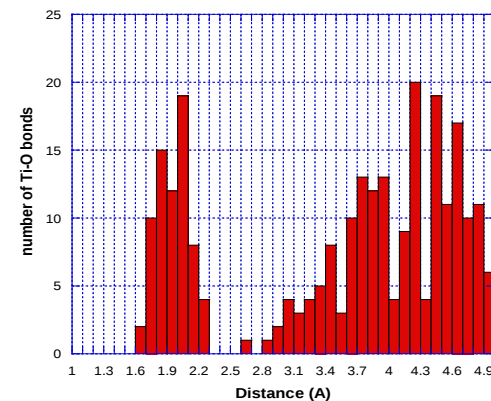




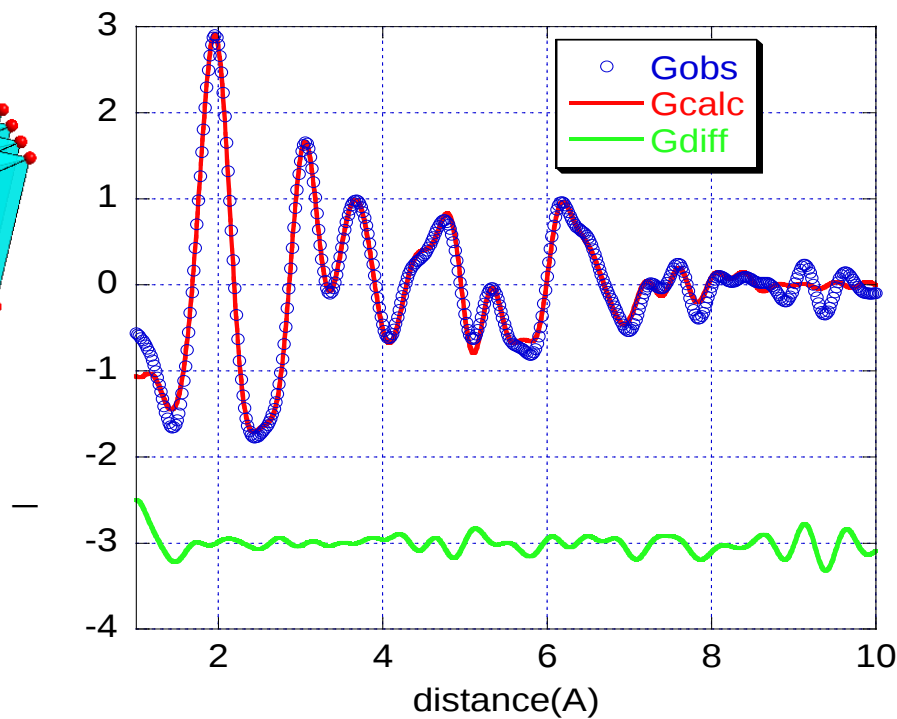
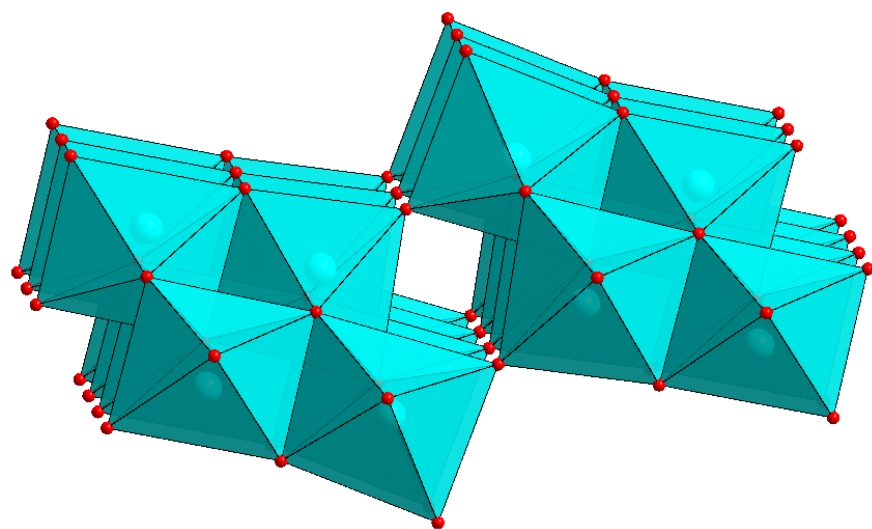
Après affinement PDF

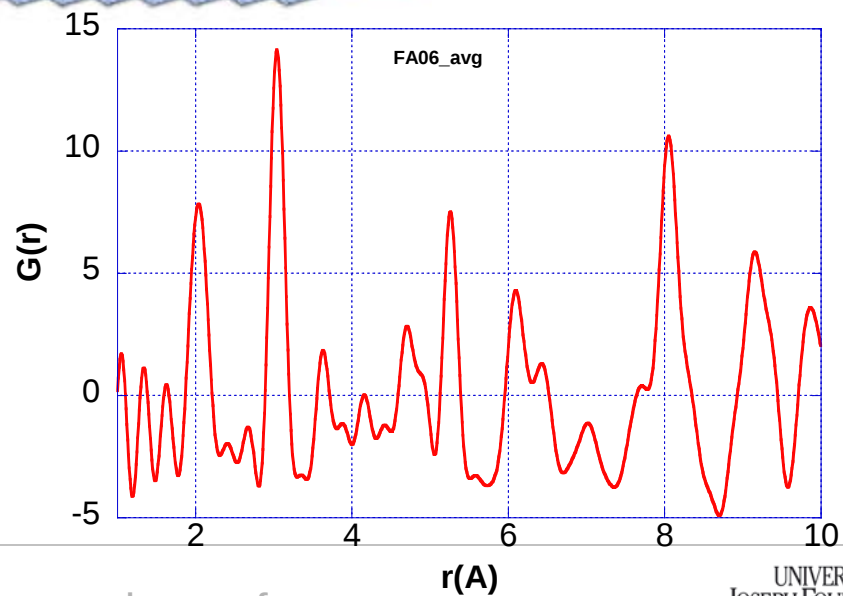
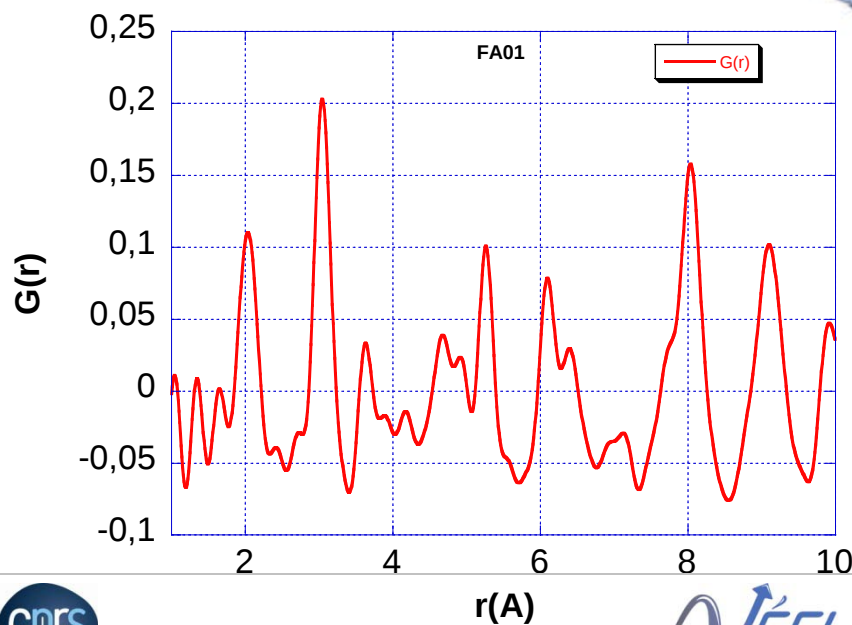
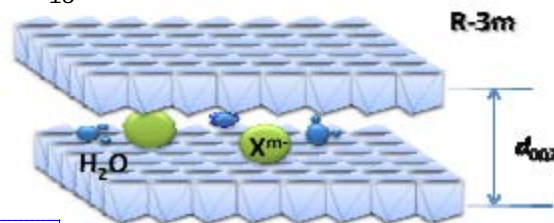
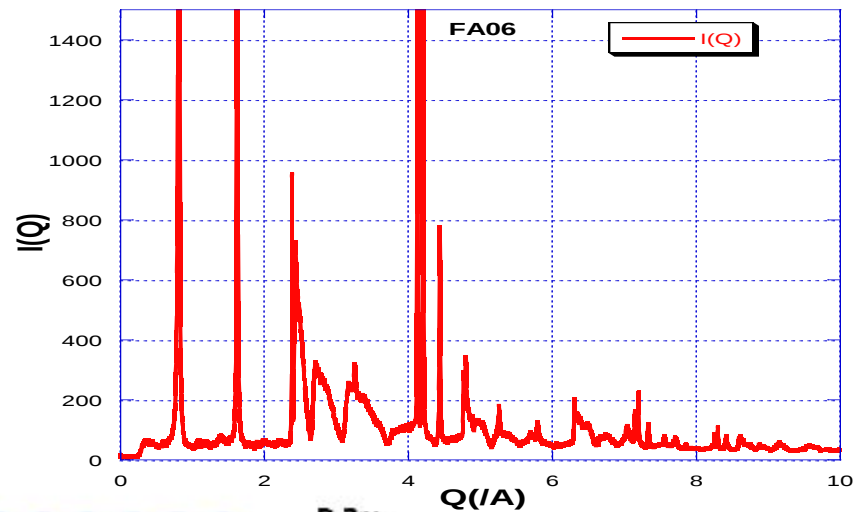
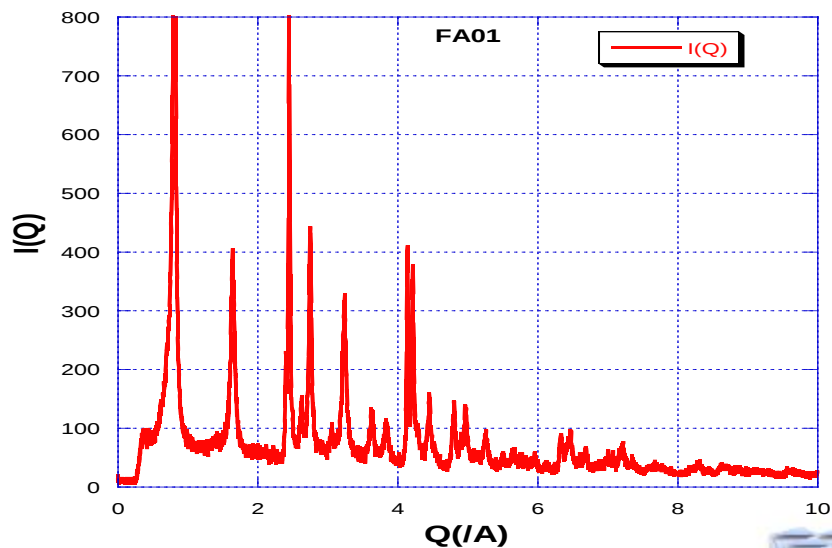


1 Ti 6-coordinated
8 Ti 5-coordinated
6 Ti 4-coordinated



Meilleur modèle ;
Construit à partir de $\text{H}_2\text{Ti}_3\text{O}_7$

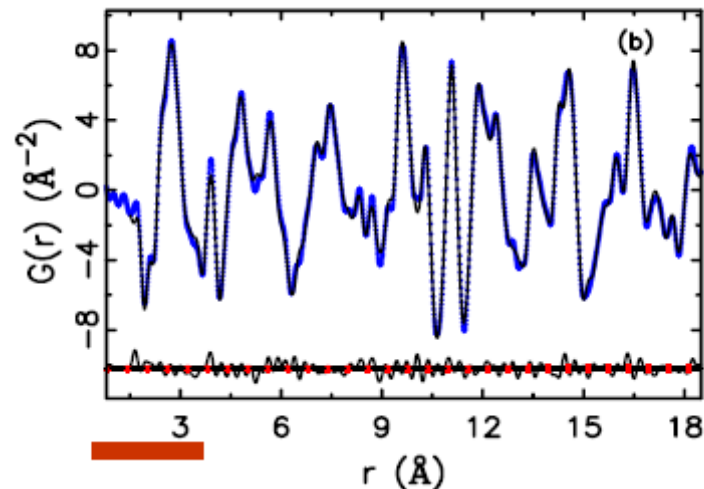
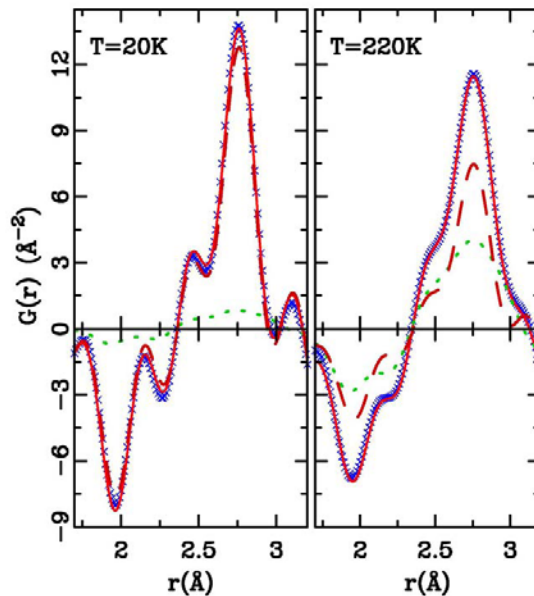
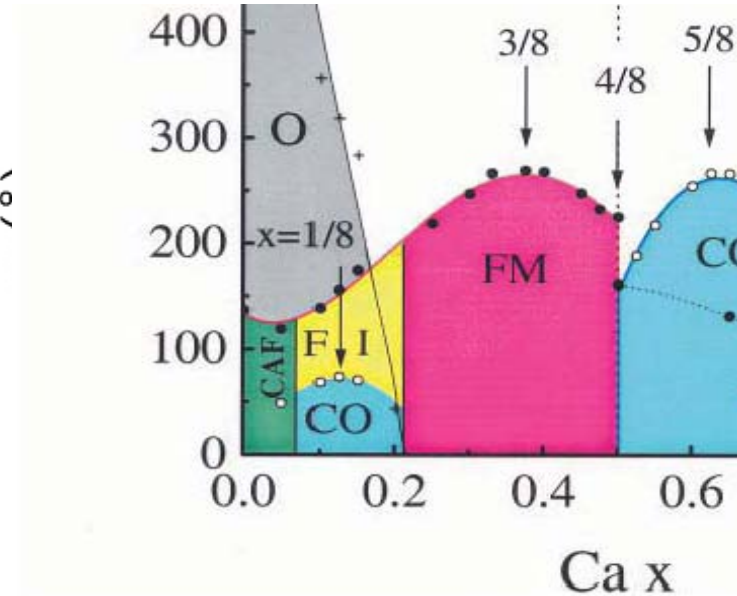
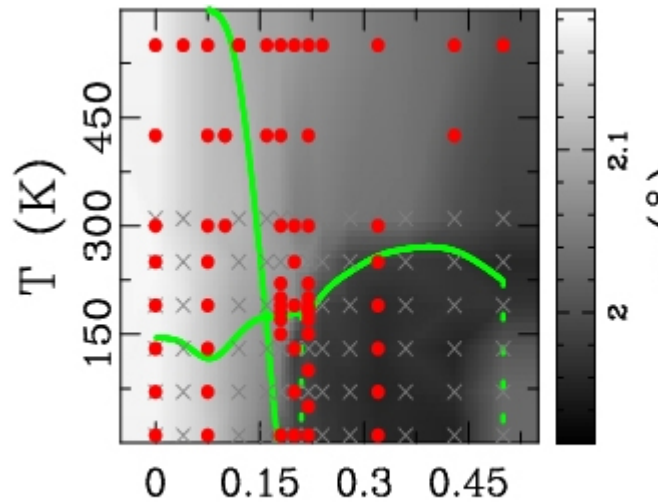




(LaCa)MnO₃ manganites

Comparaison des structures locale et moyenne

La distorsion JT persiste dans la phase métallique ?

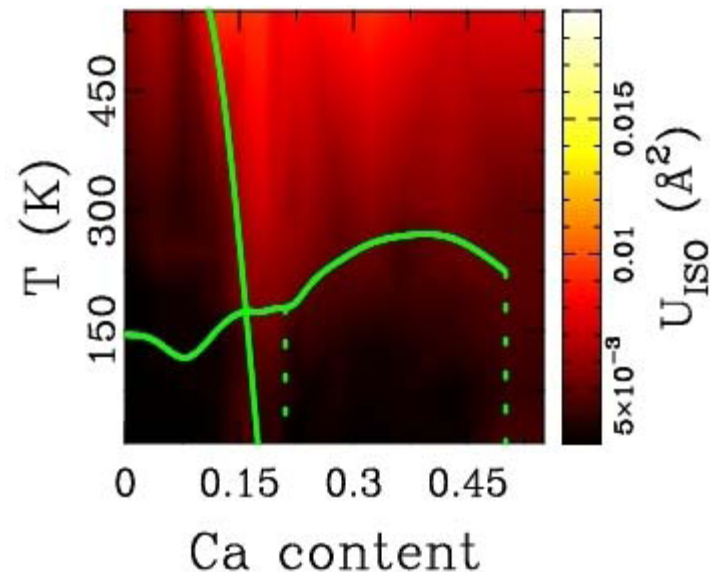
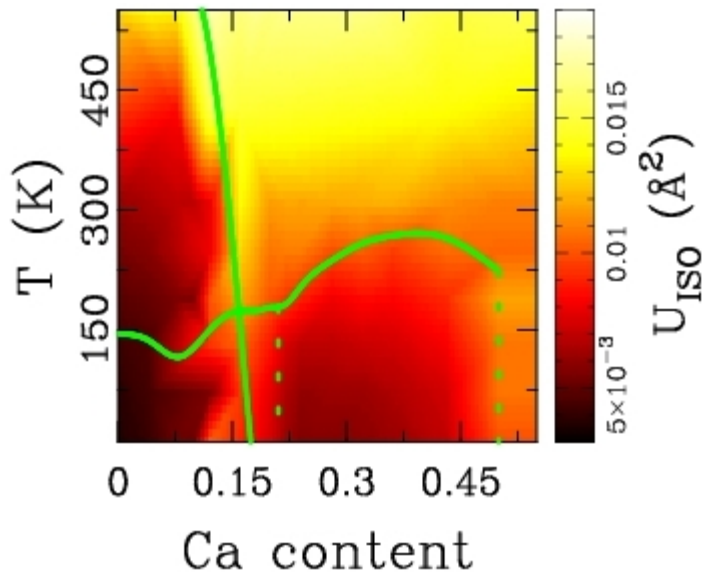
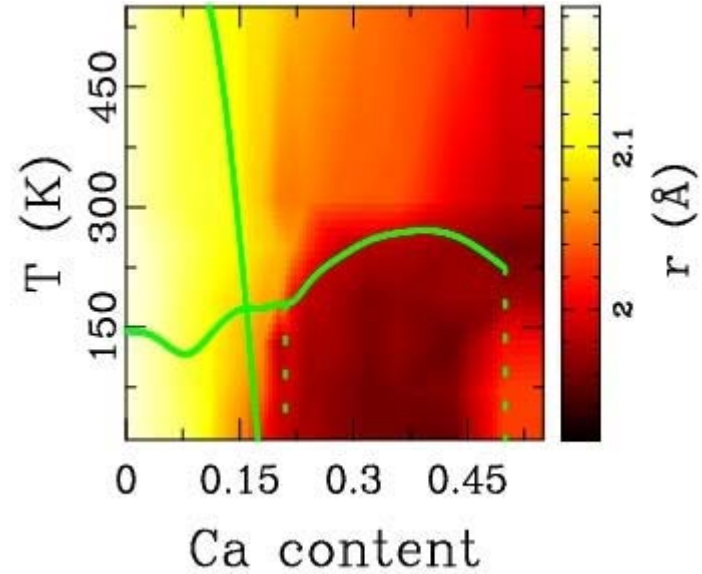
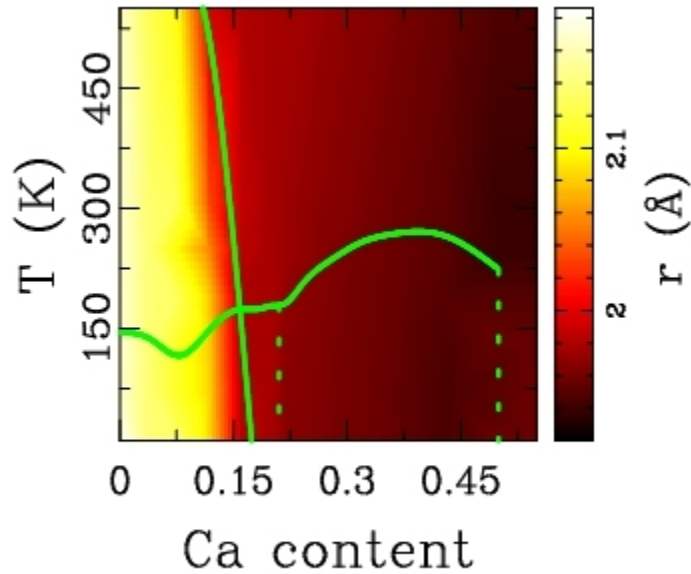


(x,T) results: Rietveld vs PDF (Pbnm)

Longueur de liaison (=distorsion Jahn-Teller)

AVERAGE

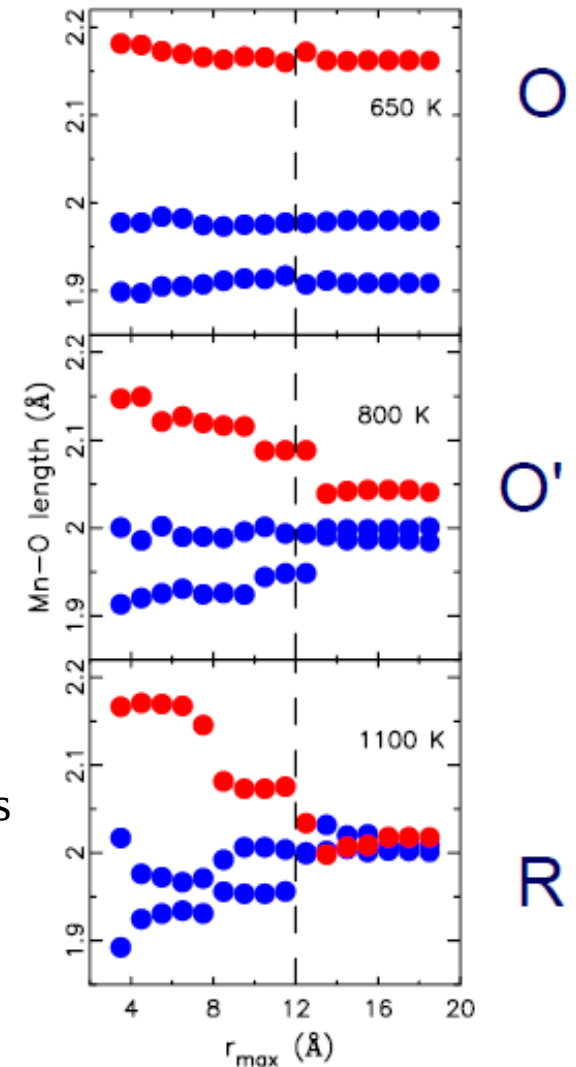
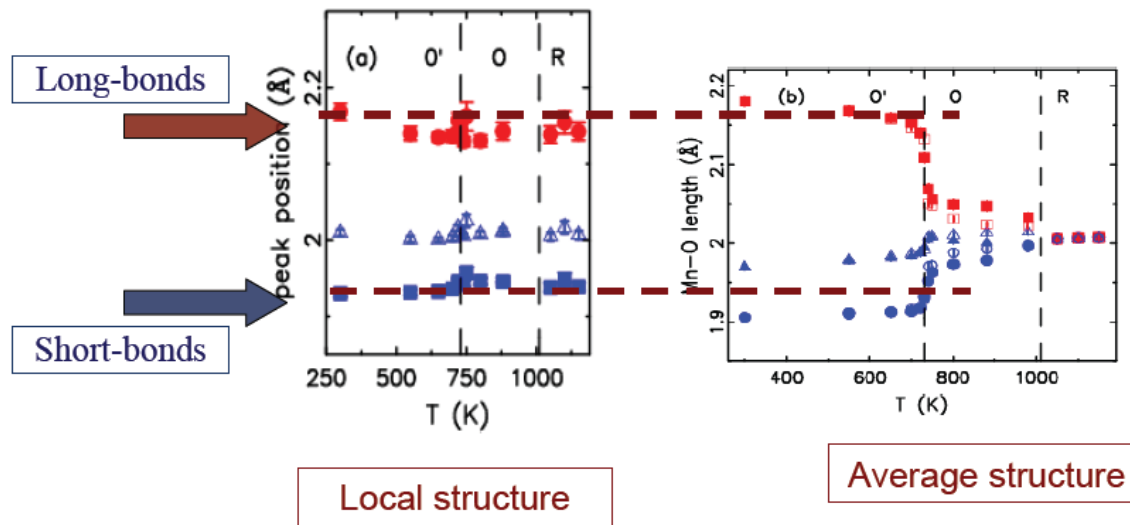
LOCAL



LaMnO₃ vs T :

Mn-O bonds are constant up to the R phase

JT distortion persists locally in the ortho and rhombo phases



LaMnO₃ vs r :

Affis dans des domaines en r variables

Fixe $r_{\min}$, varie $r_{\max}$

Perovskites multiferroïques : structures de BiMnO_3 et BiCrO_3

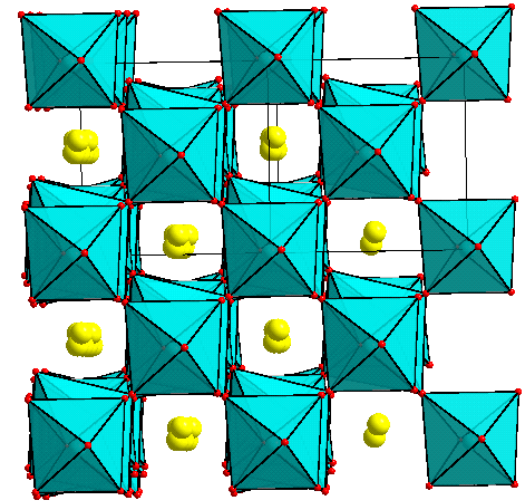
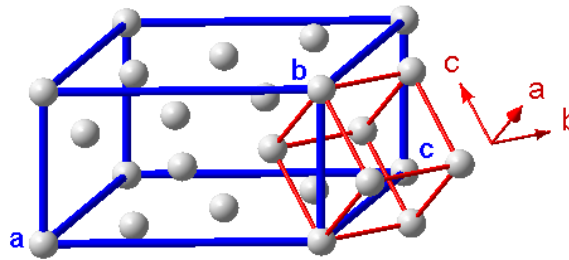
BiMnO_3 : $T(\text{"FE"})=760\text{K}$, $T(\text{FM})=105\text{K}$

BiCrO_3 : $T(\text{"FE"})=430\text{K}$, $T(\text{AFM})=120\text{K}$

Structure proposée: $Pbnm \Rightarrow C121$ at 430K

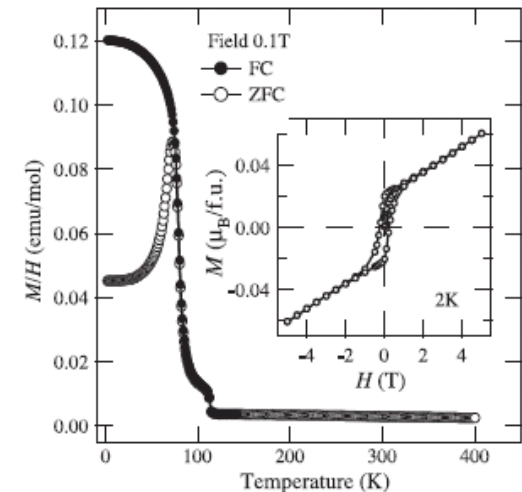
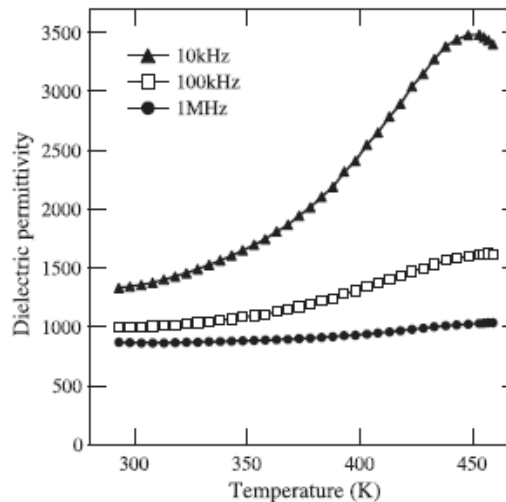
$a=9.47\text{\AA}$, $b=5.48\text{\AA}$, $c=9.59\text{\AA}$, |

isostructuraux



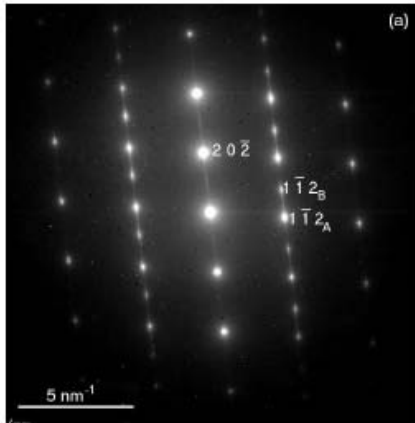
Synthèse HP-HT TEM, RX, thermo-chimie RX In situ HP-HT

C Darie, P. Toulemonde, C. Goujon,
H. Klein, M. Bacia, P. Bordet
Coll. ESRF, LMGP...

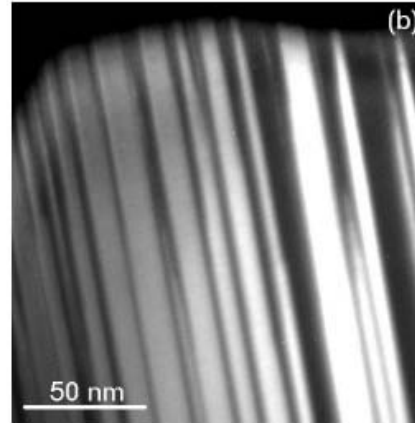


Niitaka et al., Solid State Ionics 172 (2004) 557–559

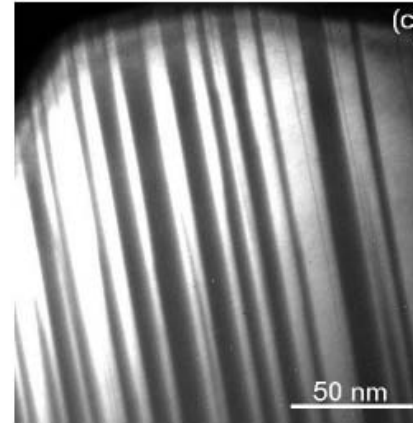
Structure « moyenne » de BiCrO_3



(a) Electron diffraction pattern of the $[1\ 3\ 1]$ zone axis of monoclinic BiCrO_3 .

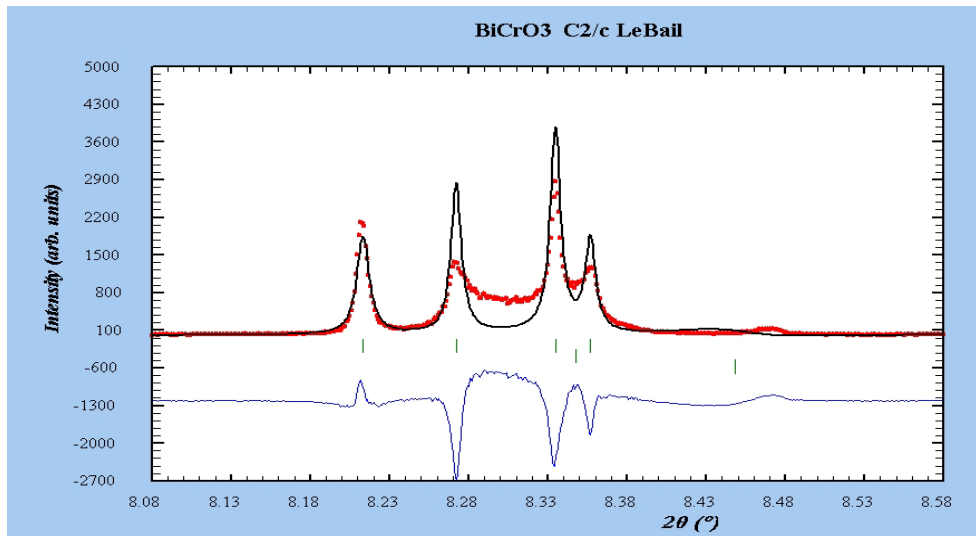


(b) Dark field image of BiCrO_3 selecting a spot of family A.



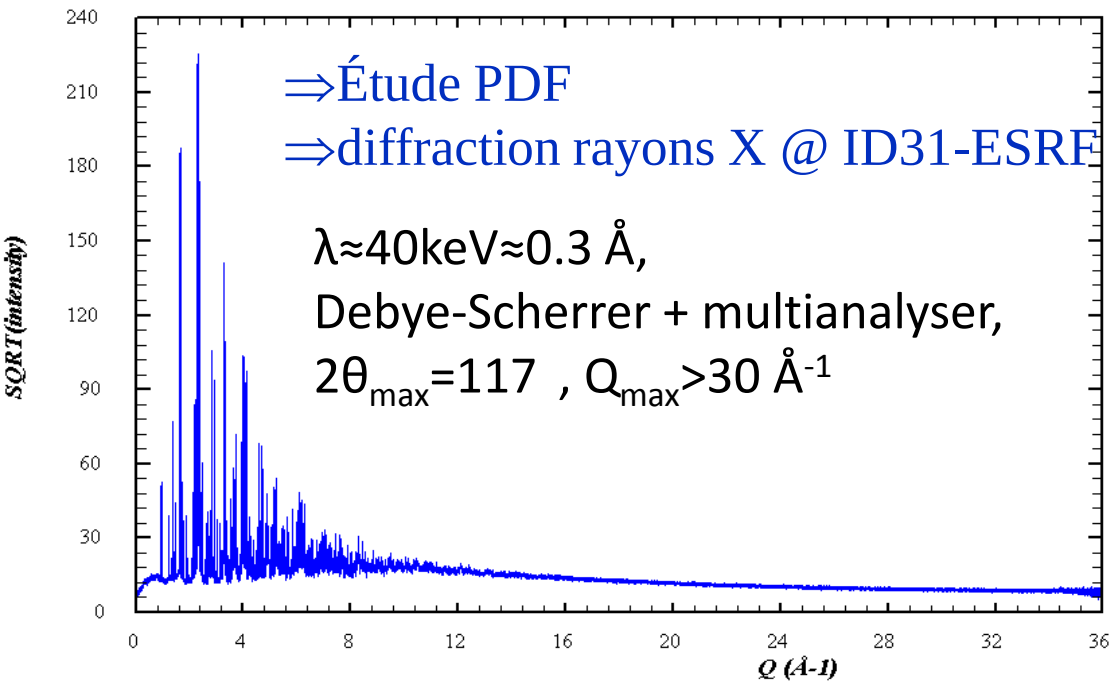
(c) Dark field image of BiCrO_3 selecting a spot of family B.

TEM
Macles
Qques
nanomètres

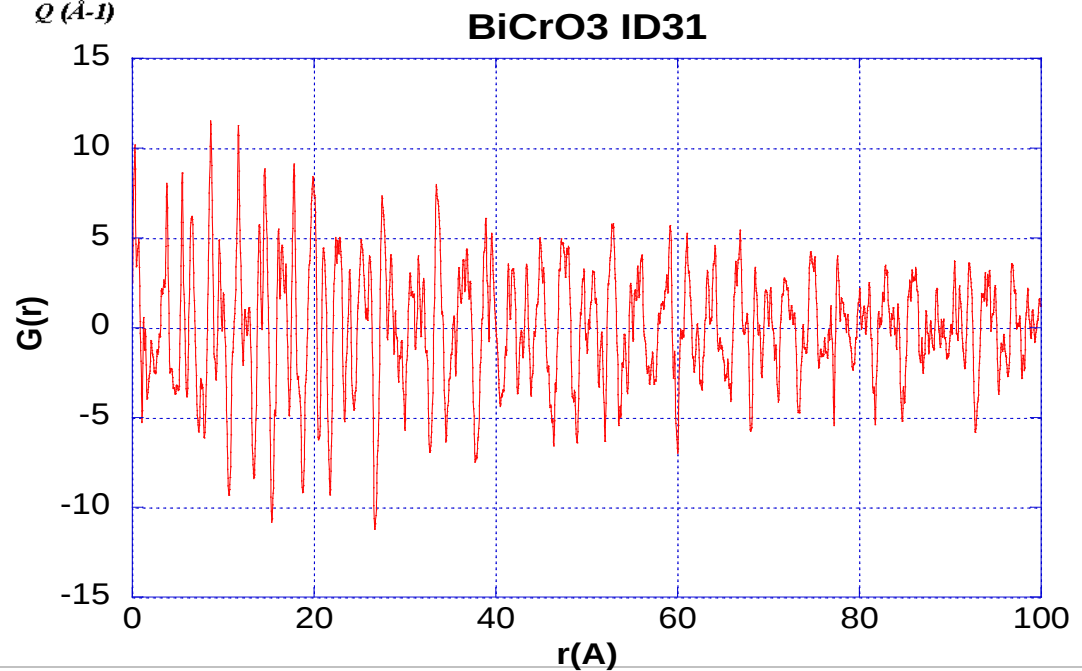


ESRF-ID31
Diffusion diffuse

=> Affinements impossibles

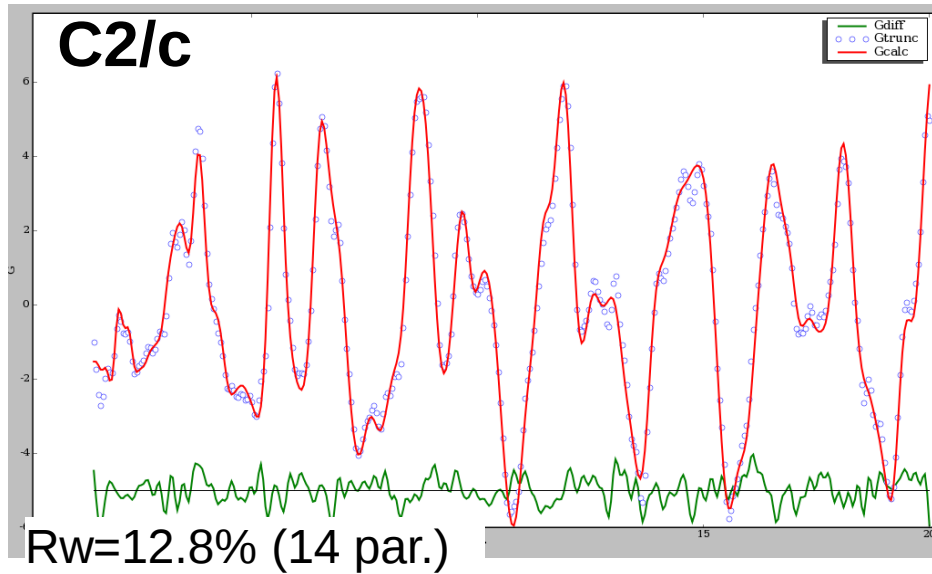


Mesure de BiMnO_3 et BiCrO_3



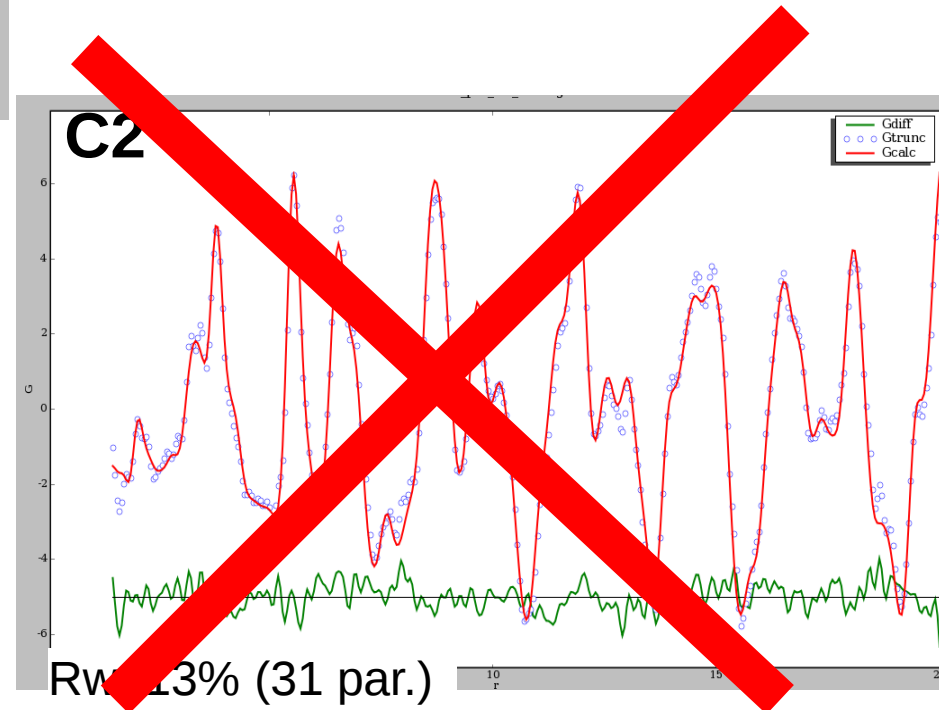


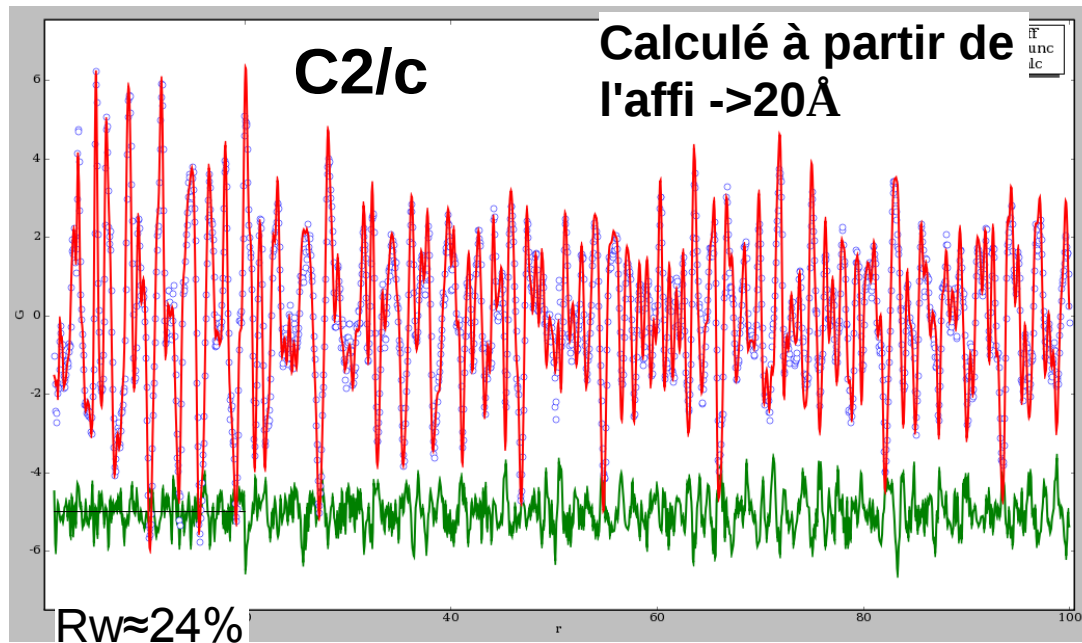
Affinements de la PDF -> 20Å



C2/c : Centrosymétrique
(=> pas ferroélectrique)

C2 : Non Centrosymétrique
(=> ferroélectrique)

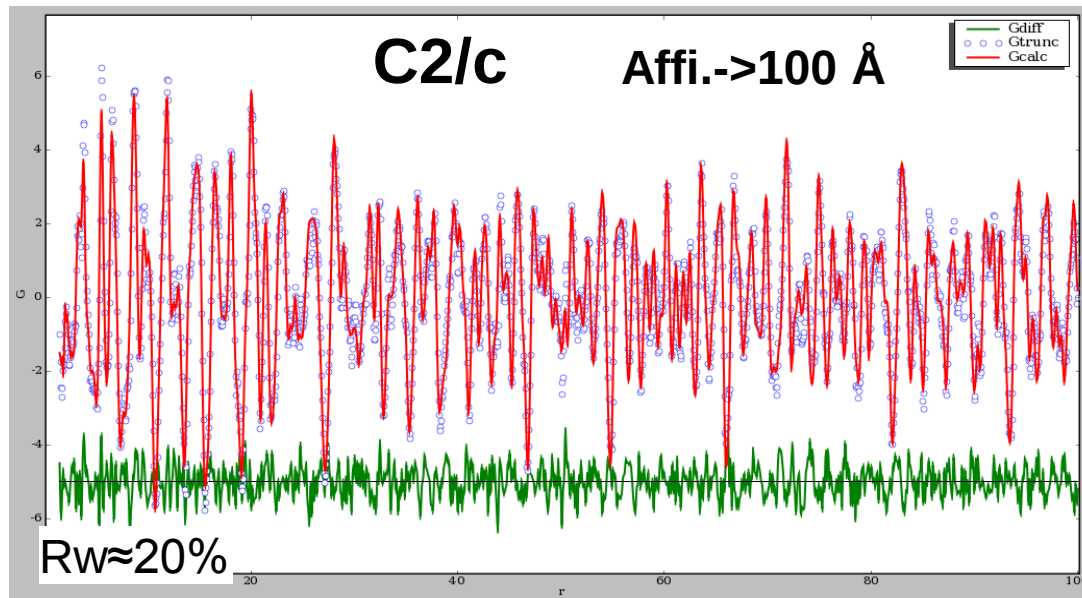




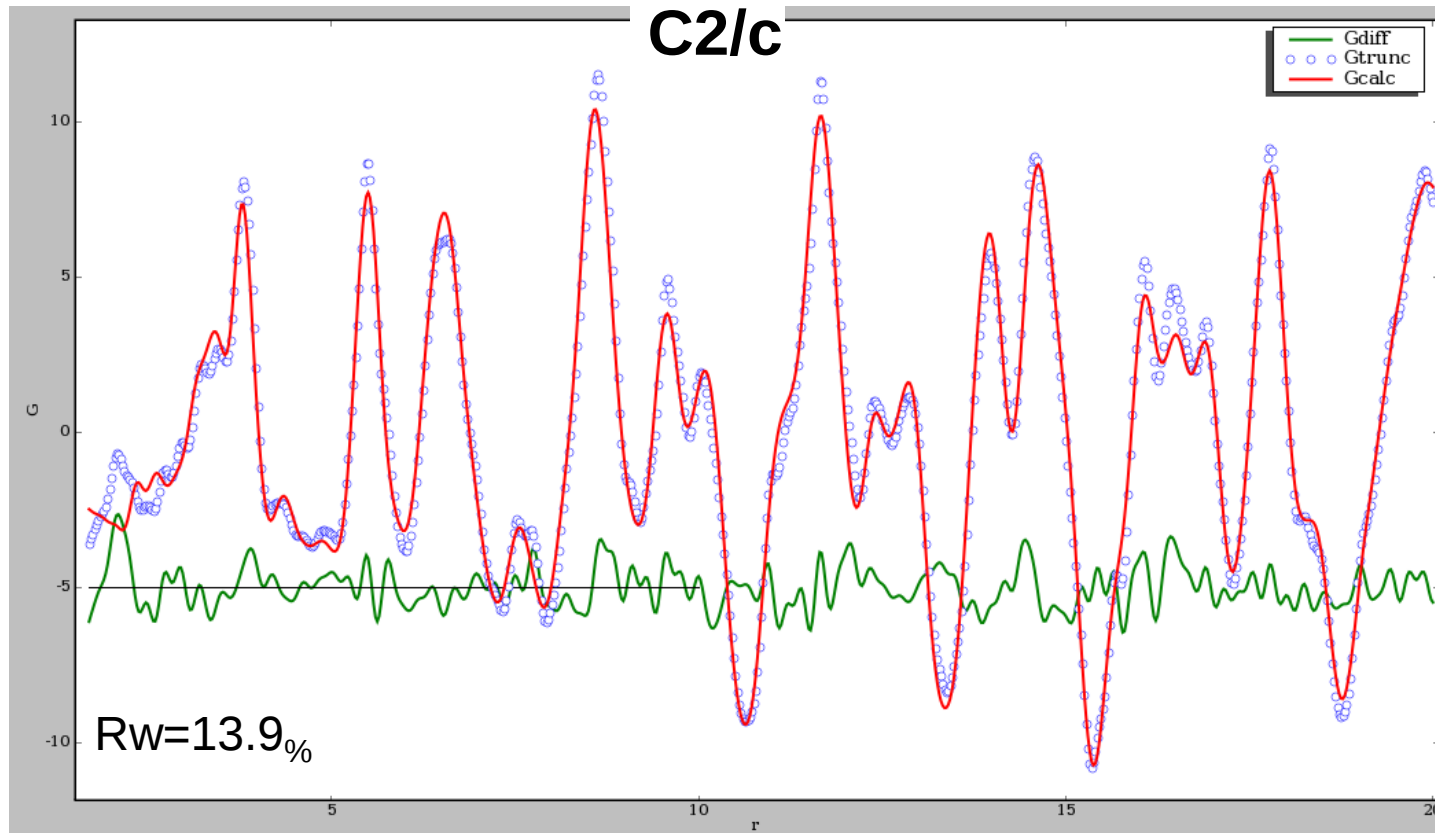
BiMnO₃

**Structure locale
 $\approx$ structure moyenne**

pas de désordre



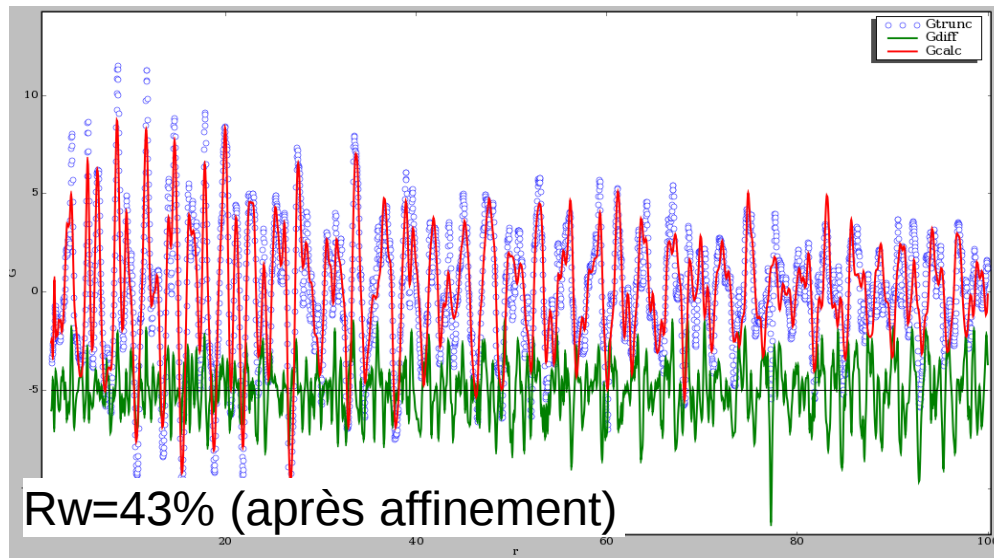
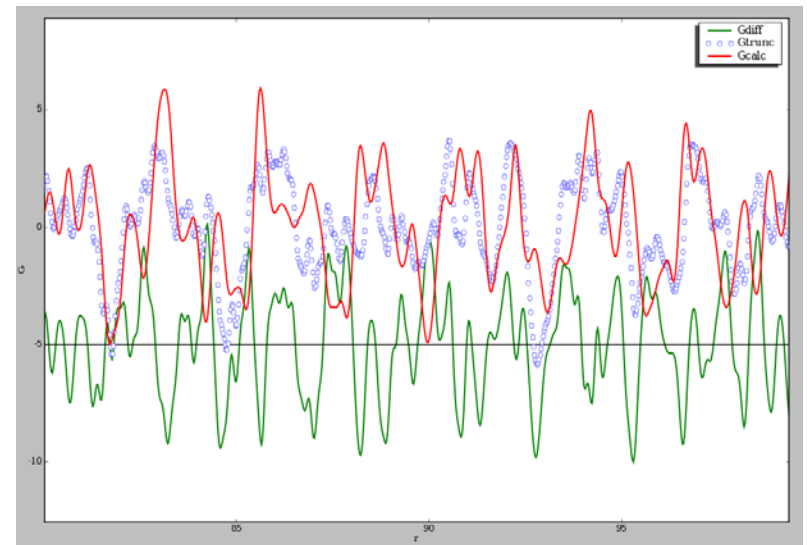
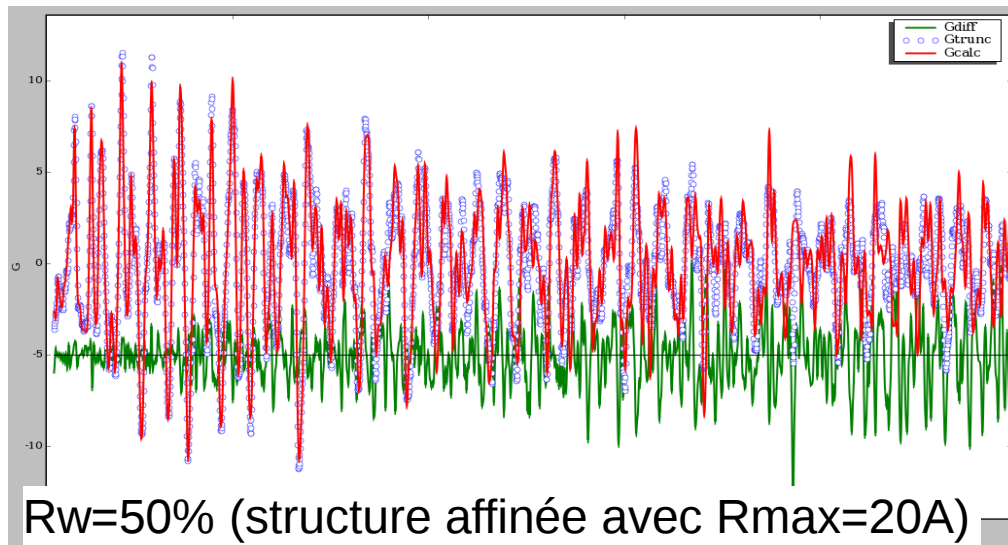
BiCrO_3 : on a accès à la structure locale malgré les macles



Affinement correct avec C2/c (pas mieux en C2)

Qualité comparable (un peu moins bonne) que BiMnO_3

=> structure locale centrosymétrique



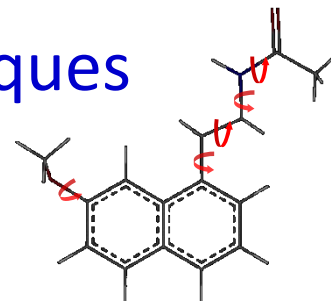
Structure locale
 $\neq$ structure moyenne

=> influence des macles

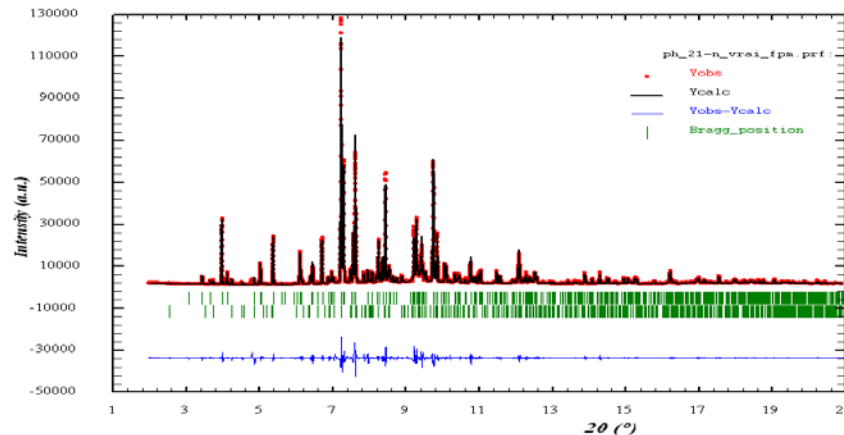
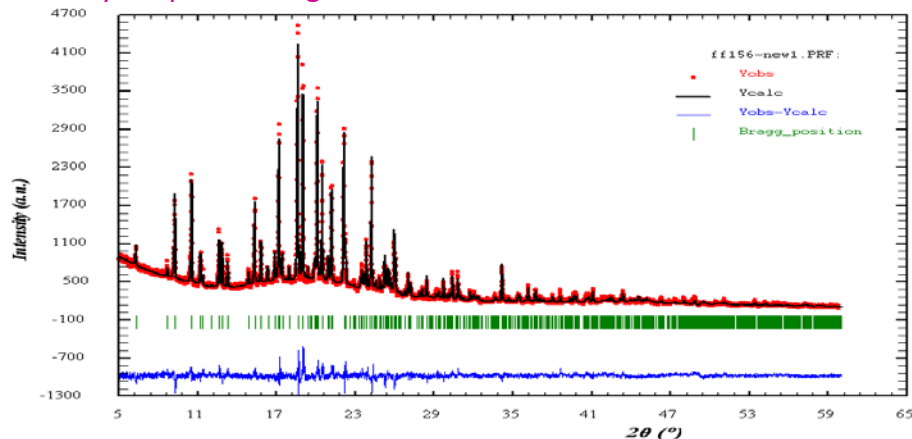
=> étudier la structure
 des parois de macles

Analyse PDF de matériaux pharmaceutiques

En général plusieurs polymorphes
=> *Structure sur poudres, blocs rigides*



Polymorphes de l'agomélatine :



Nouvelles méthodes de synthèse

(p. ex. broyage)

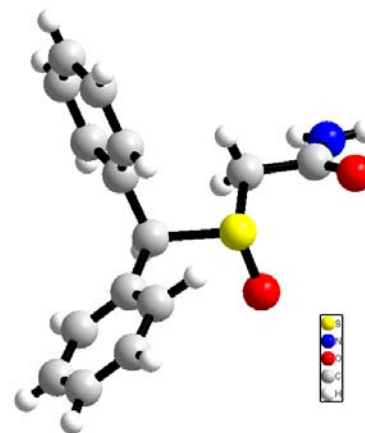
⇒ **Nouveaux polymorphes mal cristallisés**

⇒ Propriétés différentes

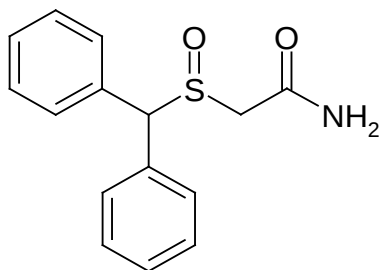
⇒ Meilleure solubilité/efficacité

⇒ **PDF pour déterminer leur structure :**

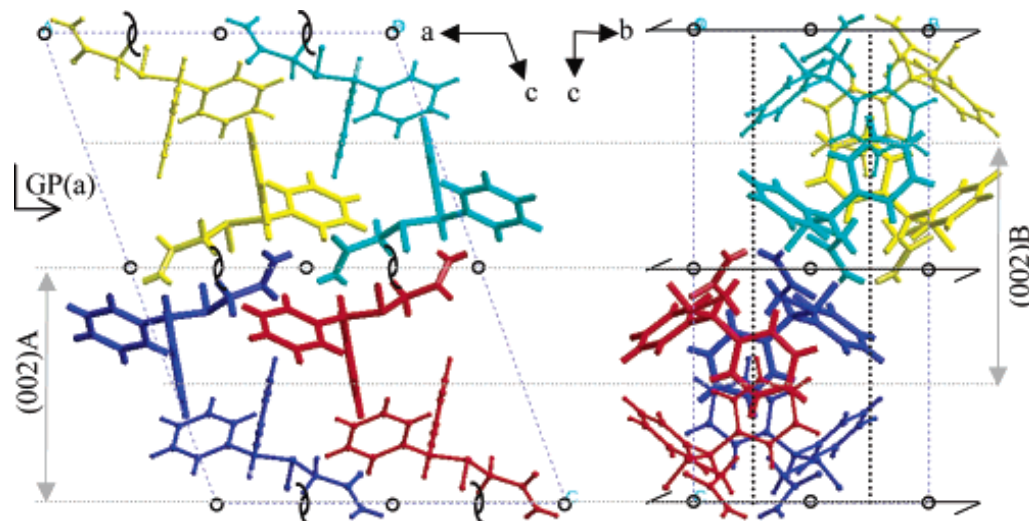
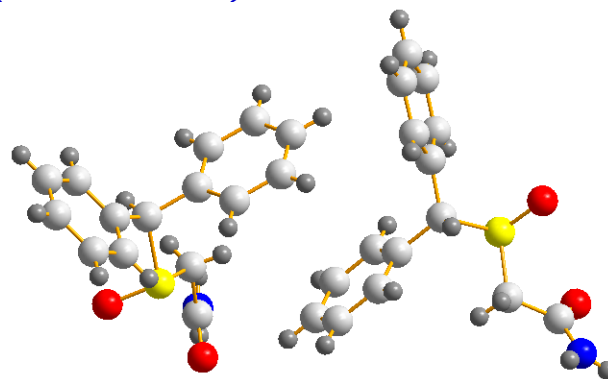
⇒ *ab initio recuit simulé en blocs rigides*



exemple d'étude PDF de composé pharmaceutique: rac-modafinil, coll. G. Coquerel et al. (univ. Rouen)



2-(diphénylméthyl)sulfinyl)-N-acétamide



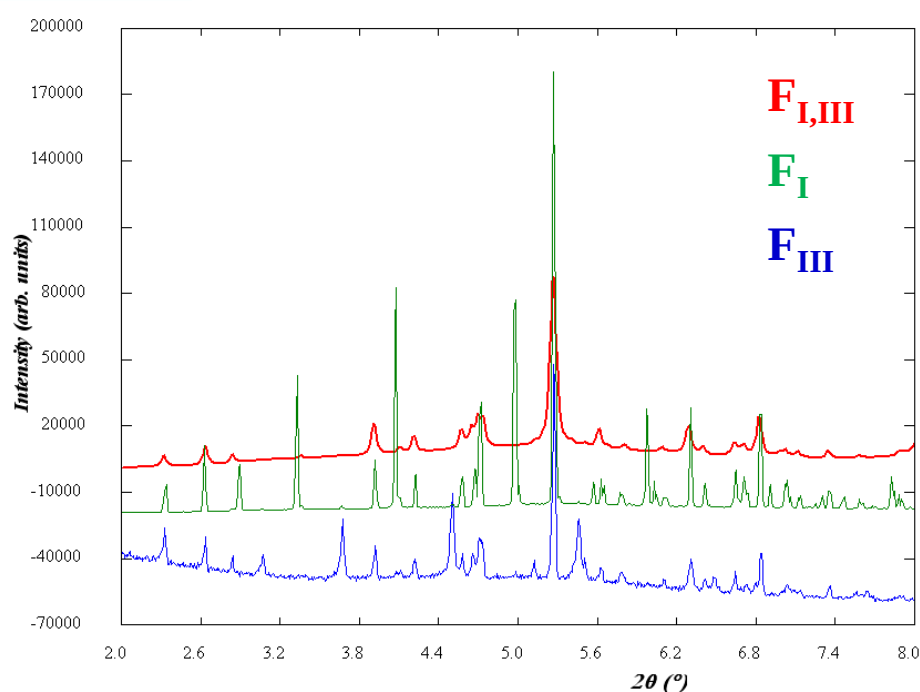
M. Pauchet et al.,
Crystal Growth and Design, 4-6, 1144 (2004)

7 polymorphes

Formes F_I & F_{III} quasi - isoenergétiques
change of (002)A slab stacking along a

Forme $F_{I,III}$ obtenue par broyage haute énergie, ou spray drying. Fortement désordonnée

Structure inconnue



$F_{I,III}$ réflexions communes à F_I & F_{III}

LeBail fits $\Rightarrow$ domaines ~ 5 nm

états intermédiaires :

Disparition progressive des (11 $\bar{l}$)

Diffractogrammes de mauvaise qualité

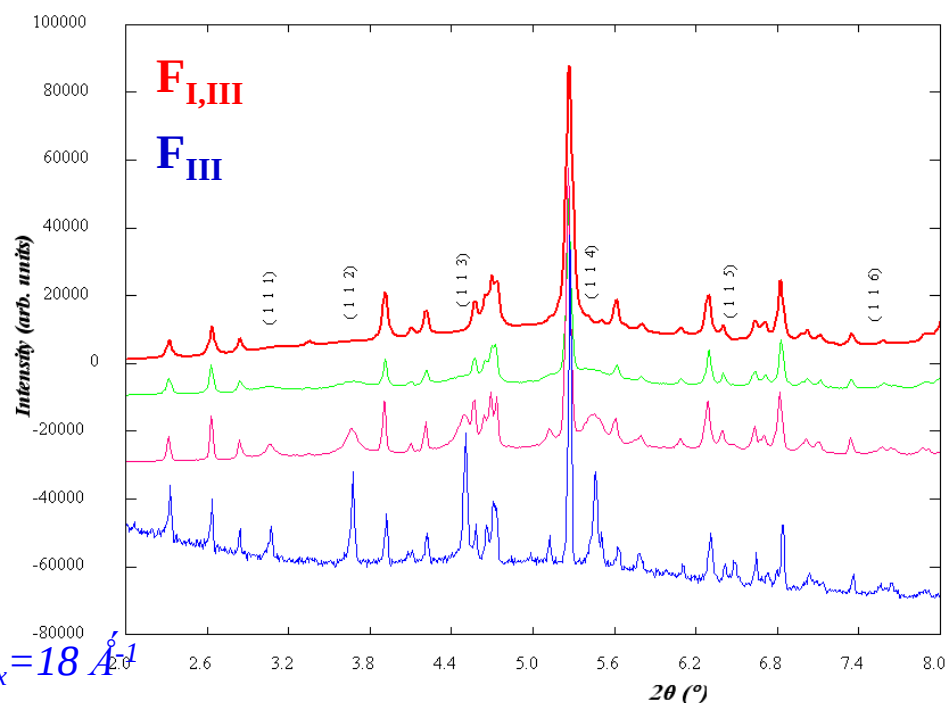
$\Rightarrow$ structure non résolue

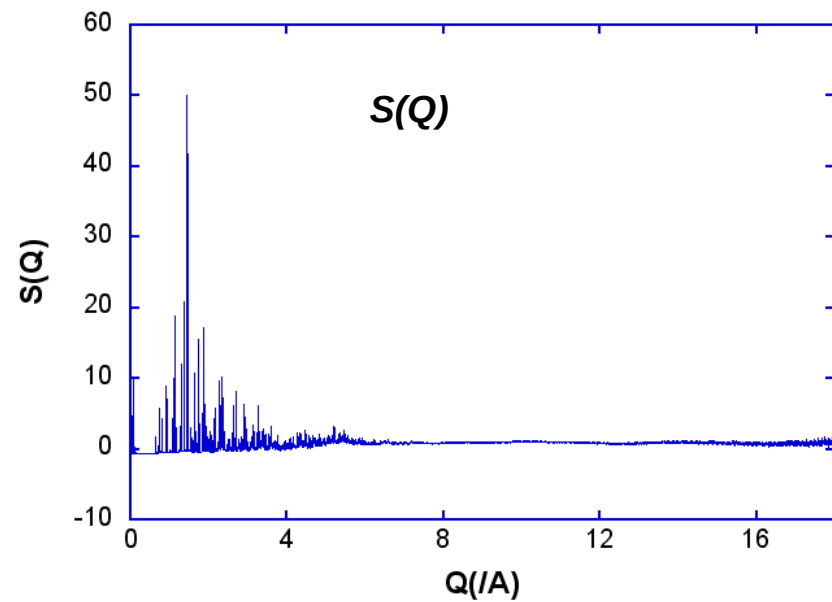
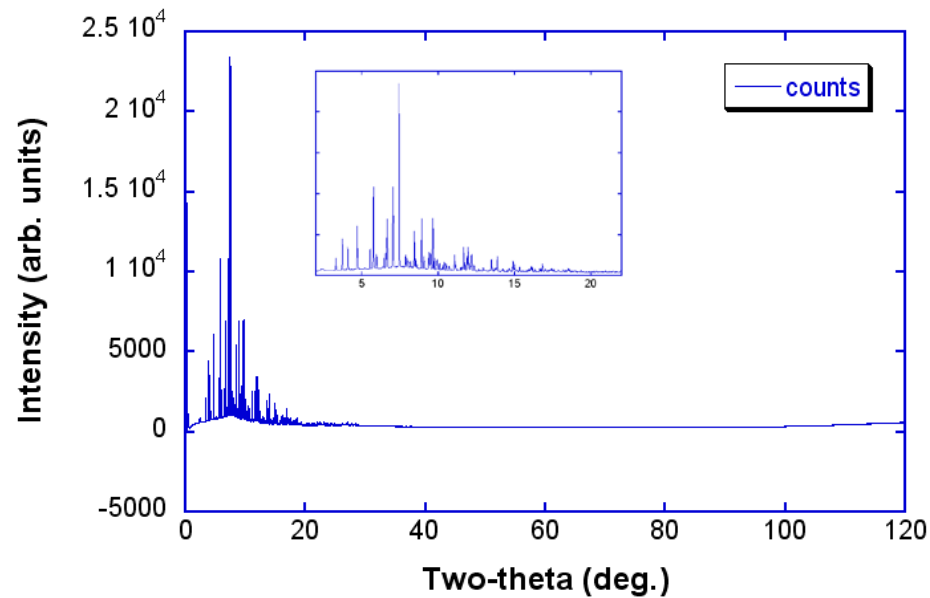
$\Rightarrow$ PDF experiment,

ESRF CRG-D2AM, Debye-Scherrer,

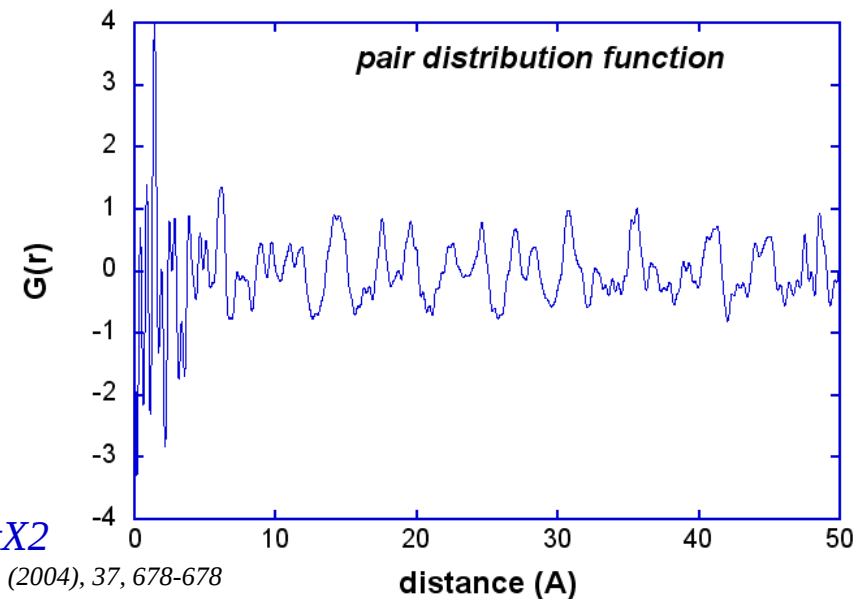
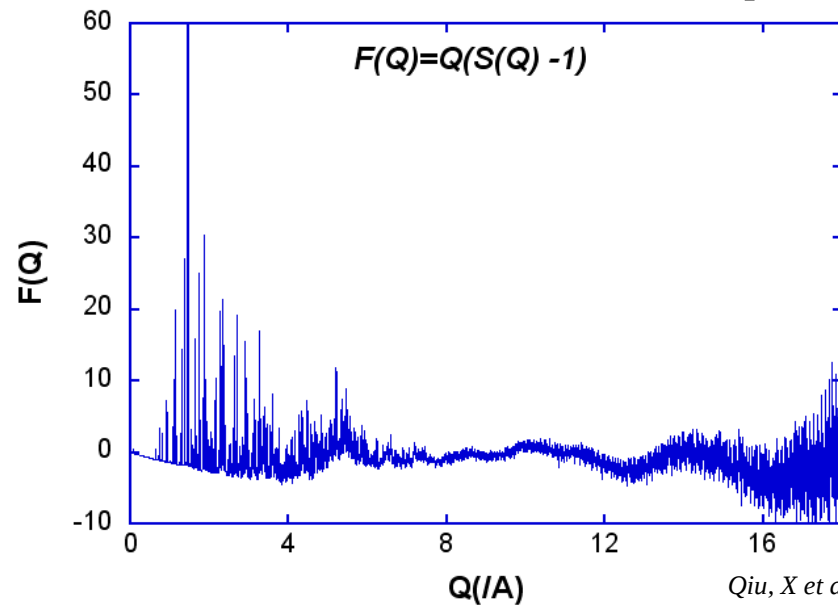
Pixel detector (XPAD)

$\lambda = 0.563 \text{ \AA}$, $E = 22 \text{ KeV}$, $2\theta_{\max} = 120^\circ$, $Q_{\max} = 18 \text{ \AA}^{-1}$



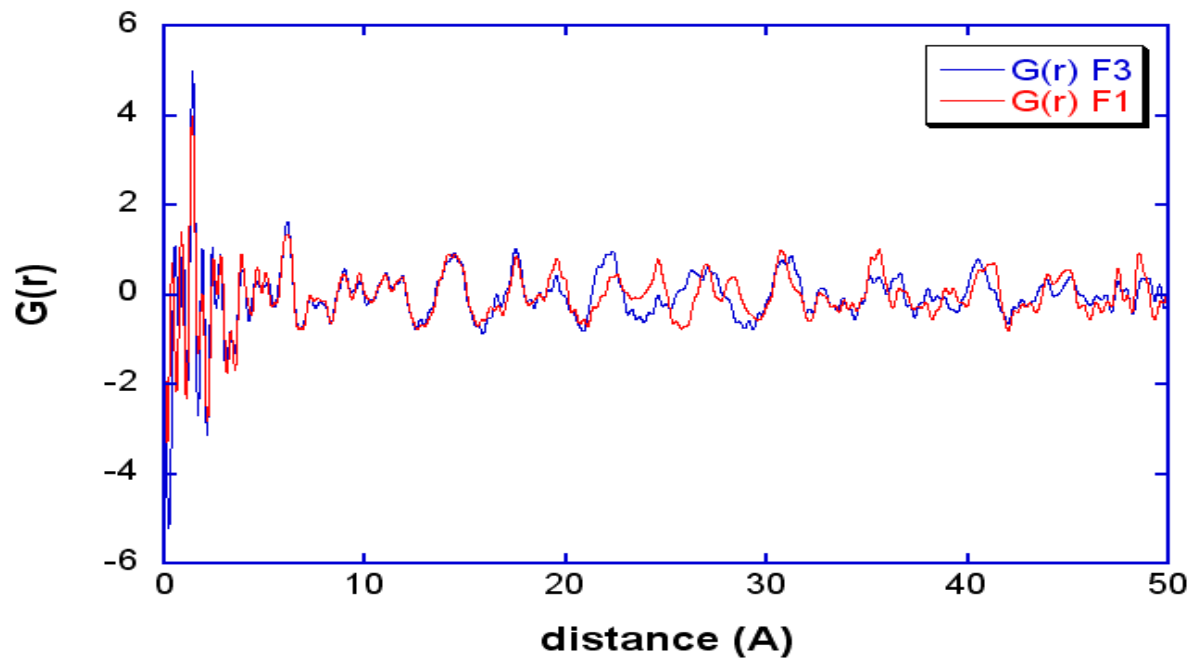


Modafinil, mesure PDF de F_I



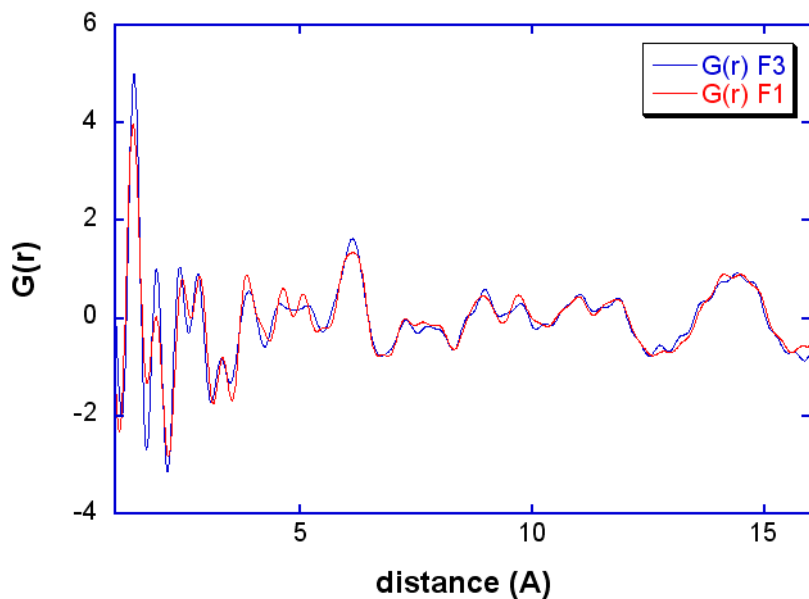
PDFGetX2

Qiu, X et al., J. Appl. Crystal. (2004), 37, 678-678

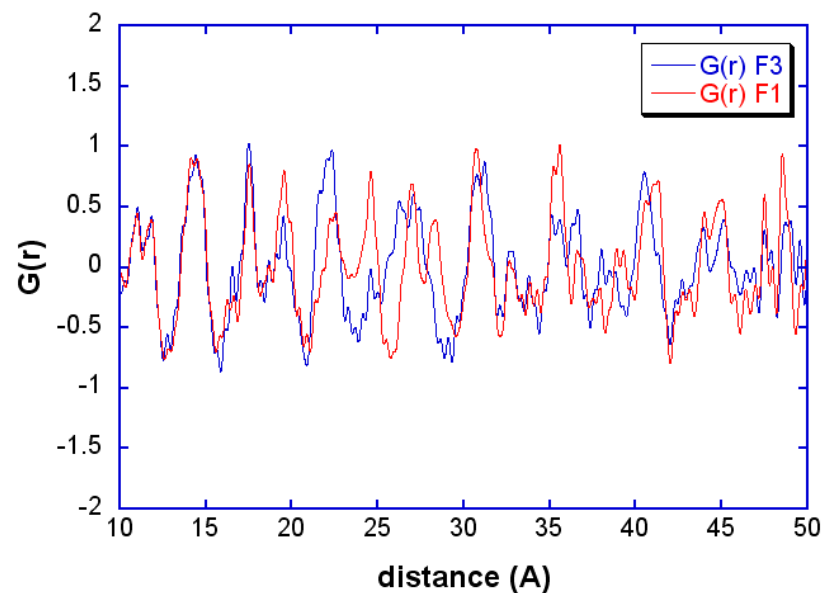


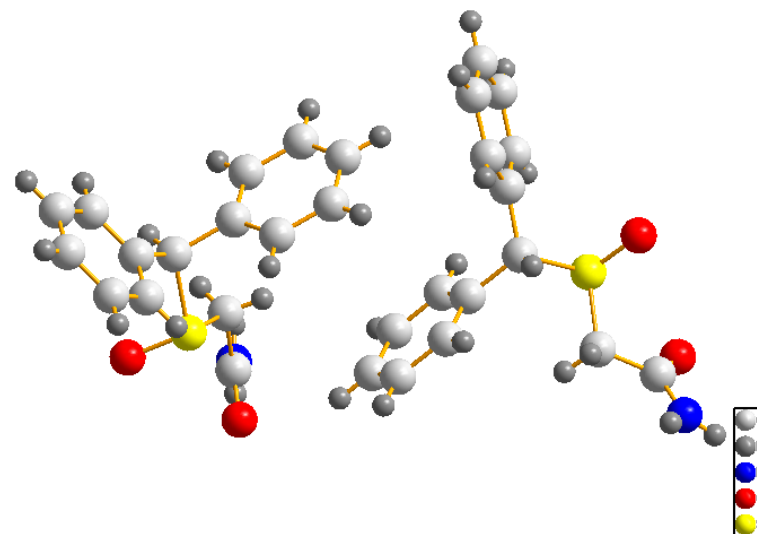
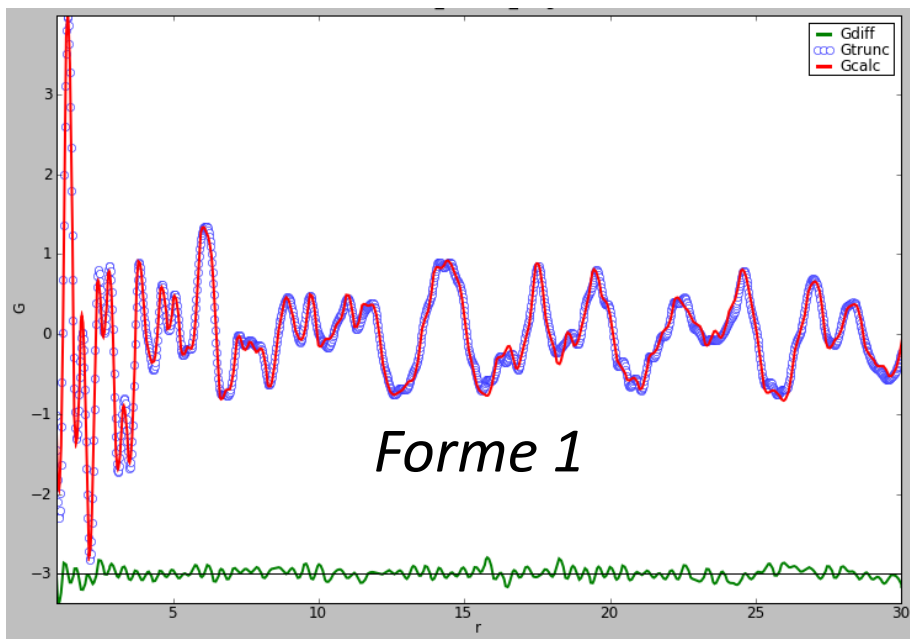
*PDF of forms 1 & 3
of modafinil*

Mêmes molécules

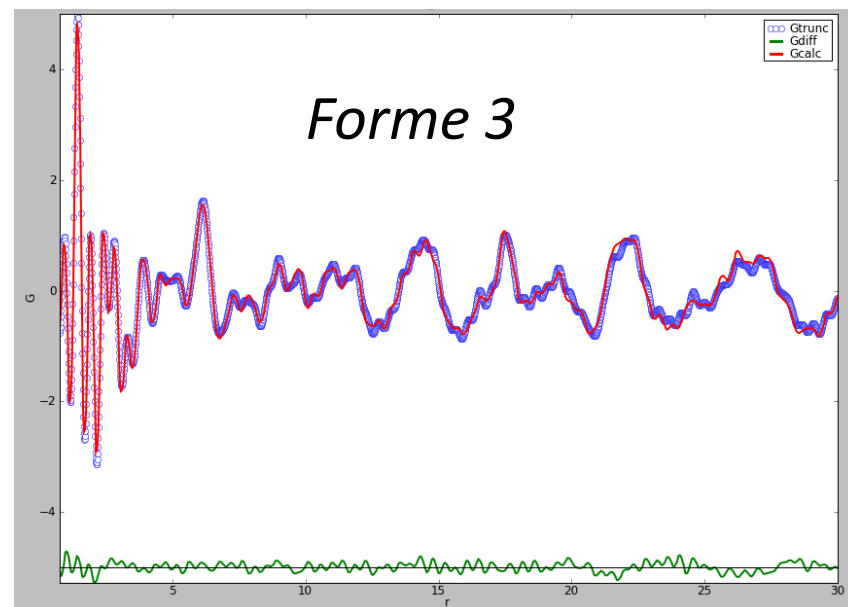


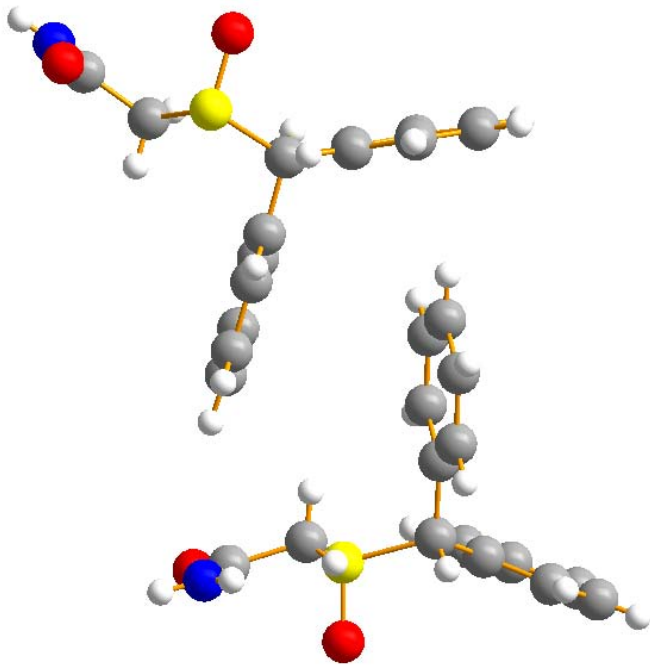
Différents arrangements



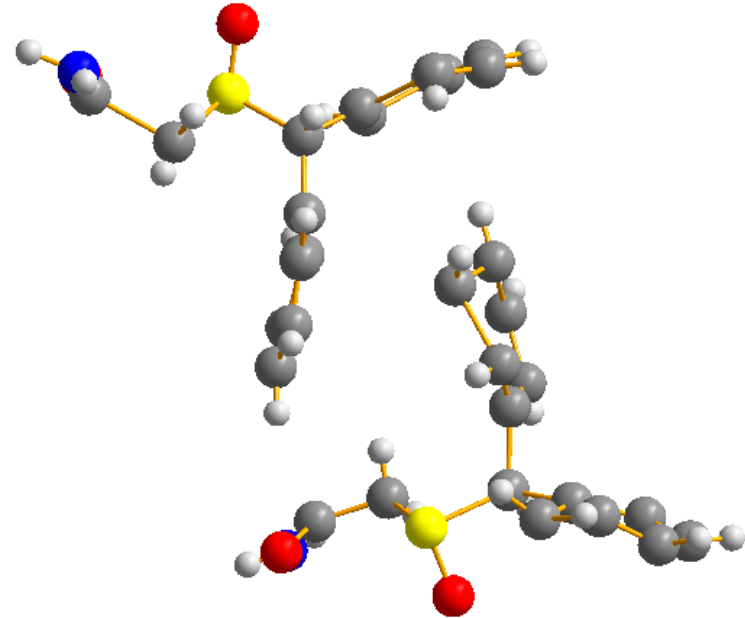


Affinements de la PDF





original



affiné

Faible écart moyen entre les 2 structures,
Trop de paramètres indépendants (115)
Nécessite un traitement en blocs rigides (positions, DW).

“amorphous” materials have a richer “PDF signature”

2 different “amorphous” compounds are hard to differentiate from their powder diffractogram

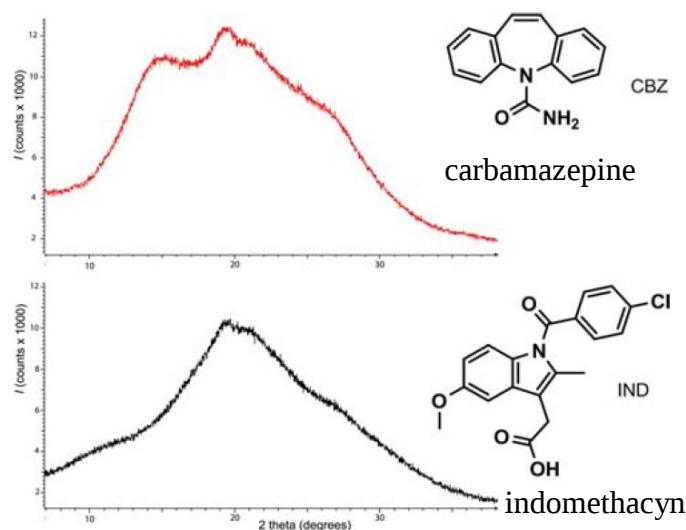


Fig. 1 Molecular structures and laboratory Cu K α_1 XRPD patterns for X-ray amorphous melt-quenched samples of CBZ (top) and IND (bottom).

An amorphous sample can be identified from its PDF by comparison with a crystalline isomorph

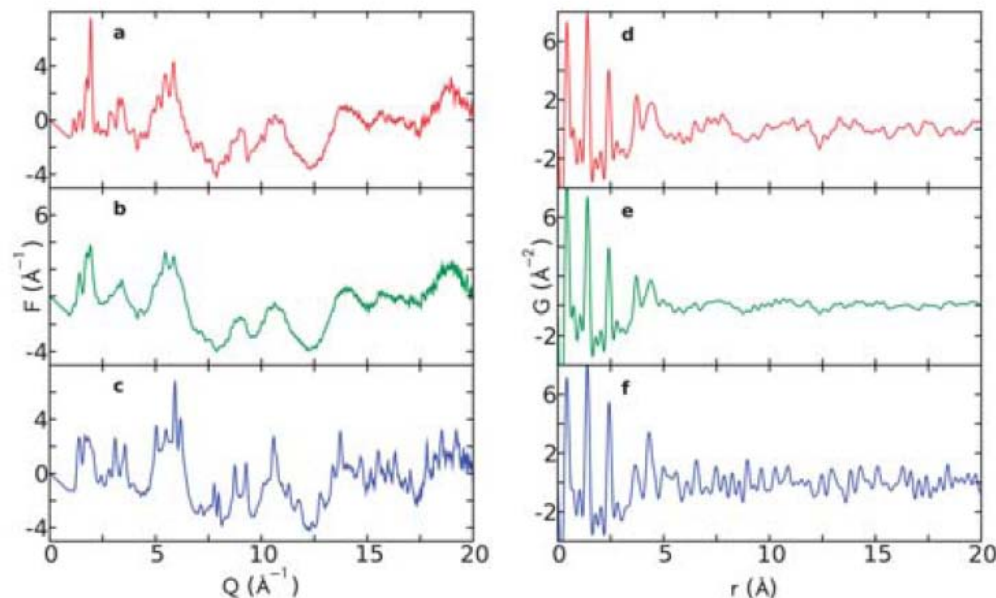


Fig. 2 Total scattering diffraction patterns and TSPDFs of CBZ. Panels (a) and (d) correspond to CBZ III, (b) and (e) to the melt-quenched sample and (c) and (f) to CBZ I; (a), (b), (c) show the total scattering data in the form of $F(Q)$ (see ESI)[†] whilst (d), (e), (f) are in the form of the TSPDF, $G(r)$.

Characterisation of amorphous and nanocrystalline molecular materials by total scattering[†]

Simon J. L. Billinge,^{a,b} Timur Dykhne,^c Pavol Juhás,^a Emil Božin,^{a,b} Ryan Taylor,^c Alastair J. Florence^a and Kenneth Shankland^a

CrystEngComm, 2010, 12, 1366–1368

⇒ Identify amorphous/nano compounds from their PDF

Requires λMo or λAg high Q PDF data

Conclusions

- ✓ La PDF peut être utilisée pour étudier la structure locale et multi-échelle
- ✓ Nécessite des données spécifique haut Q et fortes statistiques
- ✓ Structure locale $\neq$ structure moyenne, nano-clusters, désordre
- ✓ Pas de solution unique, pas d'ab initio
=> Savoir proposer un modèle
- ✓ Complémentaire des autres méthodes

Merci de votre attention !



EPDIC 13

the European Powder Diffraction conference Grenoble 28-31 October 2012

The **European Powder Diffraction Conference (EPDIC)** is the only European conference completely dedicated to all aspects of the analysis of polycrystalline materials by diffraction methods.

Started in Munich in 1991, EPDICs have rapidly become reference points for all researchers in the field and are now regarded to be ideal places for the presentation and diffusion of new developments in powder diffraction instrumentation, analysis, and applications.

EPDIC conferences are intended to be the place where all powder diffractionists, independently of whether they are more interested in the theoretical advances or in the application of the techniques, can meet and exchange ideas and experiences.

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6 plenary lectures

- 1- Nano-Imaging with X-rays.
- 2- Total Scattering Techniques
- 3- X-ray – Free Electron Lasers
- 4- Parametric Rietveld refinement.
- 5- Charge density analysis via powder diffraction
- 6- Hydrogen storage and energy related materials

12 micro-symposia

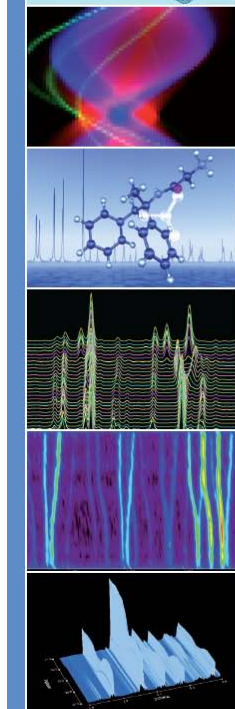
- 1- Total Scattering studies and Disorder
- 2- Ab initio Structure Solution
- 3- Powder diffraction for Biological and Molecular Materials
- 4- Combined Methods for Structure Investigation and 3-D Imaging
- 5- Materials for Sustainable Development
- 6- Progress in Instrumentation
- 7- Texture and residual stress analysis
- 8- In Situ, In Operando Studies
- 9- Nanomaterials, surfaces and Interfaces
- 10- Neutron Structural and Magnetic Scattering
- 11- Structure and Properties of Functional Materials
- 12- Advances in diffraction Line Profile Analysis.

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Minatoc Conference Center
Grenoble

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Phone : +33 (0)4 76 88 78 07
E-mail : epdic13@grenoble.cnrs.fr



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